



# Precision determinations of $|V_{cb}|$ and $|V_{ub}|$

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Probing weak interactions and  
CP violation in the quark sector  
with semileptonic B decays

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# Outline

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- Importance of testing CKM picture of ~~CP~~
- B factories – the luminosity frontier
- HQET and OPE for heavy quarks

NEW  $|V_{cb}|$  from inclusive decays ( $b \rightarrow c\ell\nu$ )

NEW  $|V_{cb}|$  from exclusive decays ( $B \rightarrow D^*\ell\nu$ )

Soon  $|V_{ub}|$  from inclusive decays ( $b \rightarrow u\ell\nu$ )

Soon  $|V_{ub}|$  from exclusive decays ( $B \rightarrow \pi\ell\nu$ )



# Weak interactions of quarks

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- Historically fruitful area of research
  - $\tau / \theta$  puzzle (1950s)
  - Parity violation (1956)
  - Flavour oscillations (1956 ( $K^0$ ), 1987 ( $B^0$ ))
  - CP violation (1964 ( $K^0$ ), 2001 ( $B^0$ ))
- The only verified mechanism for CP violation is the non-trivial phase in CKM matrix
- B factories allow precision studies of CKM
- Rare B decays offer window on new physics



# CKM matrix

- The Wolfenstein++ parameterization is used here

Buras, Lautenbacher, Ostermaier, PRD 50 (1994) 3433.

	d	s	b	
$V_{CKM}$	$1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4$	$\lambda$	$A\lambda^3(\rho - i\eta)$	u
	$-\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)]$	$1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2)$	$A\lambda^2$	c
	$A\lambda^3[1 - (\rho + i\eta)(1 - \frac{1}{2}\lambda^2)]$	$-A\lambda^2 + A(\frac{1}{2} - \rho - i\eta)\lambda^4$	$1 - \frac{1}{2}A^2\lambda^4$	t

- shown here to  $O(\lambda^5)$  where  $\lambda = \sin\theta_{12} = 0.22$
- $V_{us}$ ,  $V_{cb}$  and  $V_{ub}$  have simple forms by definition
- Free parameters  $A$ ,  $\rho$  and  $\eta$  are order unity

# A Unitarity Triangle

$\lambda$ ,  $A$ ,  $\bar{\rho}$  and  $\bar{\eta}$

At the 1% level:  $|V_{us}|$

$$\lambda = |V_{us}| = \sin \theta_c$$

$$\lambda = 0.2205 \pm 0.0018$$

At the 2% level:  $|V_{cb}|$

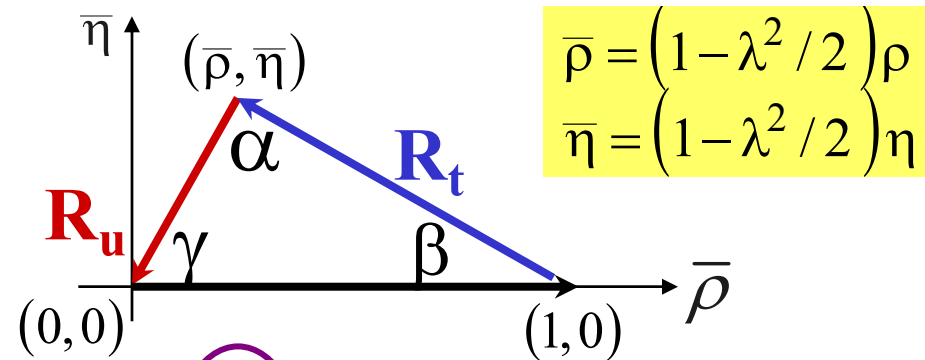
$$A = |V_{cb}| / \lambda^2$$

$$A = 0.84 \pm 0.02$$

$|V_{ub}|$  and  $|V_{td}|$

$\rightarrow \bar{\rho}-\bar{\eta}$  plane

Unitarity:  $1 + R_t + R_u = 0$



$$\bar{\rho} = \left(1 - \lambda^2 / 2\right) \rho$$

$$\bar{\eta} = \left(1 - \lambda^2 / 2\right) \eta$$

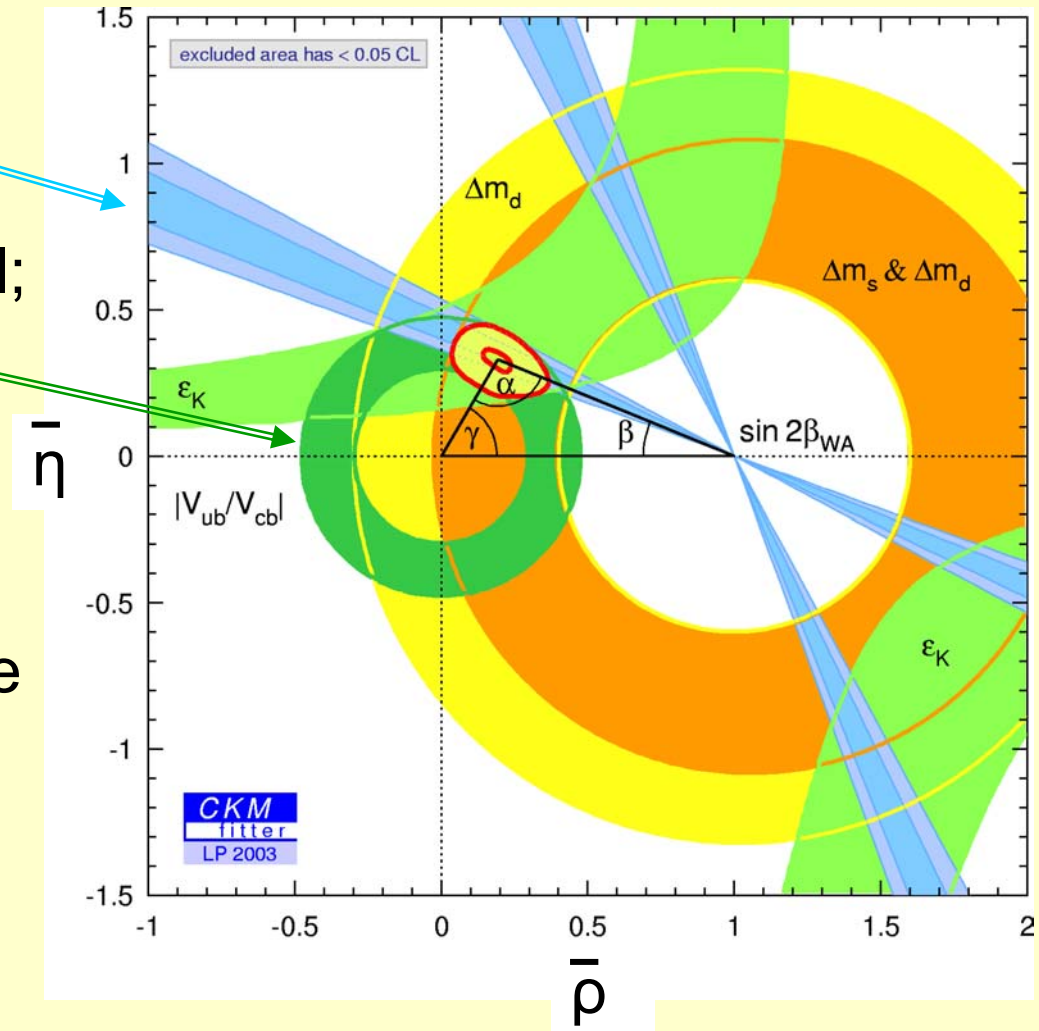
$$R_u = \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \approx -\sqrt{\bar{\rho}^2 + \bar{\eta}^2} e^{i\gamma}$$

$$R_t = \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \approx -\sqrt{(1 - \bar{\rho})^2 + \bar{\eta}^2} e^{-i\beta}$$

$$\gamma = \arg V_{ub}^*, \quad \alpha = \pi - \gamma - \beta$$

# Constraints on CKM

- Good precision (and improving) on  $\sin 2\beta$
- $|V_{ub}|/|V_{cb}|$  is powerful; improvements will have impact
- These two measurements alone could show a violation of unitarity





# B factories

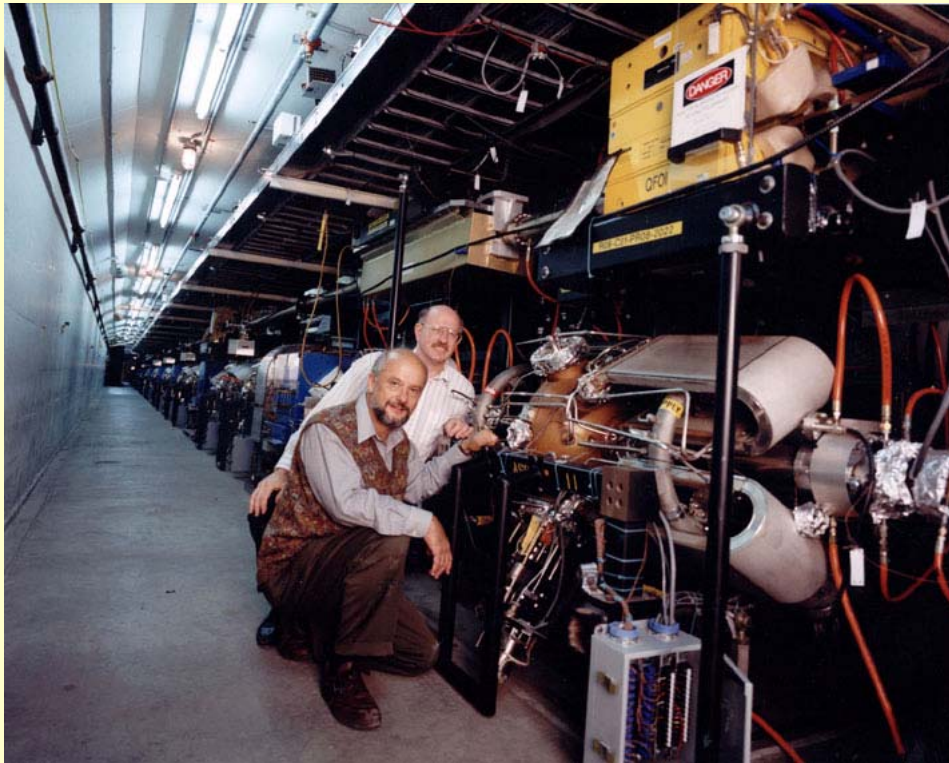
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- PEP-II/BaBar and KEK-B/Belle
  - Asymmetric  $e^+e^-$  colliders,  $\sqrt{s} = 10.58$  GeV
  - Approved in 1994, first data in 1999
  - CP violation observed in 2001
  - Luminosity records continue to be set
- *Two big success stories*
  - Focus of *this talk* is on BaBar
  - Belle results will be mentioned where relevant



# PEP-II and KEK-B

Asymmetric  $e^+e^-$  colliders

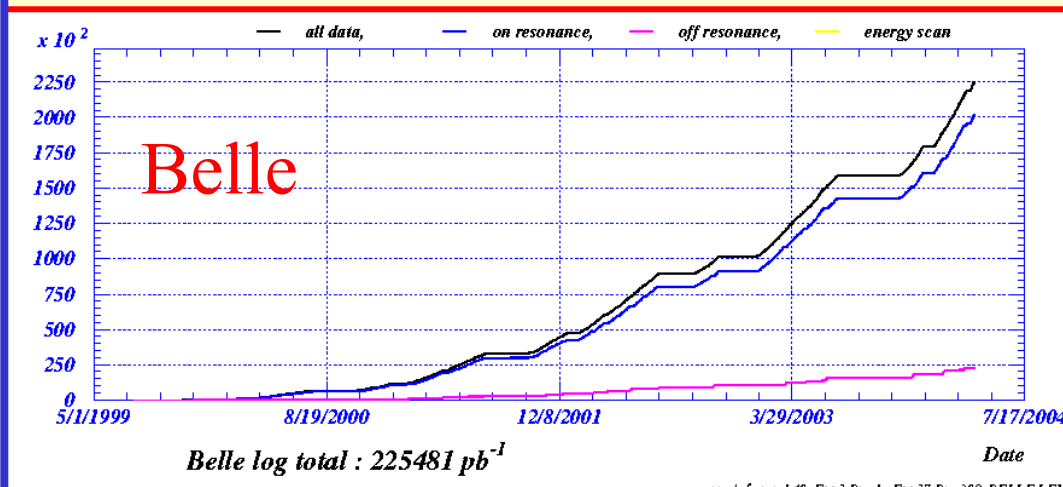
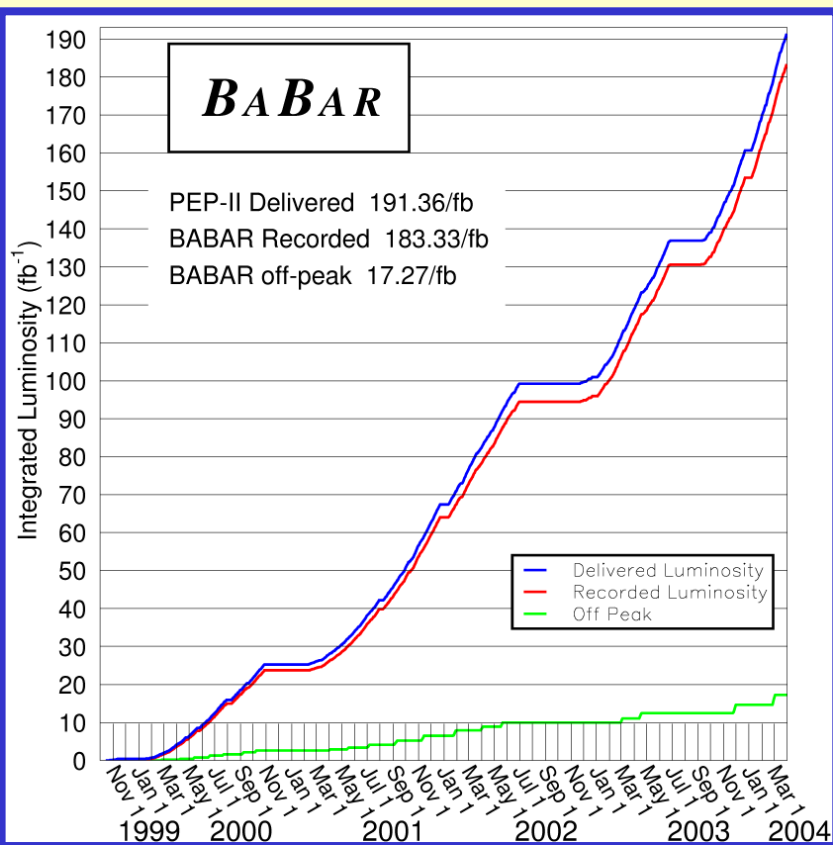




# Luminosity (as of April 7, 2004)

Both B factories are running extremely well:

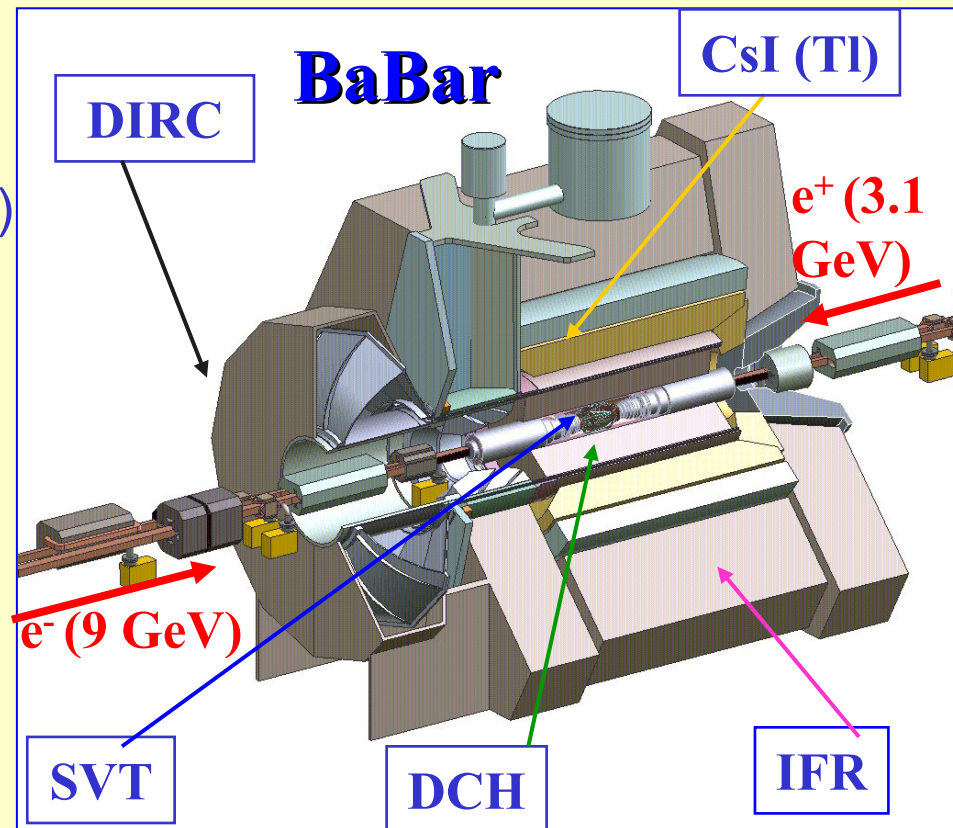
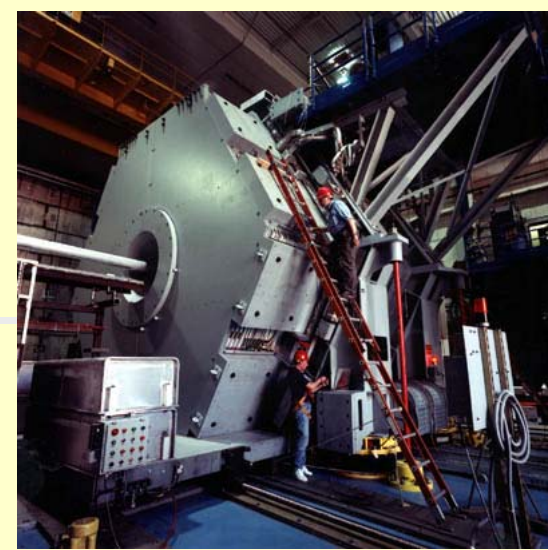
	Belle	BaBar
$\mathcal{L}_{\max}$ ( $10^{33}/\text{cm}^2/\text{s}$ )	12.0	8.3
best day ( $\text{pb}^{-1}$ )	880	622
total ( $\text{fb}^{-1}$ )	222	184



# BaBar detector

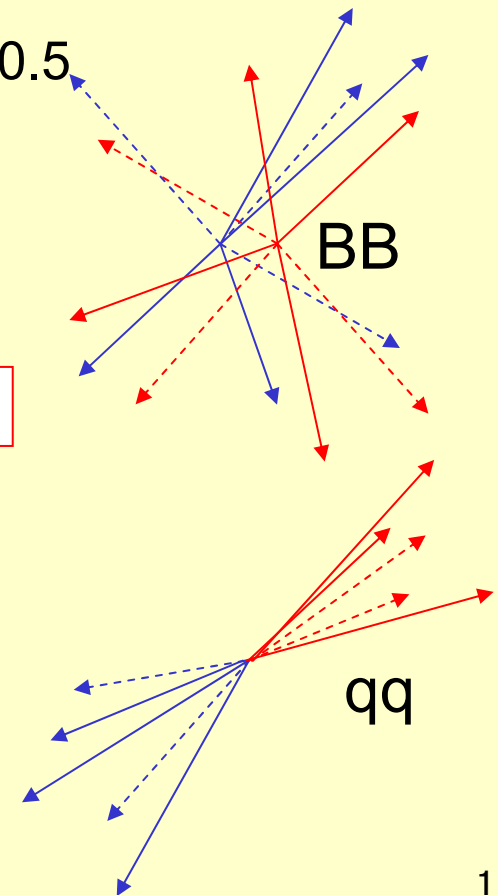
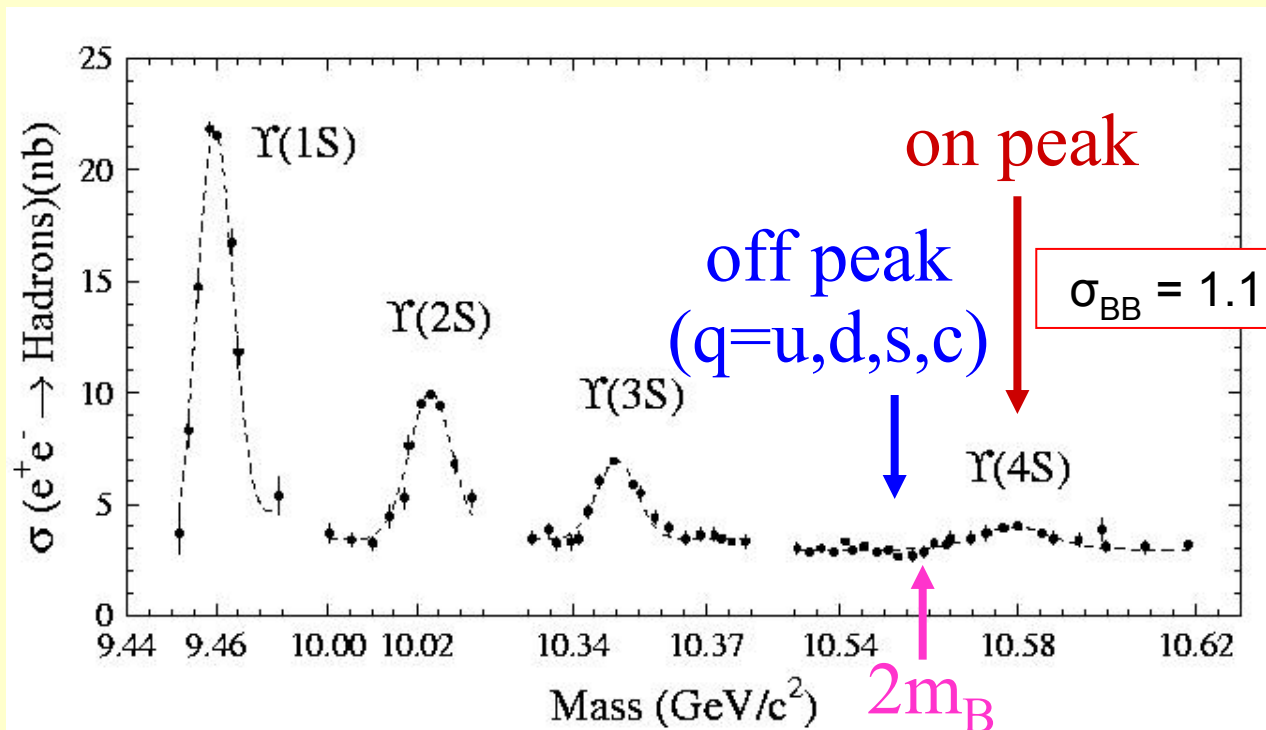
- General purpose collider detector
- F-B asymmetric due to boost of CM
- Crossings every  $n \cdot 4.2$  ns
- Standalone 5-layer Si tracker for low- $p_T$  ( $< 0.1$  GeV)
- Low-mass drift chamber with He-isobutane gas
- Unique ultra-thin imaging Cherenkov detector
- CsI(Tl) crystal calorimeter
- Instrumented flux return

increasing radius



# Y(4S) experiments

- $e^+e^- \rightarrow Y(4S) \rightarrow B^+B^-$  and  $B^0B^0 \sim 50\%$  each
- B nearly at rest ( $\beta\gamma \sim 0.06$ ) in 4S frame  $\rightarrow$  overlapping decays
- Asymmetric beam energies boost into lab:  $(\beta\gamma)_{4S} \sim 0.5$





# Understanding B decay

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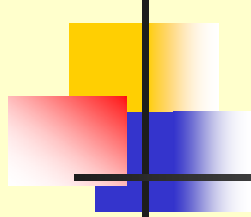
- b quark weak decay is complicated by QCD
- Both perturbative ( $m_b$ ) and non-perturbative ( $\Lambda_{\text{QCD}}$ ) effects
- Tools:
  - Heavy quark symmetry
    - Heavy Quark Effective Theory
    - Operator Product Expansion (HQE effective field theory)
  - Lattice QCD



# Heavy Quark Symmetry

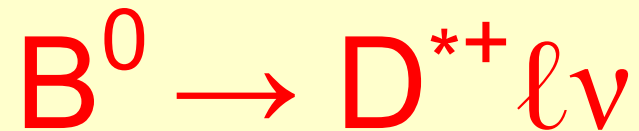
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- Heavy quark is “invisible” to gluon probes with de Broglie wavelength  $\lambda_g \gg 1/m_Q$ 
  - HQ spin and mass (flavour) are good symmetries as  $m_Q / \Lambda_{\text{QCD}} \rightarrow \infty$
  - Departures from HQ symmetry can be expressed as  $(\Lambda_{\text{QCD}} / m_Q)^n$  corrections
  - In several important cases, the  $(\Lambda_{\text{QCD}} / m_Q)^1$  term vanishes (Luke’s theorem)



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$|V_{cb}|$  from exclusive  
 $b \rightarrow c \ell \nu$  decays:





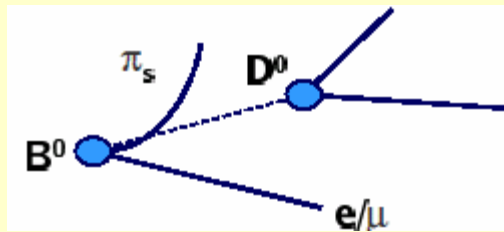
# Heavy Quark Effective Theory

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- Based on HQ symmetry for  $Q \rightarrow Q'$ 
  - Applies to  $b \rightarrow c$  transitions, e.g.  $B \rightarrow D^* \ell \nu$
  - Departures from HQ limit  $\sim (\Lambda_{\text{QCD}} / m_c)^k$
- All  $B \rightarrow D^{(*)} \ell \nu$  transitions are governed by *one form factor* (the Isgur-Wise function  $\xi(w)$ ,  $w = v_B \cdot v_{D^*} \geq 1$ ) in the HQ limit
  - In HQ limit,  $\mathcal{F}(1) = \xi(1) = 1$  ( $D^*$  at rest in B rest frame)
  - Extract  $\mathcal{F}(1) |V_{cb}|$  from rate  $d\Gamma/dw$  ( $w \rightarrow 1$ )
  - Calculate  $\mathcal{F}(1)$  using non-perturbative methods



# $B \rightarrow D^* \ell \nu$

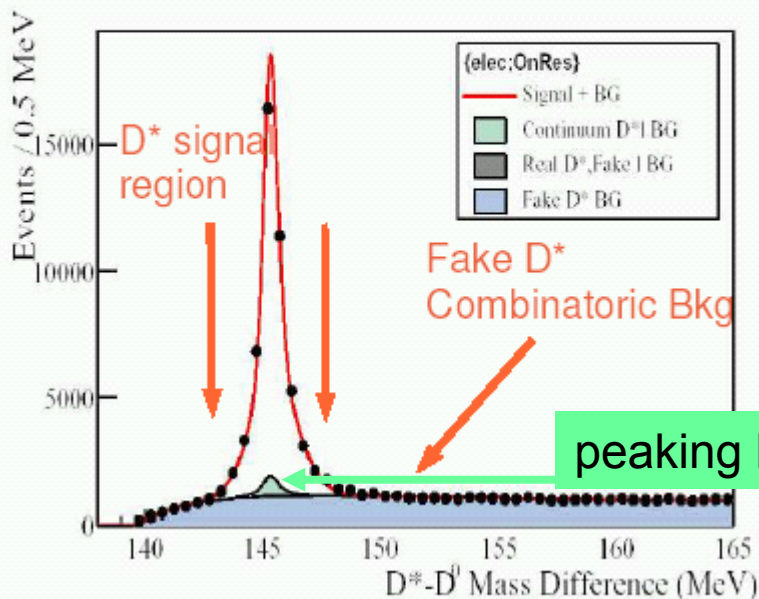


## Sample of $B^0 \rightarrow D^{*-} \ell^+ \nu$

- $D^{*-} \rightarrow D^0 \pi^-$  soft
- $D^0 \rightarrow K\pi, K3\pi, K\pi\pi^0$
- High energy lepton:  $e$  &  $\mu$   $P_T > 1.2$  GeV/c

\* **Combinatorial background:**

subtracted using the  $\Delta M$  side band



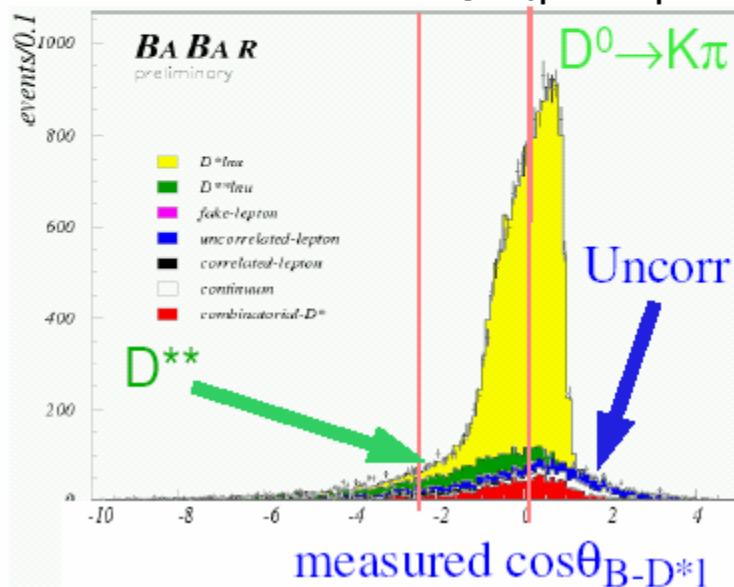
Separate fit in each  $w$  bin

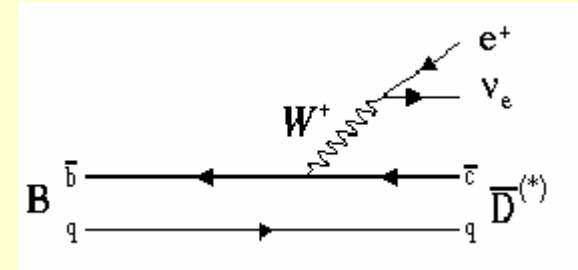
\*  $B_1 \rightarrow D^* X, B_2 \rightarrow \ell \nu$  (uncorrelated)

\*  $B \rightarrow D^* X \ell \nu$  ( $D^{**}$  background)

separated fitting  $\cos\theta_{B-D^*l}$

$$\cos\theta_{B, D^* l} \equiv \frac{2 E_B E_{D^* l} - m_B^2 - m_{D^* l}^2}{2 |\vec{p}_B| |\vec{p}_{D^* l}|}$$





- Measure differential decay rate ( $w = D^*$  boost in B frame [1-1.5])

$$\frac{d\Gamma(B \rightarrow D^* \ell \nu)}{dw} = \frac{G_F^2}{48\pi^3} \mathcal{G}(w) |V_{cb}|^2 (\mathcal{F}(w))^2 \quad \text{extrapolate to } w=1$$

- In HQ limit  $\mathcal{F}(w) \rightarrow \xi(w)$ . In HQET parameterize as

expansion in  $(1-w)$

$$\mathcal{F}(w) = \mathcal{F}(1) \left( 1 + \rho_F^2 (1-w) + c(1-w)^2 + \dots \right) \quad \text{or}$$

$$\mathcal{F}^2(w) = \frac{\mathcal{A}_1^2(w)}{1 + \frac{4w}{1+w} \frac{1-2wr+r^2}{(1-r)^2}} \left\{ 2 \frac{1-2wr+r^2}{(1-r)^2} \left[ 1 + \frac{w-1}{w+1} R_1^2(w) \right] + \left[ 1 + \frac{w-1}{1-r} (1 - R_2(w)) \right]^2 \right\} \quad \text{with}$$

$$R_1(w) \propto \frac{V(w)}{A_1(w)} \quad \text{and} \quad R_2(w) \propto \frac{A_2(w)}{A_1(w)} \quad \text{and} \quad r = \frac{m_{D^*}}{m_{B^0}}$$

$$\mathcal{A}_1(w) = \mathcal{A}_1(1) \left[ 1 - 8\rho_{\mathcal{A}_1}^2 z + (53\rho_{\mathcal{A}_1}^2 - 15)z^2 - (231\rho_{\mathcal{A}_1}^2 - 91)z^3 \right] \quad \text{with } z = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}$$

expansion in  $z$

# B → D\* ℓ ν (preliminary results)

- High statistics sample
- w resolution ~ 0.04

$$\mathcal{F}(1)|V_{cb}| = (34.03 \pm 0.24_{\text{stat}} \pm 1.31_{\text{syst}}) \times 10^{-3}$$

$$\rho^2 = 1.23 \pm 0.02_{\text{stat}} \pm 0.28_{\text{syst}}$$

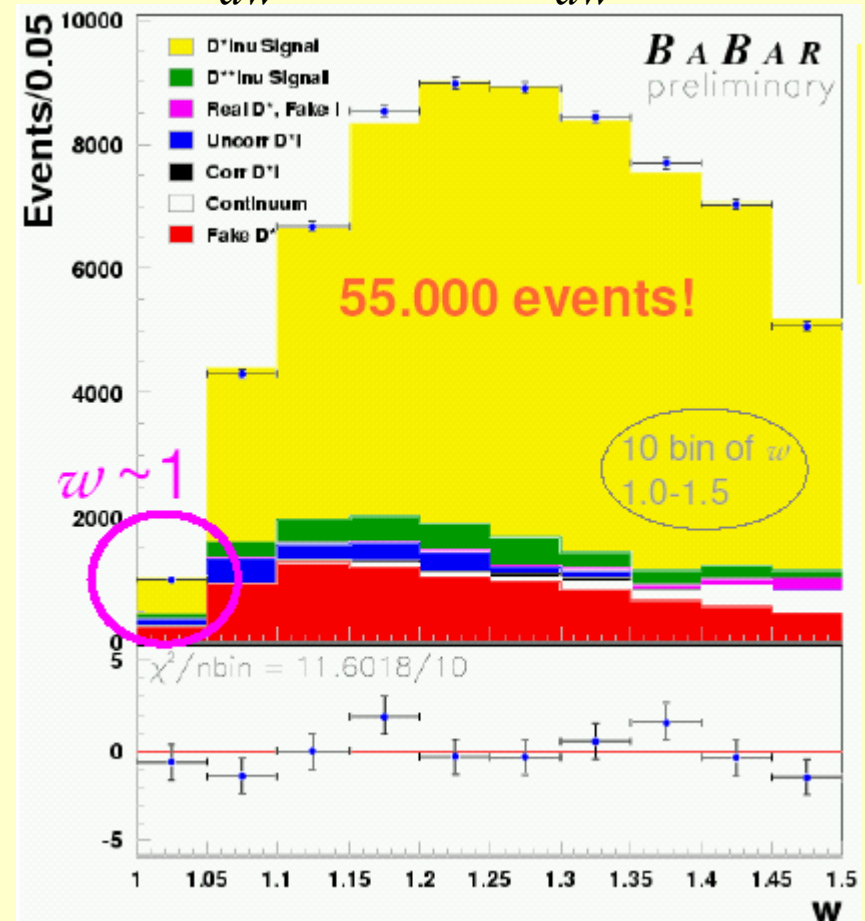
$$\text{Br}(B^0 \rightarrow D^* \ell \nu) = (4.69 \pm 0.02_{\text{stat}} \pm 0.24_{\text{syst}})\%$$

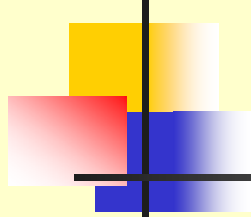
- Main uncertainties from FF ratios  $R_1$  and  $R_2$ , extrapolation to  $w=1$ ,  $D^{**}$  composition, slow  $\pi^+$  efficiency
- Using  $\mathcal{F}(1) = 0.92 \pm 0.03$  (from LQCD<sup>1</sup>)

$$|V_{cb}| = (37.27 \pm 0.26_{\text{stat}} \pm 1.43_{\text{syst}}^{+1.50}_{-1.20}) \times 10^{-3}$$

<sup>1</sup>S. Hashimoto *et al.*, PRD **66** (2002) 014503

$$\frac{dN}{dw} = \varepsilon(w) \frac{dB(B^0 \rightarrow D^* \ell \nu)}{dw}$$

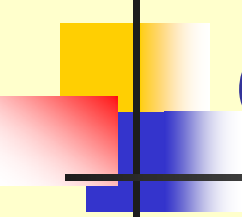




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$|V_{cb}|$  from inclusive  
 $b \rightarrow c \ell \nu$  decays

$$B \rightarrow X_c \ell \nu$$



# OPE for $b \rightarrow c \ell \nu$ transitions

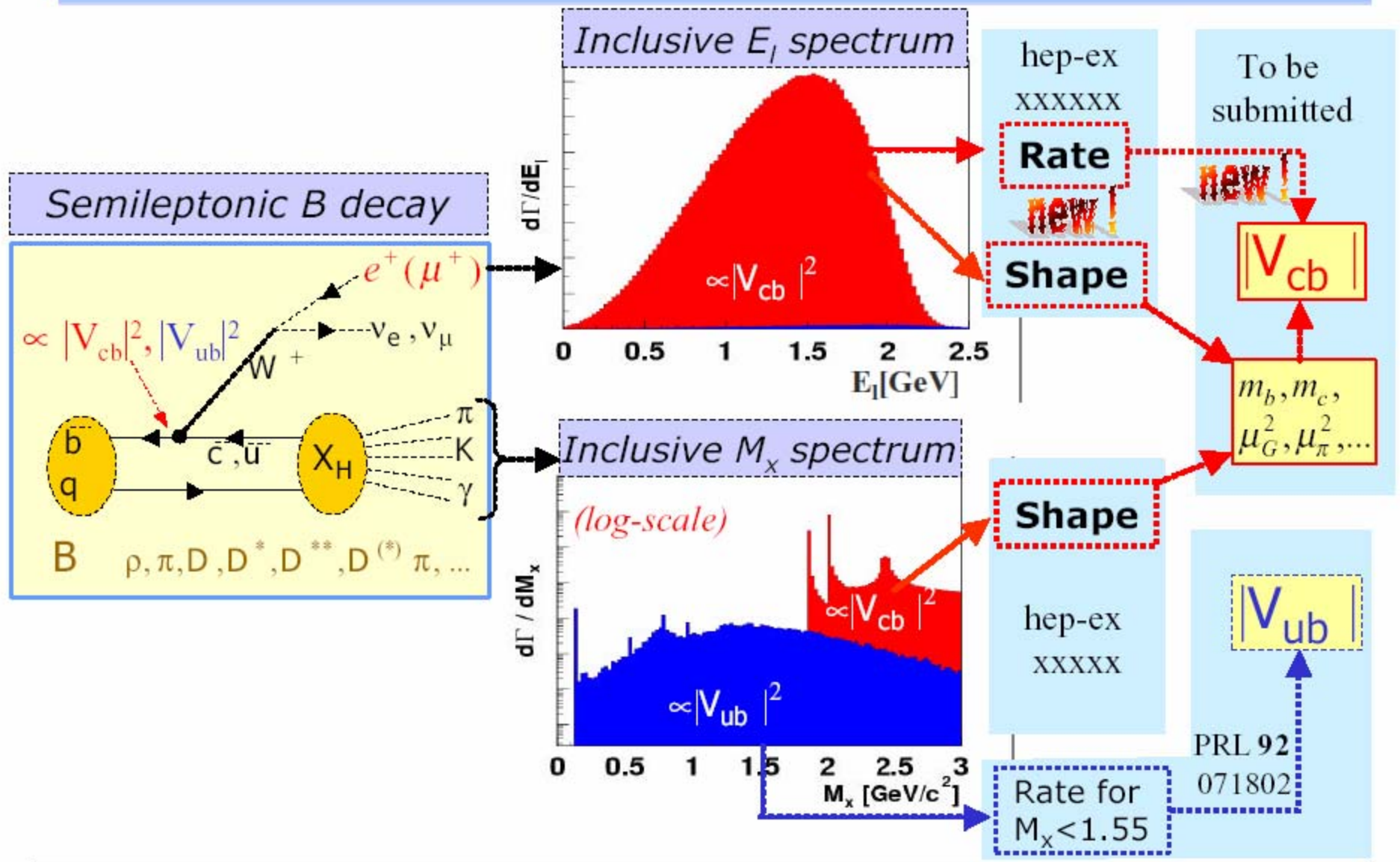
- $b \rightarrow c \ell \nu$  described by OPE in  $(1/m_b)^n$  and  $\alpha_s^k$

$$\Gamma(B \rightarrow X_c \ell \nu) = 1.014 \frac{G_F^2 m_b^5}{192 \pi^3} |V_{cb}|^2 \left[ z_0(r) \left[ 1 + A_3^{pert}(r, \mu) \left( 1 - \frac{\mu_\pi^2 - \mu_G^2}{2m_b^2} \right) - (1 + A_5^{pert}(r, \mu)) 2(1-r)^4 \frac{\mu_G^2}{m_b^2} + O\left(\frac{1}{m_b^3}\right) \right] \right]$$

$\mu = 1 \text{ GeV}/c$ , scale which separates effects from long- and short-distance dynamics  
 $r = m_b/m_c$ ,  $z_0$  = tree-level phase space factor,  $A^{pert}$  = pert. corrections ( $\alpha_s, \alpha_s^2 \beta_0$ )

- non-perturbative parameters arise at each order:
  - $\Lambda$  ( $=m_B - m_b$ )
  - $\mu_\pi^2$  (aka  $\lambda_1$ ),  $\mu_G^2$  (aka  $\lambda_2$ ) at  $(1/m_b^2)$
  - $\rho_{1-2}, \mathcal{T}_{1-4}$  at  $(1/m_b^3)$  ...
- parton-hadron duality assumed
- predicts many observables  $\rightarrow$  testable

# The Big Picture





# Spectral moments: $\langle M_X^k \rangle$ , $\langle E_e^k \rangle$

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- Measure hadronic mass and lepton energy moments (in presence of minimum lepton energy cut)

- Compare with OPE calculation

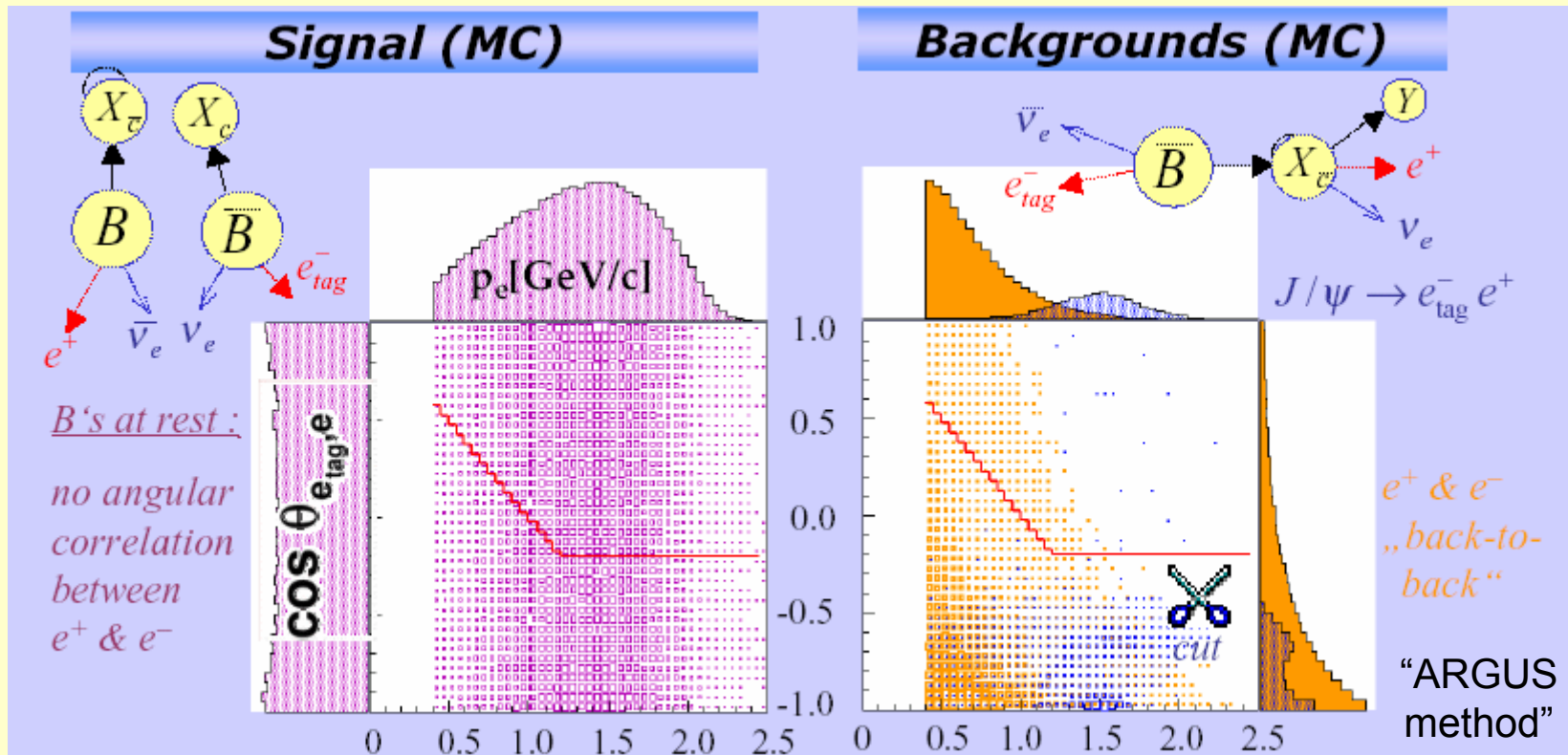
Calculations available to  $O(m_B^{-3})$  and  $O(\alpha_S^k)$ ,  $k = 1$  or  $2$

- Applying OPE calculations to real hadrons (duality) requires summing over a “large enough” phase space
- Spectral *moments* should be insensitive to duality
- A complete set of calculations is available in one renormalization scheme (soon to come in a second scheme)



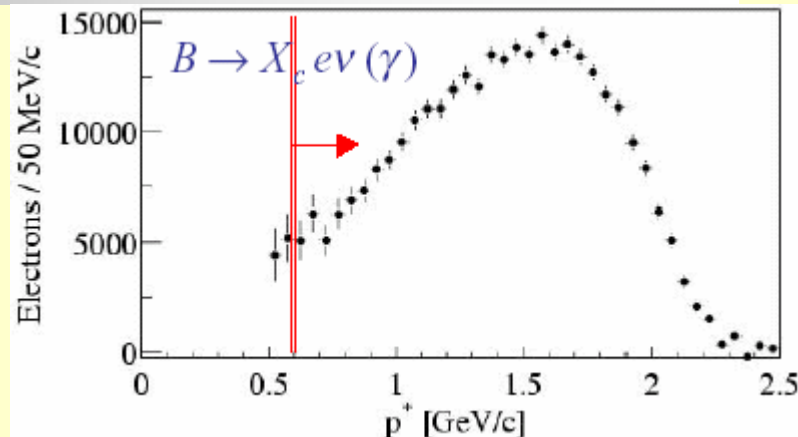
# Electron spectrum measurement

- Exploit angular correlations in di-electron events
- Extract partial BF and moments, compare with theory



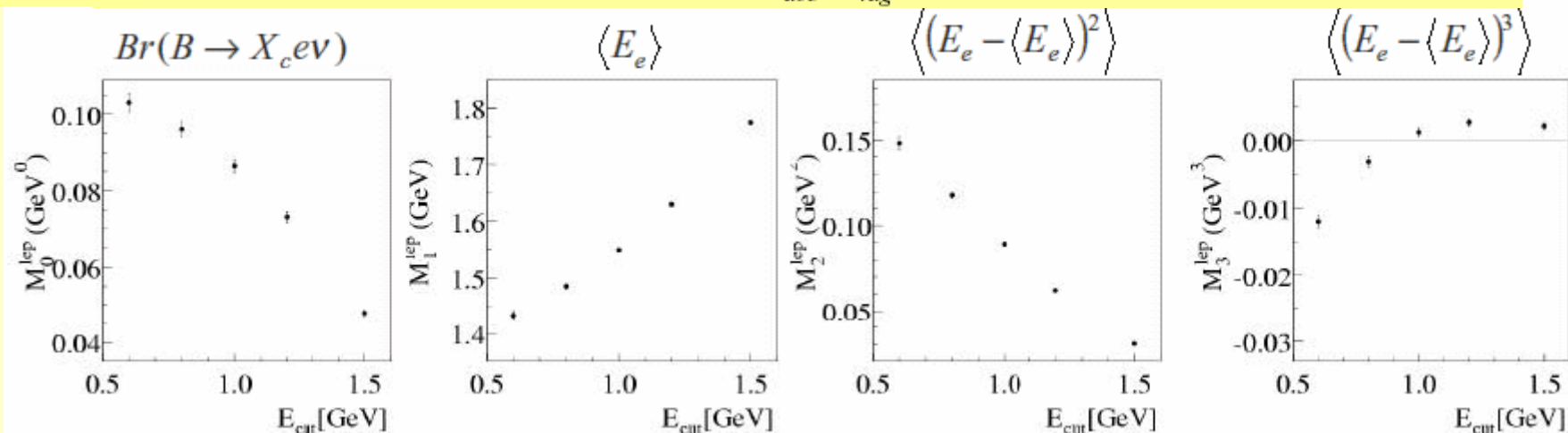
# Electron energy moments

- Correct for BB mixing,  $b \rightarrow uev$ , backgrounds, Bremsstrahlung, QED radiation, elec id and misid...
- Extract 0<sup>th</sup> – 3<sup>rd</sup> moments vs  $E_{e,cut}$



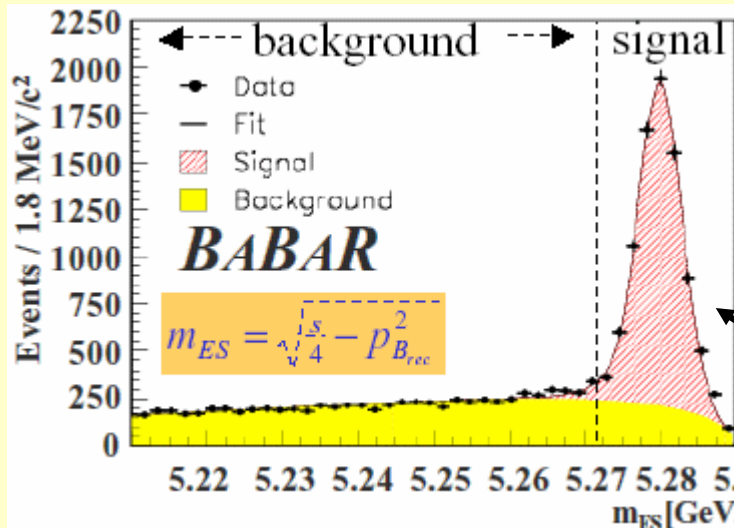
partial  
BF:

$$Br(B \rightarrow X_e v(\gamma), E_e > 0.6 \text{ GeV}) = \frac{N_{b \rightarrow xev}(E_e > 0.6 \text{ GeV})}{\epsilon_{acc} N_{tag}} = (10.36 \pm 0.06_{stat} \pm 0.23_{sys})\%$$



# Measuring $M_X$ in $b \rightarrow c\ell\nu$ decays

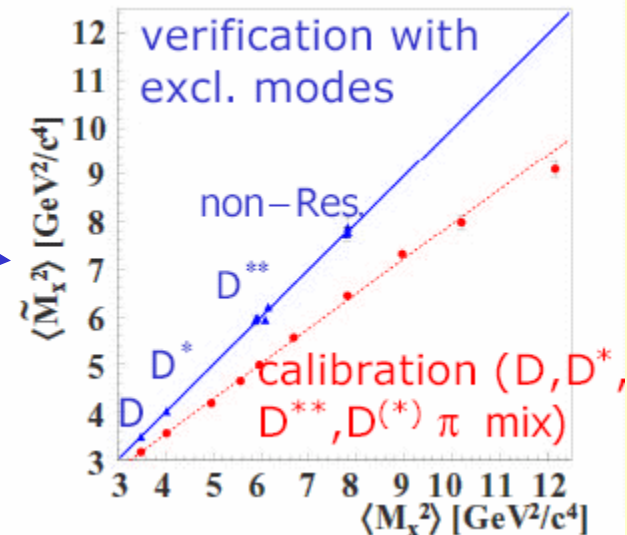
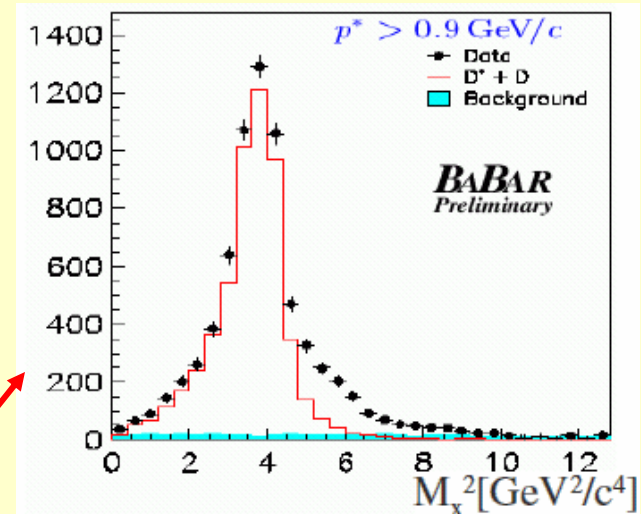
- Analysis strategy: fully reconstruct one B and study semileptonic decays of the recoiling B
  - Require  $E_{\text{miss}} \approx |p_{\text{miss}}|$
  - kinematic constraints  $\rightarrow$  fit for better  $m_X$  resolution ( $\sigma \sim 0.35$  GeV)
  - B-factory statistics make it possible



Recoil  $M_X^2$

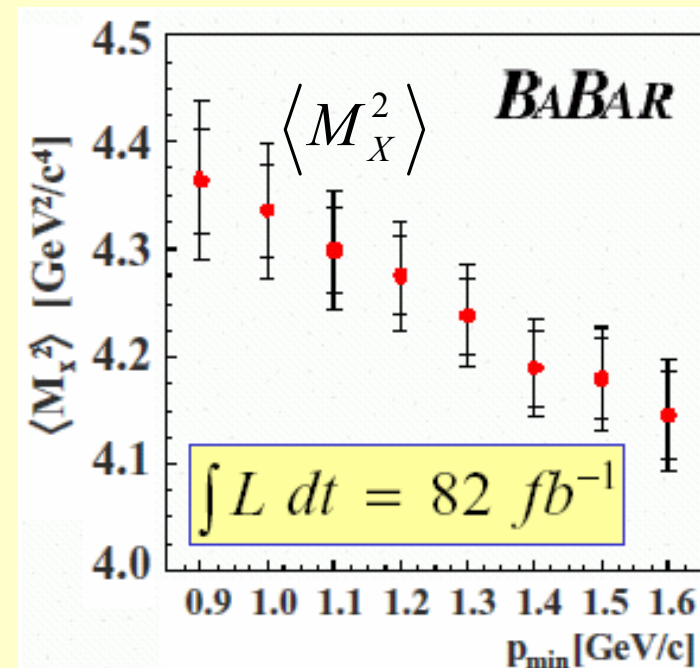
$M_X$  calibration curve, applied event-by-event

Fully reconstructed



# Hadronic mass moments

- Method validated on data using partially-reconstructed  $D^* \ell \nu$  decays ( $\pi_s$ - $\ell$  correlations)
- Extract  $\langle M_X^k \rangle$ ,  $k=1..4$  as a function of  $E_{e,\text{cut}}$
- Main systematic uncertainties:
  - non  $b \rightarrow c \ell \nu$  background
  - simulation of track and neutral reconstruction
  - modeling of QED radiation
  - B-reco sideband subtraction





# Fit to moments

- Fit  $E_e$  and  $M_X$  moments vs.  $E_0$  to set of parameters:
  - $|V_{cb}|$ ,  $\mathcal{B}(b \rightarrow c\ell\nu)$ ,  $m_b$ ,  $m_c$ ,  $\mu_\pi^2$ ,  $\mu_G^2$ ,  $\rho_D^3$ ,  $\rho_{LS}^3$
  - 8 unknowns, 25-35 observables (with reasonable correlations)

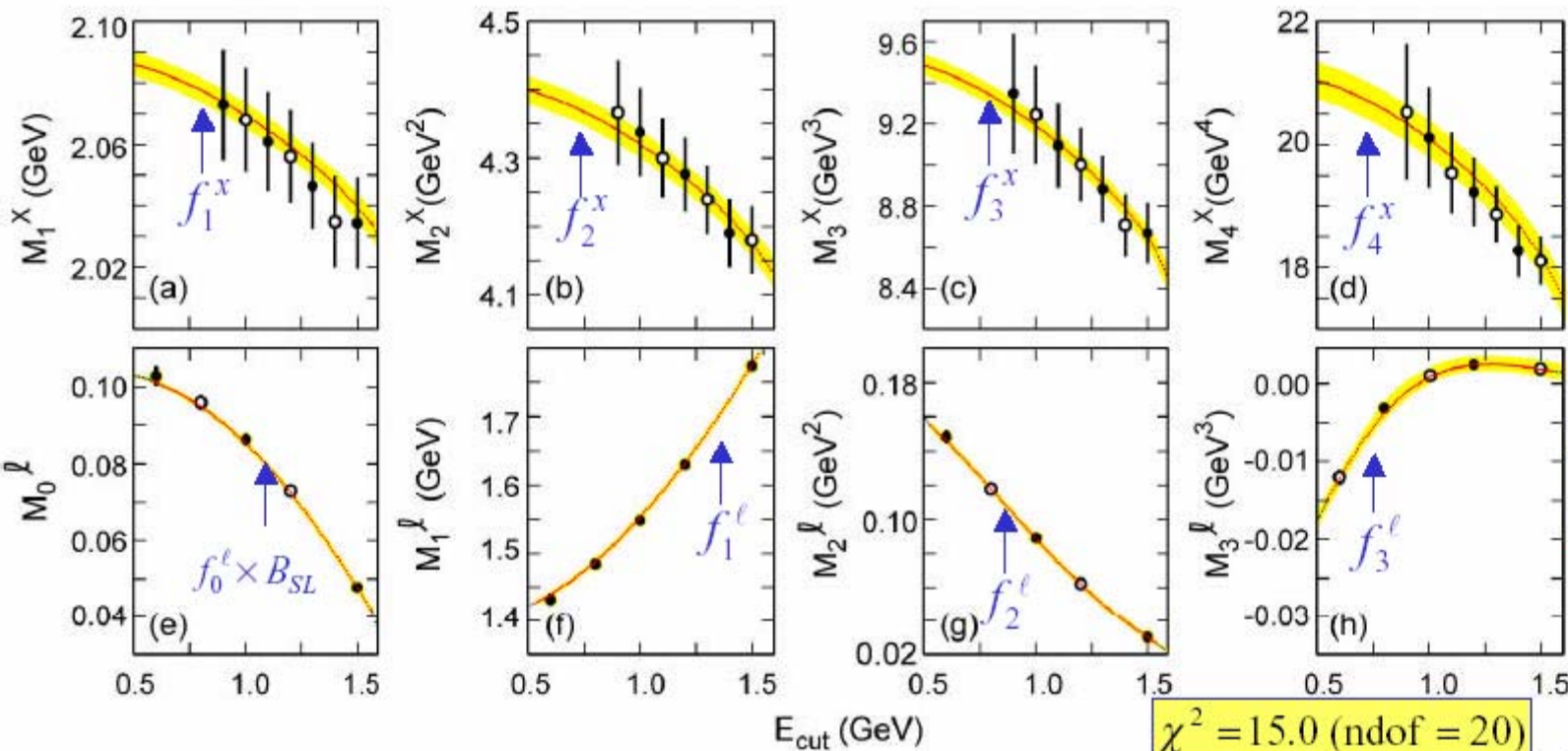
>  $|V_{cb}|$  „master“ formula :  $|V_{cb}|^2 = Br(B \rightarrow X_c e \nu) / \tau_B f_\Gamma^\ell(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_{LS}^3, \rho_D^3)$   
 >  $Br(B \rightarrow X_c e \nu, E_l > E_0)$  :  $M_0^\ell(E_0) / Br(B \rightarrow X_c e \nu) = f_0^\ell(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_{LS}^3, \rho_D^3)$   
 > i-th central  $E_l$  moment for  $E_l > E_0$ :  $M_i^\ell(E_0) = f_i^\ell(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_{LS}^3, \rho_D^3)$  ( $i = 1..3$ )  
 > i-th  $M_X$  moment and  $E_l > E_0$ :  $M_i^X(E_0) = f_i^X(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_{LS}^3, \rho_D^3)$  ( $i = 1..4$ )

- cross-check lepton vs. hadron moments
- compare  $|V_{cb}|$  with  $D^*\ell\nu$  result
- compare non-perturbative parameters with other determinations



# Combined Fit to $E_1$ and $M_x$ Moments

	$ V_{cb} (10^{-3})$	$m_b$ (GeV)	$m_c$ (GeV)	$\mu_\pi^2$ ( $\text{GeV}^2$ )	$\rho_D^3$ ( $\text{GeV}^3$ )	$\mu_G^2$ ( $\text{GeV}^2$ )	$\rho_{LS}^3$ ( $\text{GeV}^3$ )	$B_{c\ell\nu}$ (%)
Results	41.390	4.611	1.175	0.447	0.195	0.267	-0.085	10.611
$\delta_{exp}$	0.437	0.052	0.072	0.035	0.023	0.055	0.038	0.163
$\delta_{HQE}$	0.398	0.041	0.056	0.038	0.018	0.033	0.072	0.063
$\delta_{\alpha_B}$	0.150	0.015	0.015	0.010	0.004	0.018	0.010	0.000
$\delta_\Gamma$	0.620							
$\delta_{tot}$	0.870	0.068	0.092	0.053	0.029	0.067	0.082	0.175



Calculations taken from Gambino and Uraltsev, hep/ph 0401063

high correlation between measurements :  
 $\Rightarrow$  this fit uses solid points only

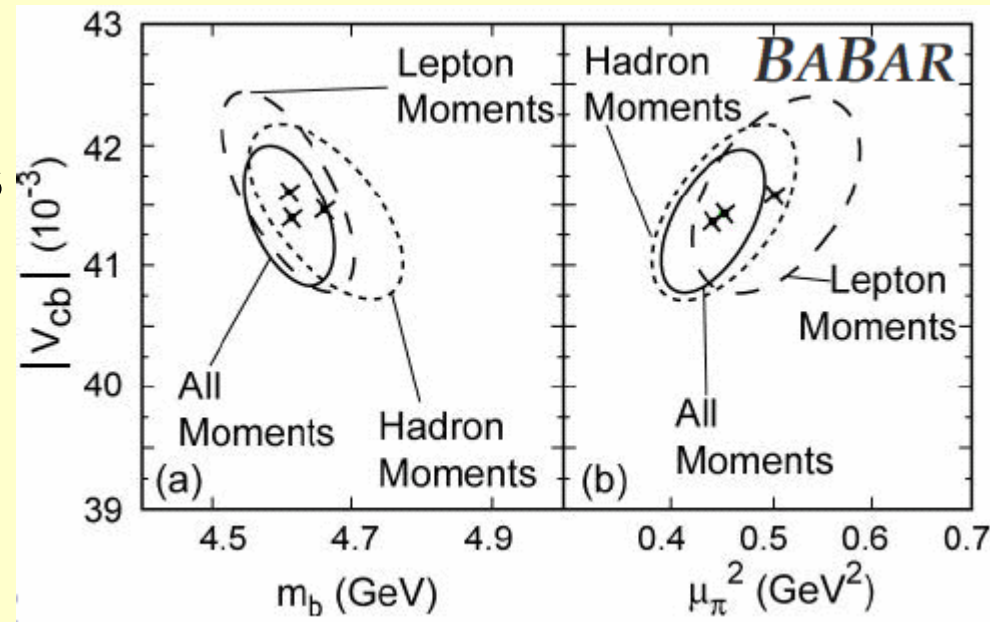
$$\chi^2 = 15.0 \text{ (ndof} = 20)$$

# Cross-checks of fit results

- $E_e$  moments calculated up to  $\alpha_s^2\beta_0$ ;  $M_X$  moments to  $\alpha_s$  (higher orders small compared with exp error)

- **Separate fits to  $E_e$  and  $M_X$  moments agree well**

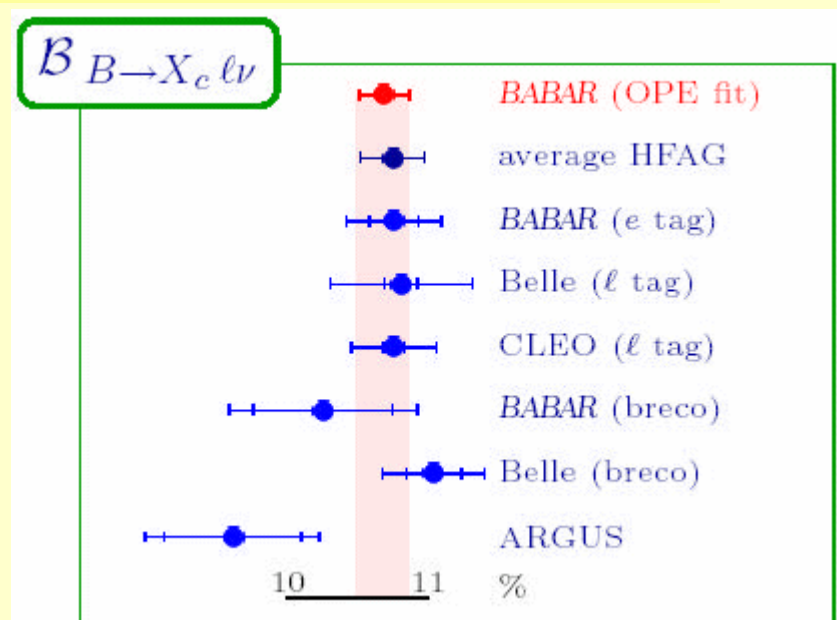
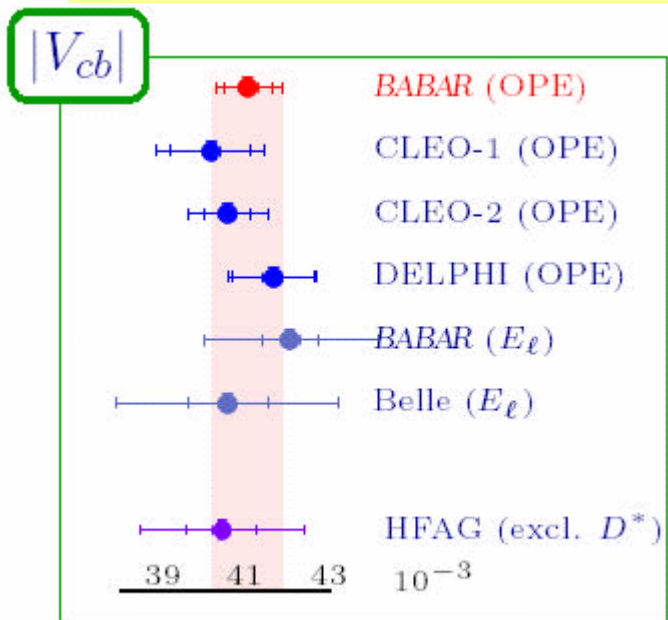
- Overall power of  $E_e$  and  $M_X$  moments is comparable
- Values for  $\mu_G^2$  and  $\rho_{LS}^3$  are consistent with independent measurements based on  $m_{B^*}-m_B$  and HQ sum rules.





# OPE preliminary fit results

$$\begin{aligned}
 |V_{cb}| &= (41.4 \pm 0.4_{\text{exp}} \pm 0.4_{\text{HQE}} \pm 0.6_{\text{th}}) \times 10^{-3} \\
 Br(B \rightarrow X_c e \nu) &= (10.61 \pm 0.16_{\text{exp}} \pm 0.06_{\text{HQE}}) \% \\
 m_b(1 \text{ GeV}) &= (4.61 \pm 0.05_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.02_{\text{th}}) \text{ GeV} \\
 m_b(1 \text{ GeV}) - m_c(1 \text{ GeV}) &= (3.44 \pm 0.03_{\text{exp}} \pm 0.02_{\text{HQE}} \pm 0.01_{\text{th}}) \text{ GeV} \\
 \mu_\pi^2 &= (0.45 \pm 0.04_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.01_{\text{th}}) \text{ GeV}^2
 \end{aligned}$$

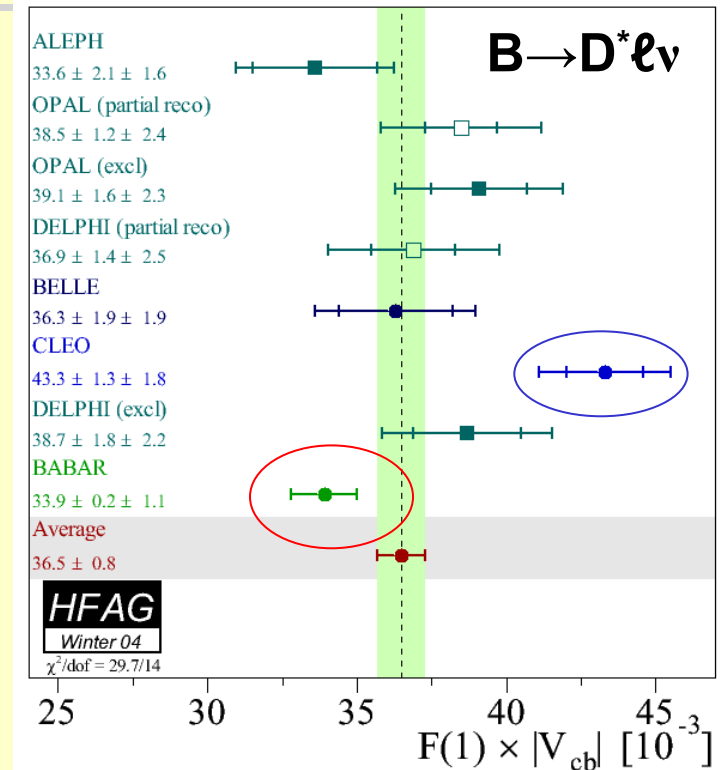


- Different OPE schemes used -

# Comparison of inclusive and exclusive $|V_{cb}|$ determinations

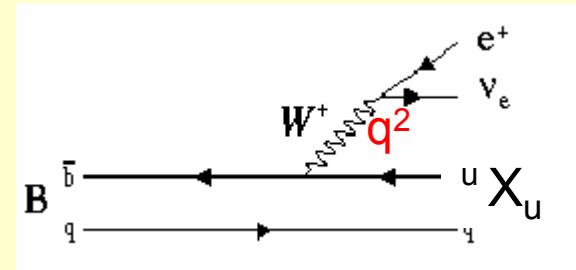
- HFAG average from  $D^*\ell\nu$   
 $|V_{cb}| = (40.1 \pm 0.9_{\text{exp}} \pm 1.8_{\text{theo}}) \times 10^{-3}$
- BaBar (preliminary)  $D^*\ell\nu$   
 $|V_{cb}| = (37.3 \pm 1.5_{\text{exp}} \pm 1.6_{\text{theo}}) \times 10^{-3}$
- BaBar (preliminary) HQE fit to semileptonic moments

$$|V_{cb}| = (41.4 \pm 0.4_{\text{exp}} \pm 0.4_{\text{HQE}} \pm 0.6_{\text{theo}}) \times 10^{-3}$$



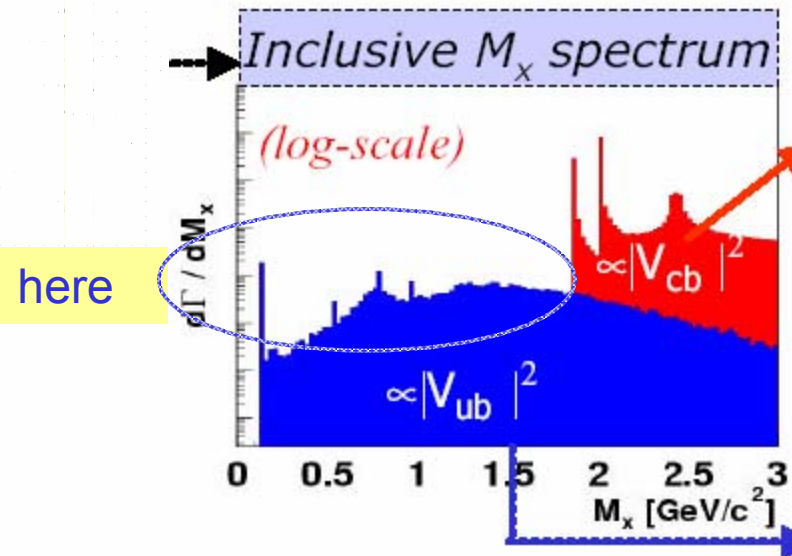
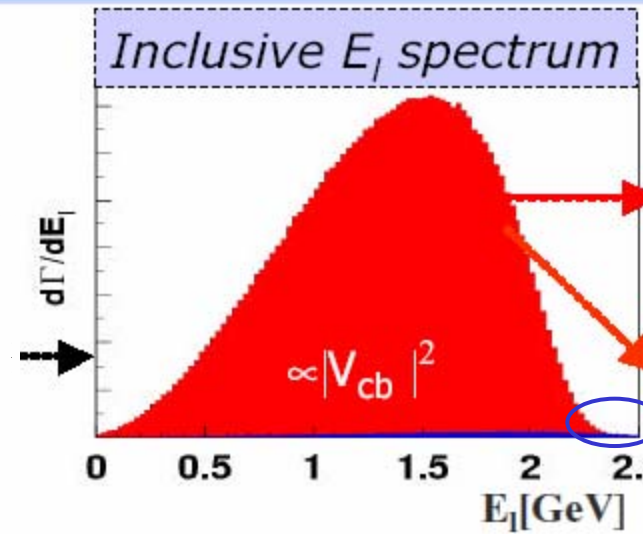
$$F(1) = 0.92 \pm 0.03$$

# $|V_{ub}|$ from inclusive decays

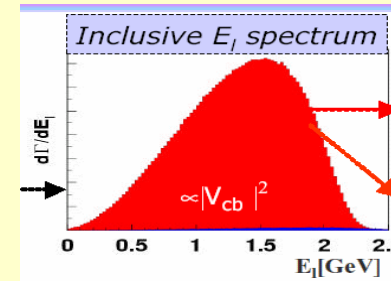


- OPE gives  $|V_{ub}|$  from  $\Gamma(B \rightarrow X_u \ell \nu)$  to  $< 5\%$
- Challenges:
  - separate  $b \rightarrow u$  from  $b \rightarrow c$
  - calculate  $|V_{ub}|$  from partial rate after  $b \rightarrow c$  suppression cuts
- review of published results and methods
- new method
- outlook

# Finding $b \rightarrow u$ decays

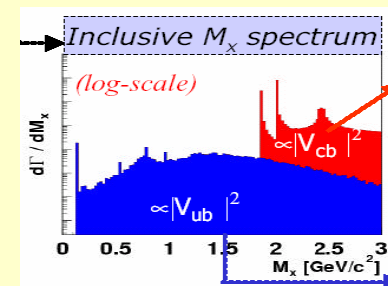


# Lepton endpoint

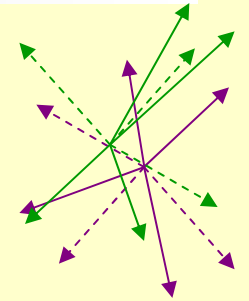


- ☺ Experimentally clean for  $E_e > 2.3$  GeV  $\approx \frac{m_B^2 - m_D^2}{2m_B}$
- ☹ Can't go below  $E_e \sim 2.2$  GeV due to  $b \rightarrow c$  background
- ☠ **OPE breaks down when restricted to endpoint region**  
(need twist expansion in which power corrections are resummed into a light cone distribution function, or “shape function”, which must be measured...)
- ☺ Determine shape function from  $b \rightarrow s\gamma$  or perhaps from semileptonic decays
- Best measurements give  $\sigma_{|V_{ub}|} / |V_{ub}| \sim 0.15$

# Mass of recoiling hadrons



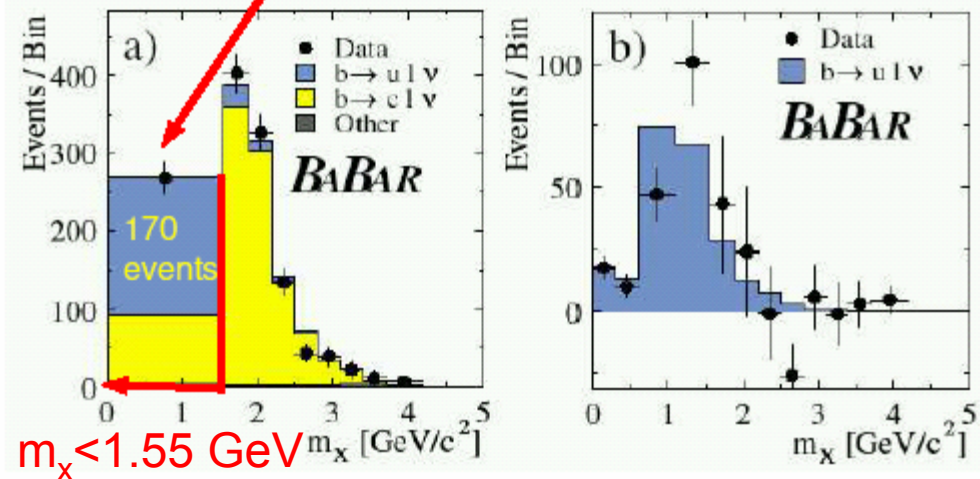
- Larger phase space ( $\sim 70\%$ ) means smaller theoretical uncertainties (but not that **simple...**)
- Experimentally more challenging; need either B tagging (cleanest, very low efficiency) or “simulated annealing” (poor S/B, higher efficiency)
- Combine with  $q^2$  (invariant mass of e- $\nu$  pair) to improve theory error?
- Early measurements show promise



# BaBar $|V_{ub}|$ from tagged analysis

- Reconstruct  $B \rightarrow D^{(*)} n \pi$
- Select lepton  $p_\ell > 1$  GeV; good signal/background
- Perform kinfit to remaining particles to determine  $m_X$
- Measure  $BF(B \rightarrow X_u \ell \nu)$

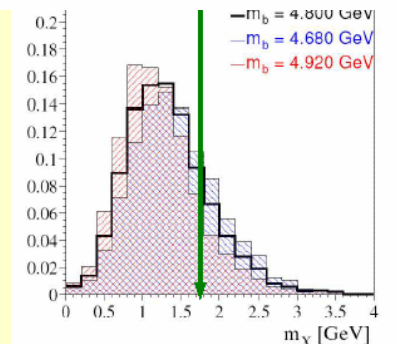
$$\frac{\mathcal{B}(B \rightarrow X_u \ell \nu)}{\mathcal{B}(B \rightarrow X \ell \nu)} = \frac{N_{data} - N_{bg}}{N_{sl}} \times \frac{\epsilon_l^{sl} \epsilon_t^{sl}}{\epsilon_l^u \epsilon_t^u}$$



$$Br(B \rightarrow X_u \ell \nu) = (2.24 \pm 0.27_{stat} \pm 0.26_{syst} \pm 0.39_{theo}) \times 10^{-3}$$

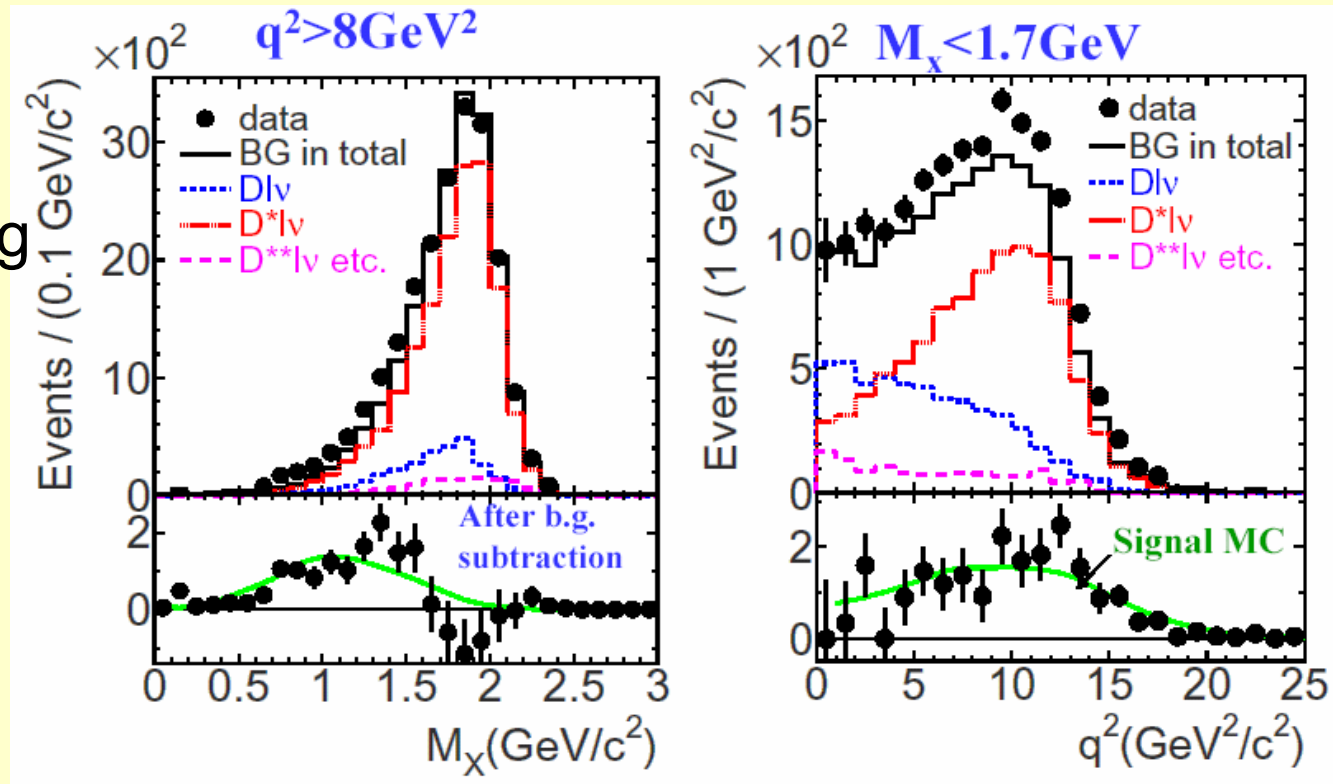
$$|V_{ub}| = (4.62 \pm 0.28_{stat} \pm 0.27_{syst} \pm 0.40_{theo} \pm 0.26_{\Gamma}) \times 10^{-3}$$

- In future consider  $q^2$  to reduce theory error



# Belle simulated annealing

- Try to assign particles to s.l. and other B using kinematics ( $m_B$ ,  $E_B$ ,  $m_{\text{miss}}^2$ )
- Validate on  $D^*\ell\nu$
- S/B poor**



$$|V_{ub}| = (4.66 \pm 0.28(\text{stat}) \pm 0.35(\text{syst}) \pm 0.17(b \rightarrow c) \pm 0.08(b \rightarrow u) \pm 0.58(\text{theo})) \times 10^{-3}$$

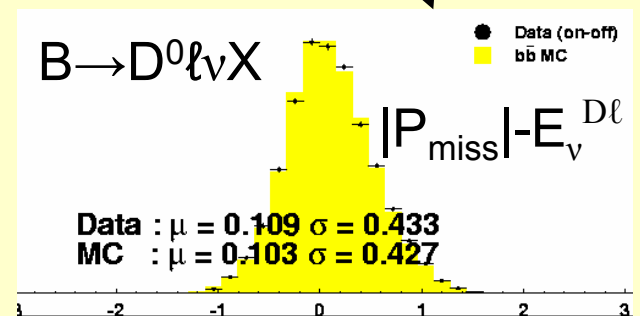
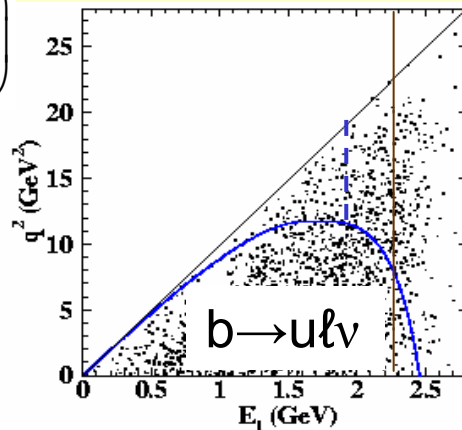
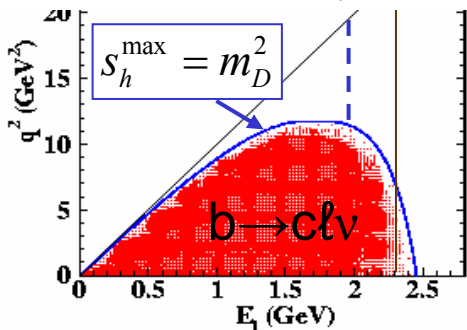
$$= (4.66 \pm 0.76) \times 10^{-3}$$

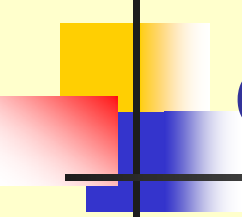


# Lepton-pair invariant mass

- New method – combine  $E_e$  with  $q^2$  to reduce  $E_e$  cut (and theory uncertainty); expect few  $\times 10^3$  events with  $S/B \sim 0.6$ .
- Estimate neutrino momentum based on “missing” momentum. Resolution is modest but usable
- Check / limit theory error by using  $b \rightarrow u \ell \nu$  distributions (e.g.  $\langle E_W + |P_W| \rangle \approx m_b$ ).

$$S_h^{\max} = m_B^2 + q^2 - 2m_B \left( E_\ell + \frac{q^2}{4E_\ell} \right)$$





# $|V_{ub}|$ from inclusive semileptonic decays - status and prospects

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- Active area for theory and experiment
- New analyses with better acceptance and ability to measure decay distributions coming
- Expect significant progress if HQE parameters measured in  $b \rightarrow c$  decays can be used in predictions for  $d\Gamma(b \rightarrow u) / dy$
- My view – 10% measurements of  $|V_{ub}|$  will appear in 2004/05.



# $|V_{ub}|$ from $B \rightarrow \pi \ell \nu$

---

- Extracting  $|V_{ub}|$  from exclusive decays requires Form Factors (FF)
- $\pi \ell \nu$  is the best mode experimentally (low background) and theoretically:
  - Lattice QCD is making good progress on FF
  - measure  $q^2 = m_W^2$  dependence to constrain theory
- status and prospects



# Current status of $B \rightarrow \pi \ell \nu$

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- CLEO

- Based on neutrino reconstruction

- PRD 68, 072003 (2003)

$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.33 \pm 0.18 \pm 0.11 \pm 0.01 \pm 0.07) \times 10^{-4}$$

$$|V_{ub}| = (3.24 \pm 0.22 \pm 0.13 \begin{matrix} +0.55 \\ -0.39 \end{matrix} \pm 0.09) \times 10^{-3}$$

- Belle... (2001 conference paper, never published)

- BaBar...



# Tagged analyses

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- Events where companion B is reconstructed are starting to be used:
  - Much better signal/background, kinematic acceptance
  - Much lower yield (10-100 times smaller than untagged)
  - Better for BF, but not yet for determining FF shapes
- Several tag methods:

Better for  $B^+$   
than for  $B^0$  { Fully reconstructed hadronic B decays  
"Fully" reconstructed semileptonic B decays to  $D^{(*)}\ell\nu$

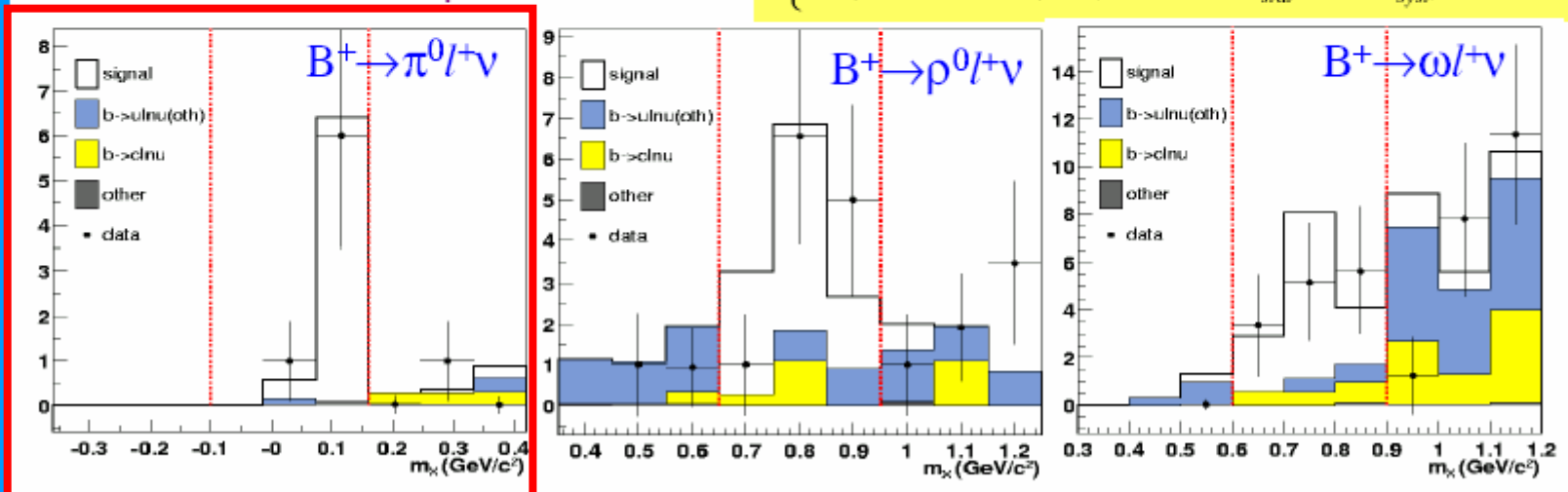
Only for  $B^0$  { Partially reconstructed semileptonic B decays ( $\pi_s\text{-}\ell$   
correlation)

# Exclusive $B^+ \rightarrow \pi^0, \rho^0, \omega l \nu$ decays

## B recoil technique: as in inclusive $V_{ub}$ analysis

- Small statistics
- Very high purity
- Loose cuts
- small model dependence

$$\begin{cases} \mathcal{B}(B^+ \rightarrow \pi^0 l \nu) = (0.78 \pm 0.32_{stat} \pm 0.13_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \rho^0 l \nu) = (0.99 \pm 0.37_{stat} \pm 0.19_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \omega l \nu) = (2.20 \pm 0.92_{stat} \pm 0.57_{syst}) \cdot 10^{-4} \end{cases}$$

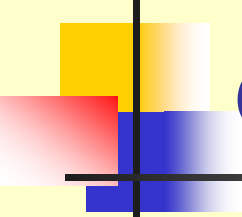


Lake Louise Winter Institute, 2004

Marcello Rotondo

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Preliminary



# $|V_{ub}|$ from exclusive semileptonic decays - status and prospects

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Soon results on  $B \rightarrow \pi \ell \nu$  - tagged and untagged analyses

- Untagged analyses  $\rightarrow$  form factor ( $q^2$ ) shape
- Tagged analyses  $\rightarrow$  BF with small experimental systematics, convincing S/B
- Lattice calculations are becoming more believable
- Expect  $\sigma(|V_{ub}|) \sim 10\%$  in a year or two.





# Summary

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- Significant progress on  $|V_{cb}|$  - accuracy 2% (inclusive), 5% (exclusive)
  - Clear progress due to HQE and precise measurements
- Anticipate improvements in  $|V_{ub}|$  in near future
  - Cleaner and more comprehensive measurements
  - Improvements in theoretical methods
- B factories are systematically probing the weak and strong interactions of quarks

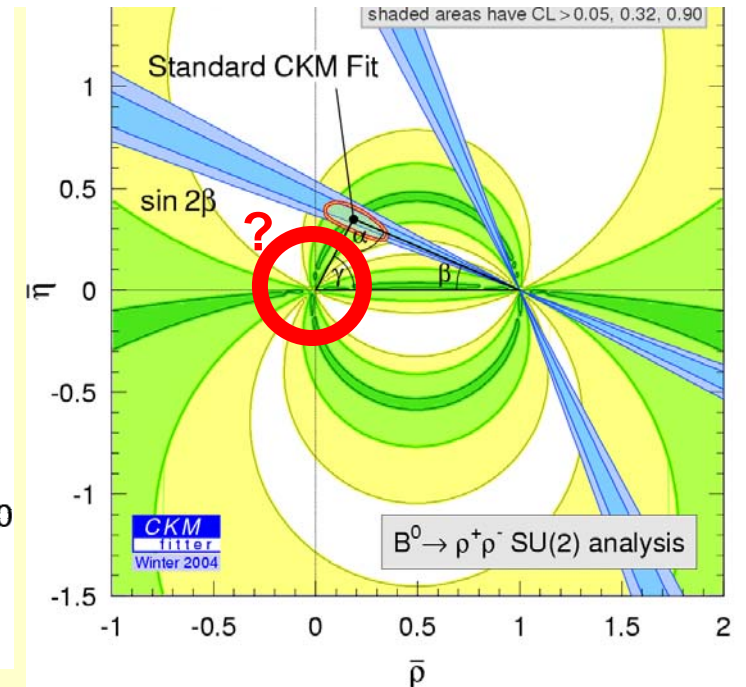
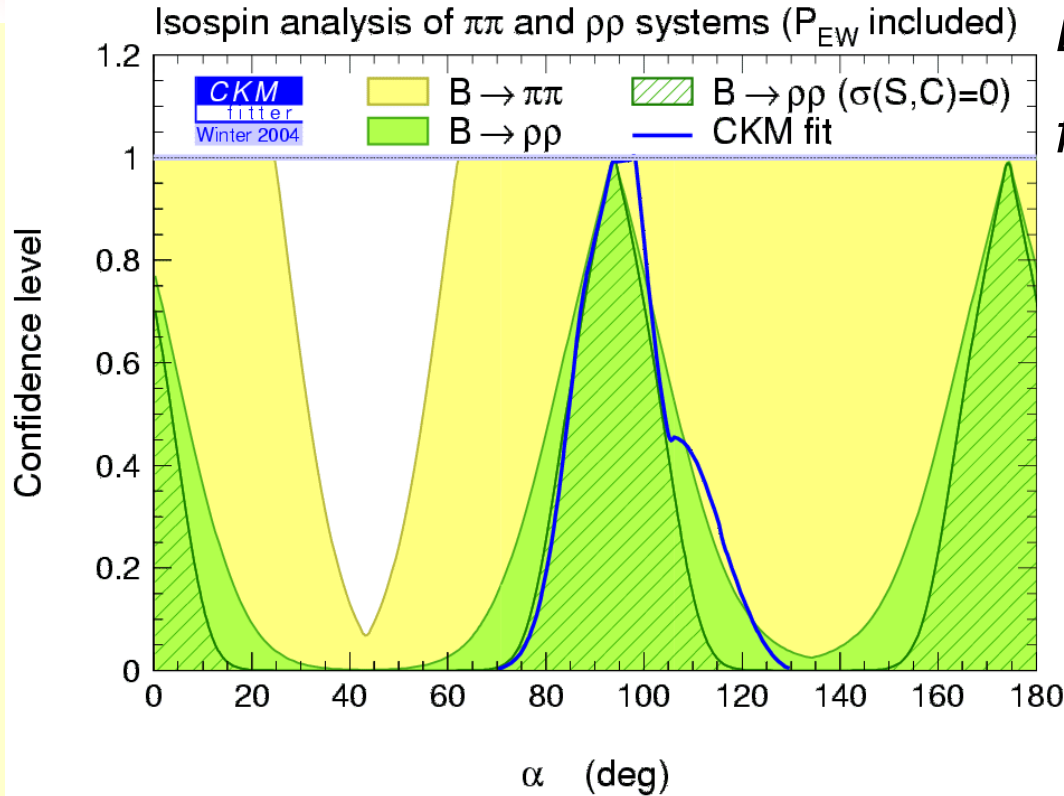
NEW

# sin2α from B → ππ and B → ρρ decays

NEW

$$BR(\rho^+ \rho^-) = (30 \pm 4_{stat} \pm 5_{syst}) 10^{-6}$$

$$f_{long} = 0.99 \pm 0.03(stat)_{-0.03}^{+0.04} (syst)$$



Other ingredients in ρρ isospin analysis:

$$BR(\rho^+ \rho^0) = (26.4 \pm 6.4) 10^{-6} \text{ (BABAR \& Belle)} \quad BR(\rho^0 \rho^0) = (0.62_{-0.60}^{+0.72} \pm 0.12) 10^{-6}$$

$$f_{long}(\rho^+ \rho^0) = 0.962_{-0.065}^{+0.049} \text{ (BABAR \& Belle)}, \quad f_{long}(\rho^0 \rho^0) = 1.0$$

Plots from the CKMfitter group: <http://ckmfitter.in2p3.fr>