

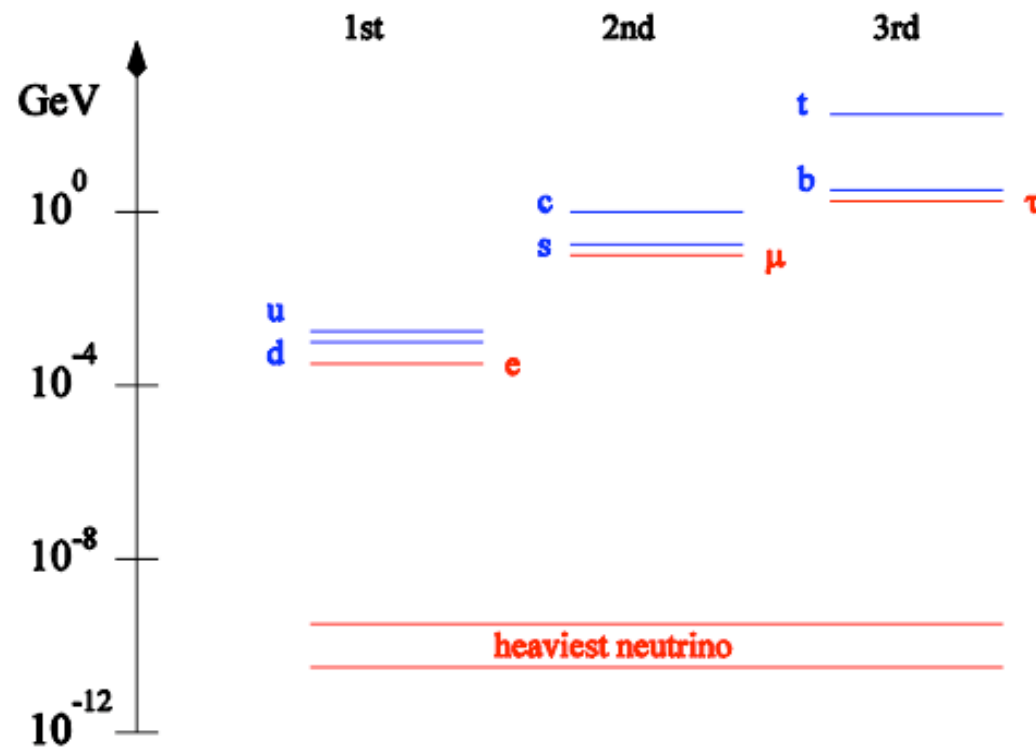
# Some Cutting-Edge Neutrino Topics:

Majorana Neutrinos, the See-Saw Mechanism, Sphalerons, and Leptogenesis

*Did neutrinos cause the matter-antimatter asymmetry of the Universe?*

Neutrino mass is fundamentally different from the other fermions....  
we need new physics to understand it.

Standard model fermion mass spectrum



**A simple Dirac mass for the neutrino requires a Higgs coupling of  $10^{-13}$ .**

## Fermion mass is closely tied to particle/antiparticle nature.

Charged fermions can only have a Dirac mass

$$L_D = m_D \bar{\nu}_R \nu_L + h.c.,$$

Higgs only generates Dirac masses

$$L_{M_L} = \frac{1}{2} m_L \bar{\nu}_L^c \nu_L + h.c.,$$

neutral fermions can also have two types of Majorana masses

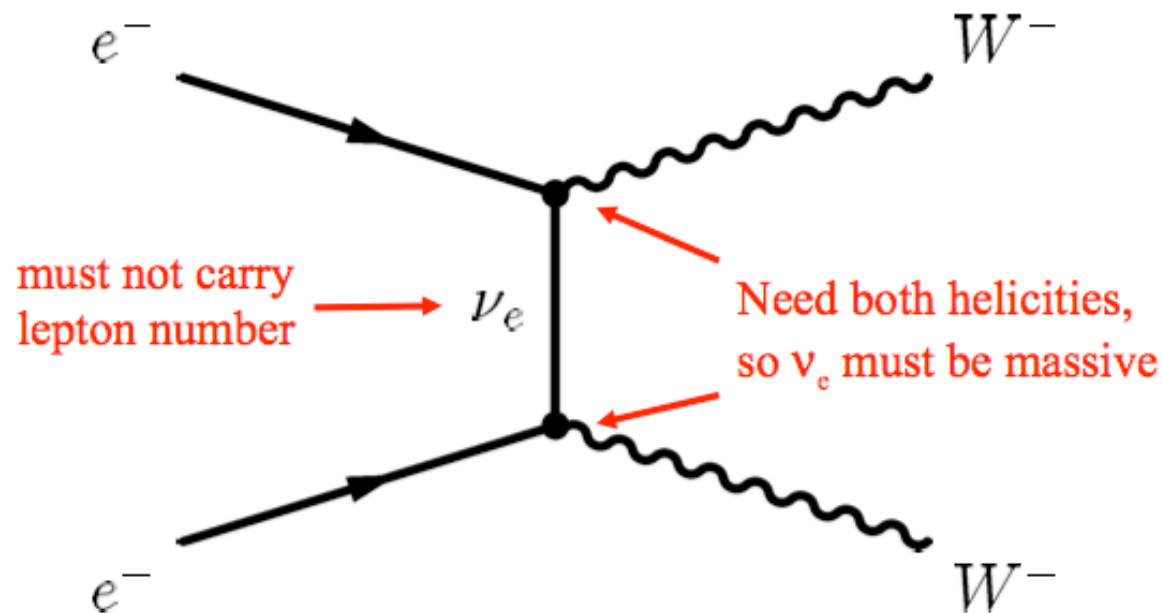
$$L_{M_R} = \frac{1}{2} m_R \bar{\nu}_R^c \nu_R + h.c.$$

**Pure Dirac fermions carry charge: e-, μ-, τ-, ect.**

**Majorana fermions are their own antiparticles... maybe neutrinos?**

**Is lepton number conserved or not?**

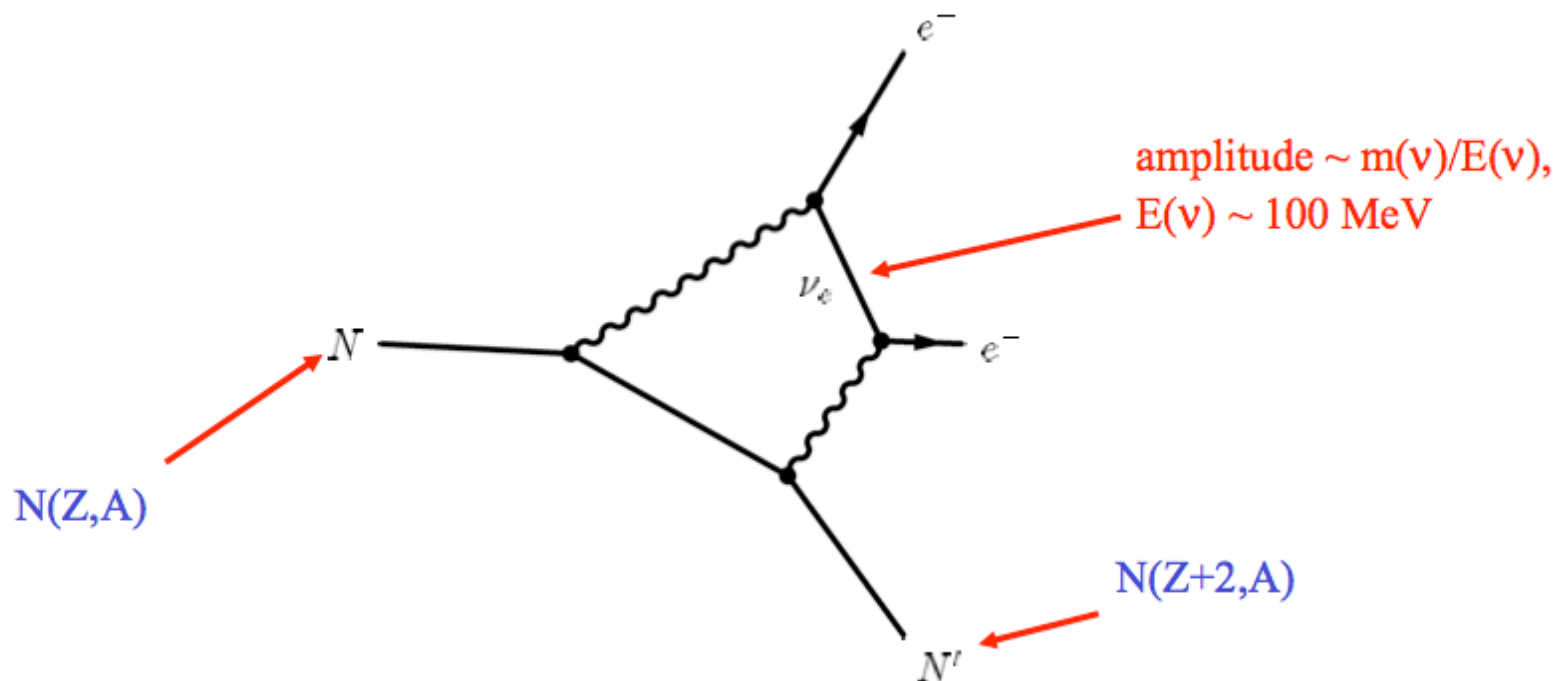
**We need a process which violates total lepton number:**



Observation of this process at an e-e- ILC would indicate the existence of TeV-scale Majorana neutrinos.

To get information on the known light neutrinos, we need a low energy equivalent process.

## $\beta\beta_{0\nu}$ is the same physics at low $Q^2$



“Neutrino mass mechanism” for double beta decay

The process most sensitive to the possible Majorana nature of  $\nu_j$  -  $(\beta\beta)_{0\nu}$ -decay



of even-even nuclei,  $^{48}\text{Ca}$ ,  $^{76}\text{Ge}$ ,  $^{82}\text{Se}$ ,  $^{100}\text{Mo}$ ,  $^{116}\text{Cd}$ ,  $^{130}\text{Te}$ ,  $^{136}\text{Xe}$ ,  $^{150}\text{Nd}$ .

## PMNS Matrix: Standard Parametrization

$$U = V \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\frac{\alpha_{21}}{2}} & 0 \\ 0 & 0 & e^{i\frac{\alpha_{31}}{2}} \end{pmatrix} \quad (4)$$

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13}e^{i\delta} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13}e^{i\delta} \end{pmatrix} \quad (5)$$

- $s_{ij} \equiv \sin \theta_{ij}$ ,  $c_{ij} \equiv \cos \theta_{ij}$ ,  $\theta_{ij} = [0, \frac{\pi}{2}]$ ,
- $\delta$  - Dirac CP-violation phase,  $\delta = [0, 2\pi]$ ,
- $\alpha_{21}$ ,  $\alpha_{31}$  - the two Majorana CP-violation phases.
- $\Delta m_{\odot}^2 \equiv \Delta m_{21}^2 \cong 8.0 \times 10^{-5} \text{ eV}^2 > 0$ ,  $\sin^2 \theta_{12} \cong 0.30$ ,  $\cos 2\theta_{12} \gtrsim 0.28$  ( $2\sigma$ ),
- $|\Delta m_{\text{atm}}^2| \equiv |\Delta m_{31}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$ ,  $\sin^2 2\theta_{23} \cong 1$ ,
- $\theta_{13}$  - the CHOOZ angle:  $\sin^2 \theta_{13} < 0.027$  (0.041)  $2\sigma$  ( $3\sigma$ ).

## The $\beta\beta 0\nu$ half-life depends directly on the absolute neutrino masses:

$$\left(T_{1/2}^{0\nu\beta\beta}\right)^{-1} = G^{0\nu\beta\beta} \cdot |NME|^2 \cdot \left|\langle m_\nu \rangle\right|^2,$$

phase space  $\nearrow$  Nuclear Matrix Element  $\uparrow$  effective mass  $\nwarrow$

$$\langle m_\nu \rangle = \sum_i U_{ei}^2 m_i e^{i\alpha_i}$$

mixing matrix (with phases)  $\nearrow$  mass eigenvalues  $\nwarrow$  Majorana phases

### Two caveats to $\beta\beta 0\nu$ as a mass measurement:

- 1) we must have a reliable calculation of the nuclear matrix element
- 2) the neutrino mass mechanism must dominate the decay

One of the most attractive ideas for explaining small neutrino masses is the one based on the

## Seesaw Mechanism

The tiny masses of light neutrinos are naturally understood if we introduce **heavy Majorana neutrinos** to the SM.

$$\mathcal{L} = -\frac{1}{2}M N^T N + (-h N^T \ell \varphi + h.c.)$$

By integrating out the heavy right-handed neutrinos, one obtains the **small Majorana masses for light neutrinos**

$$m_\nu \sim \frac{h^2 \langle \varphi \rangle^2}{M}$$

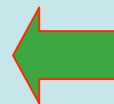
Minkowski, PLB 1977  
Gell-Mann, Ramond & Slansky, 1979  
Yanagida, 1979  
Glashow, 1980  
Mohapatra & Senjanovic, PRL 1980



Thanks to MIKE LESTER (and FRJ)

## Leptogenesis

Fukugita & Yanagida, PLB 1986



When the **heavy Majorana neutrinos** decay into leptons and Higgs scalars they **violate lepton number**, and the interference between the tree-level and the one-loop amplitudes yields a **non-zero CP-asymmetry**. This leads to a **lepton asymmetry** which is then partially converted into **baryon asymmetry** by **sphaleron** processes.



- simple seesaw formula

$$m_\nu = -m_D \frac{1}{M} m_D^T$$

$m_D$ ,  $m_\nu$  and  $M$  are complex matrices  $\Rightarrow$  natural source of  $CP$  violation

- heavy RH neutrino mass matrix  $M \Rightarrow$  three new heavy RH neutrinos  $N_1, N_2$  and  $N_3$  with masses  $M_{ew} \ll M_1 \leq M_2 \leq M_3$
- Dirac neutrino mass matrix  $m_D \sim M_{ew}$
- light neutrino mass matrix  $m_\nu$  ( $m_\nu = m_D^2/M \sim 10^{-2}$  eV for  $M \sim 10^{15}$  GeV)
- lightest RH neutrinos play the role of the decaying particles  $X \equiv N_1$  (Fukugita, Yanagida '86)

Adding to the SM (3) RH neutrinos with Yukawa couplings  $h$  and a Majorana mass  $M$ ,

$$\mathcal{L}_Y = -\bar{l}_L \phi h \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + h.c.,$$

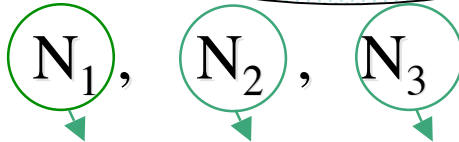
a usual Dirac mass  $m_D = v * h$  is also generated after SSB. For  $M \gg m_D$ :

3 light LH neutrinos:

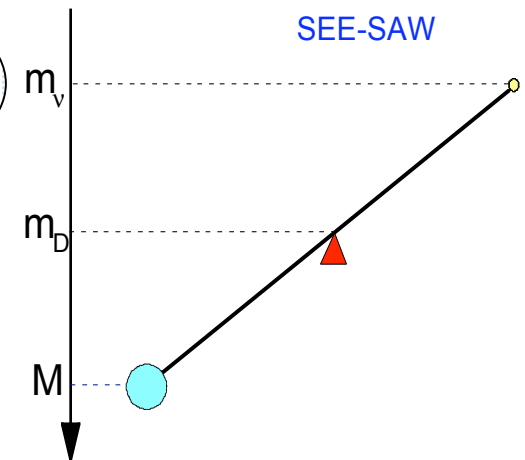
$$m_\nu = -m_D \frac{1}{M} m_D^T$$

Typical example:  
 $m_D \sim 100$  GeV,  $M \sim 10^{14}$  GeV  
 $\Rightarrow m_\nu \sim m_{atm} \sim 0.1$  eV

3 heavy RH neutrinos:



$$100 \text{ GeV} \sim M_{ew} \simeq m_D \ll M_1 \leq M_2 \leq M_3$$



# Leptogenesis

Fukugita & Yanagida, PLB 1986

Leptogenesis via heavy Majorana neutrino decay

Asymmetry in the lepton number

Seesaw Mechanism

Neutrino masses

Can be converted into baryon number through

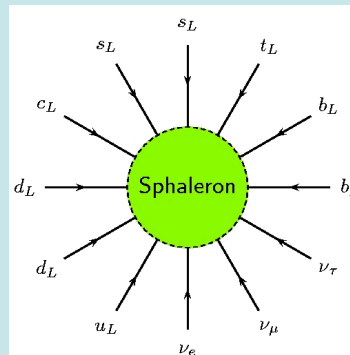
Sphalerons

Non-perturbative effects

Violate B+L

Conserve B-L

Efficient above the EW scale



$$Y_B \equiv \frac{n_B}{s} = \xi Y_L$$

$$\xi = 28/79 \quad (\text{SM})$$

$$\xi = 8/23 \quad (\text{MSSM})$$

Kuzmin et al 1985  
Khlebnikov et al 1985

In the SM Baryon Number conserved at classical level but violated at quantum level :  $\Delta B = \Delta L$

**Anomalies arise in the process of regularization of divergences.**

**Impossible to do it preserving gauge and B and L symmetries.**

$$\partial^\mu j_\mu^{B,L} = \frac{N_f g^2}{32 \pi^2} \text{Tr} \left( \epsilon^{\mu\nu\alpha\beta} F_{\mu\nu} F_{\alpha\beta} \right)$$

**Instantons are minimal action configuration with non-vanishing values of the integral of the right –hand side of the above Eq.**

**Instanton configurations may be regarded as semiclassical amplitudes for tunnelling effect between vacuum states with different baryon number**

$$S_{inst} = \frac{4\pi}{\alpha_W} \quad \Gamma_{\Delta B \neq 0} \propto \exp(-S_{inst})$$

**Weak interactions: Transition amplitude exponentially small.  
No observable baryon number violating effects at T = 0**

# Non-equivalent Vacua and Static Energy in Field Configuration Space

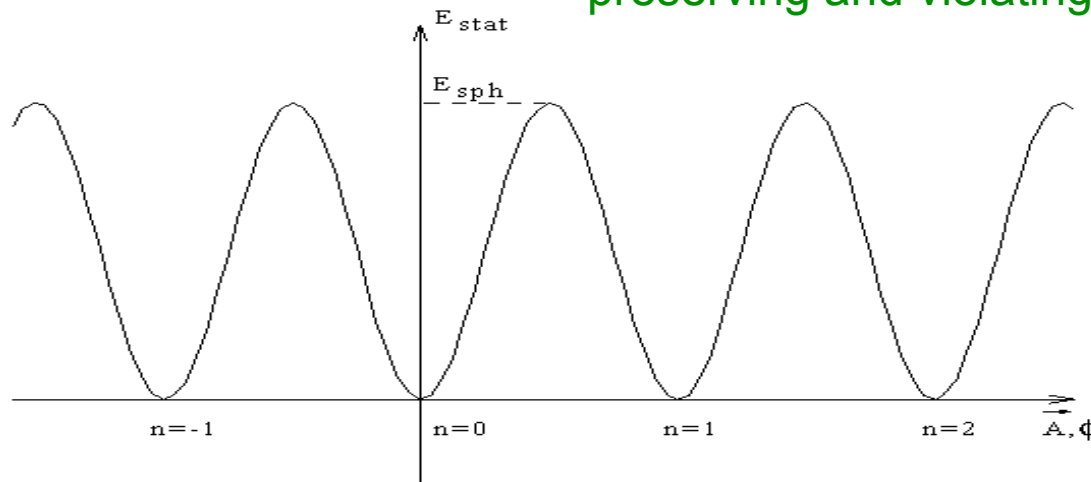
*The sphaleron is a static configuration with non-vanishing values of the Higgs and gauge boson fields.*

*Its energy may be identified with the height of the barrier separating vacua with different baryon number*

$$E_{sph} = \frac{8\pi v}{g_W}$$

The quantity  $v$  is the Higgs vacuum expectation value,  $\langle H \rangle = v$ .

This quantity provides an order parameter which distinguishes the electroweak symmetry preserving and violating phases.



# Baryon Number Violation at Finite Temperature

*Anomalous processes violate both B and L number, but preserve B-L.  
(Important for the explanation of the Baryon Asymmetry of the Universe)*

- At  $T = 0$ , Baryon number violating processes exponentially suppressed*

$$\Gamma_{\Delta B \neq 0} \cong \exp(-2\pi / \alpha_W)$$

- At very high temperatures they are highly unsuppressed,*

$$\Gamma_{\Delta B \neq 0} \propto T$$

- At Finite Temperature, instead, only Boltzman suppressed*

$$\Gamma_{\Delta B \neq 0} \cong \beta_0 T \exp(-E_{\text{sph}}(T) / T)$$

with  $E_{\text{sph}} \cong 8\pi v(T) / g$  and  $v(T)$  the Higgs v.e.v.

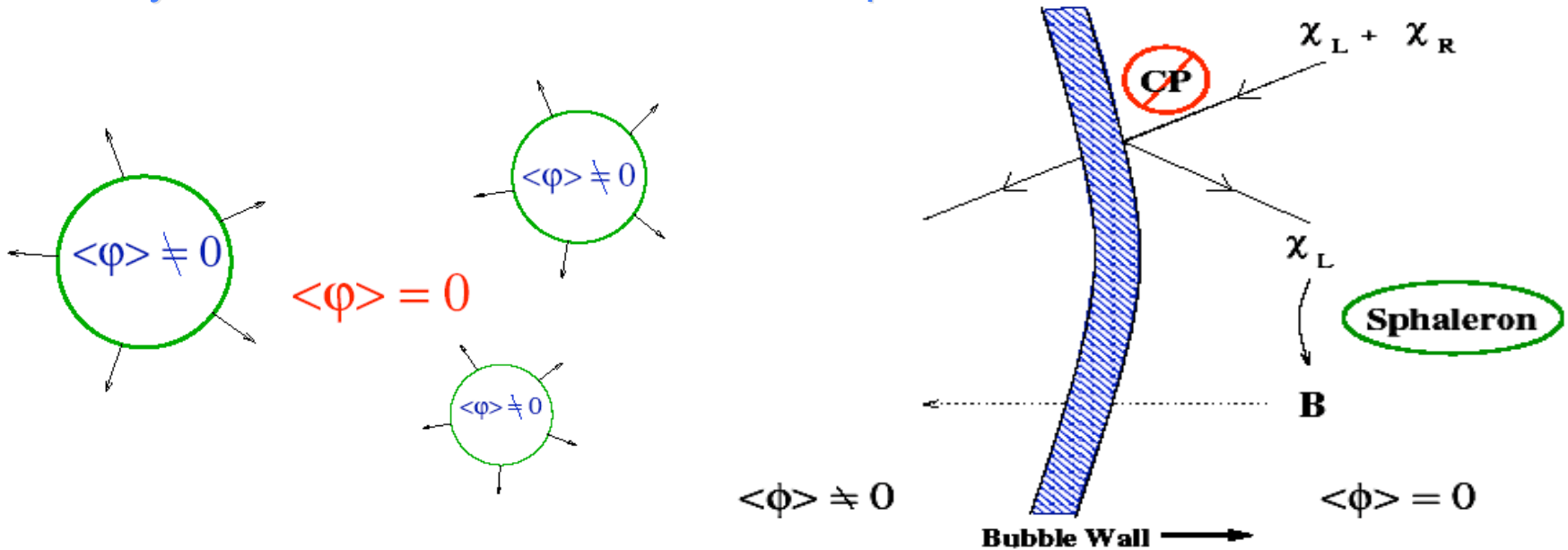
# Baryogenesis at the Electroweak Phase transition

Kuzmin, Rubakov and Shaposhnikov, '85-'87  
Cohen, Kaplan and Nelson '93

- Start with  $B=L=0$  at  $T > T_c$
- CP violating phases create chiral baryon-antibaryon asymmetry in the symmetric phase.  $n_L + n_R = n_{\bar{L}} + n_{\bar{R}} \Rightarrow B = \bar{B}$  but  $\Delta_{n_L} = \Delta_{n_{\bar{R}}} \neq 0$
- Sphaleron processes create net baryon asymmetry.

Sphalerons violate  $B+L$  but conserve  $B-L$ ; change net  $B$  into  $-L$  only for left handed

- Net Baryon Number diffuse in the broken phase



# Baryon Asymmetry Preservation

if  $n_B = 0$  at  $T > T_c$ , independently of the source of baryon asymmetry

$$\frac{n_B}{s} = \frac{n_B(T_c)}{s} \exp\left(-\frac{10^{16}}{T_c(\text{GeV})} \exp\left(-\frac{E_{\text{sph}}(T_c)}{T_c}\right)\right)$$

Baryon number erased unless the baryon number violating processes are out of equilibrium in the broken phase.  $\Gamma_{\Delta B \neq 0} < H \Rightarrow \mathcal{B}$  processes frozen

$$\Gamma_{\Delta B \neq 0} \cong \beta_0 T \exp(-E_{\text{sph}}(T)/T) \Rightarrow \frac{M_{\text{Pl}}}{T} \exp(-E_{\text{sph}}(T)/T) \ll 1$$
$$H \cong g_*^{1/2} T^2 / M_{\text{Pl}}$$

To preserve the generated baryon asymmetry:  
**strong first order phase transition:**

$$v(T_c) / T_c > 1$$

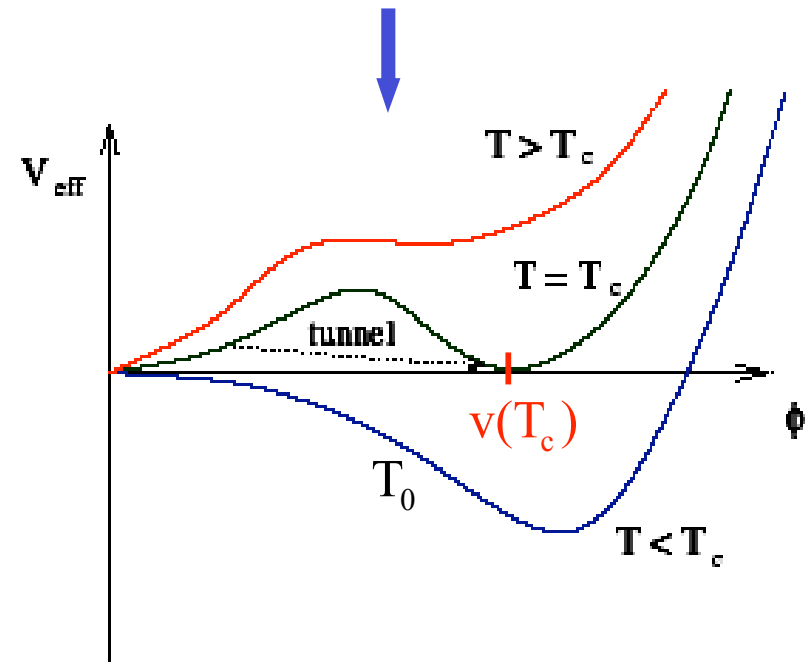
## Electroweak Phase Transition

- The critical temperature is the one for which the symmetry breaking vacuum has the same depth as the symmetry conserving one

$$V(v = 0, T_c) = V(v(T_c), T_c)$$

- If the phase transition is second order:  $T_c = T_0$

### Higgs Potential Evolution in the case of a first order Phase Transition



SM Electroweak Baryogenesis fulfills the Sakharov conditions

- **SM Baryon number violation:** Anomalous Processes
- **CP violation:** Quark CKM mixing
- **Non-equilibrium:** Possible at the electroweak phase transition.



# Leptogenesis

- Out of equilibrium decays of

$$N_{heavy \rightarrow l + \text{Higgs}} \neq N_{heavy \rightarrow \bar{l} + \text{Higgs}}$$

created a *lepton* asymmetry

- Electroweak tunneling (actually thermal fluctuation) then converts some of the lepton asymmetry into a baryon asymmetry!
- Difficulties in supersymmetric version: gravitino problem suggests reheating temperature too low (unless  $N_{heavy}$  produced nonthermally)

# Leptogenesis II

$$N_L^c \rightarrow \bar{\Phi} + \ell \quad \text{Interference between tree-level} \\ \text{\& absorptive part of 1-loop vertex} \\ N_L^c \rightarrow \Phi + \bar{\ell} \quad \text{gives asymmetry.}$$

- Usually requires right-handed mass  $\sim 10^{10}$  GeV
- Decays are out of equilibrium because of expansion of universe
- Attractive because such massive RH neutrinos needed to get now-observed neutrino masses.
- Less attractive because hard to test in colliders.
- Some low-scale versions exist, but not compelling.

# This is More Popular than Ever

## *Neutrinos*, by John Updike

Neutrinos: they are very small  
They have no charge; ~~they have no mass;~~  
~~They do not interact at all.~~  
The Earth is just a silly ball  
To them, through which they simply pass  
Like dustmaids down a drafty hall  
Or photons through a sheet of glass.  
They snub the most exquisite gas,  
Ignore the most substantial wall,  
Cold shoulder steel and sounding brass,  
Insult the stallion in his stall,  
And, scorning barriers of class,  
Infiltrate you and me. Like tall  
And painless guillotines they fall  
Down through our heads into the grass.  
At night, they enter at Nepal  
And pierce the lover and his lass  
From underneath the bed. You call  
It wonderful; I call it crass.

- We now know neutrinos do have mass!
- In fact, as much of the mass of the Universe comes from neutrinos as from stars and galaxies
- **Most popular way to explain this (the seesaw mechanism) requires a heavy right-handed neutrino of about the right scale for leptogenesis**