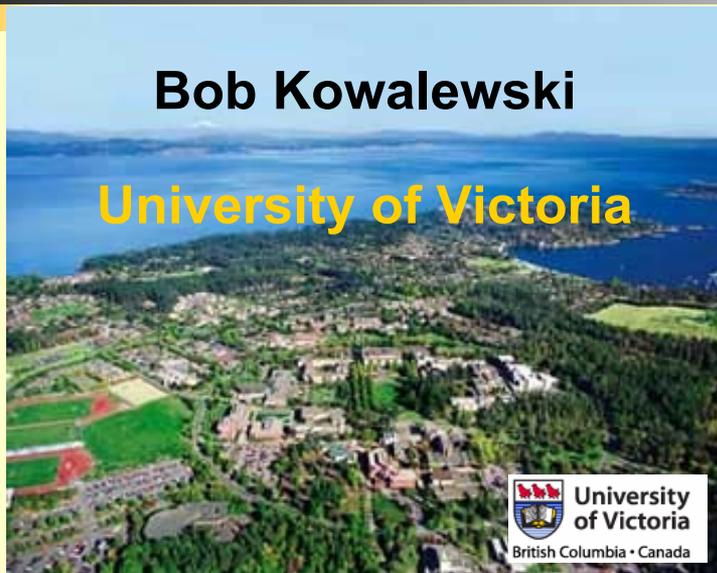


Results on Semileptonic B Decays from BaBar

Bob Kowalewski

University of Victoria



**Stanford
Linear
Accelerator
Center**

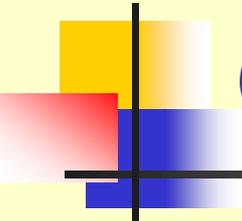
Currently at

Università degli Studi di Roma



**and the Laboratori
Nazionali di Frascati**



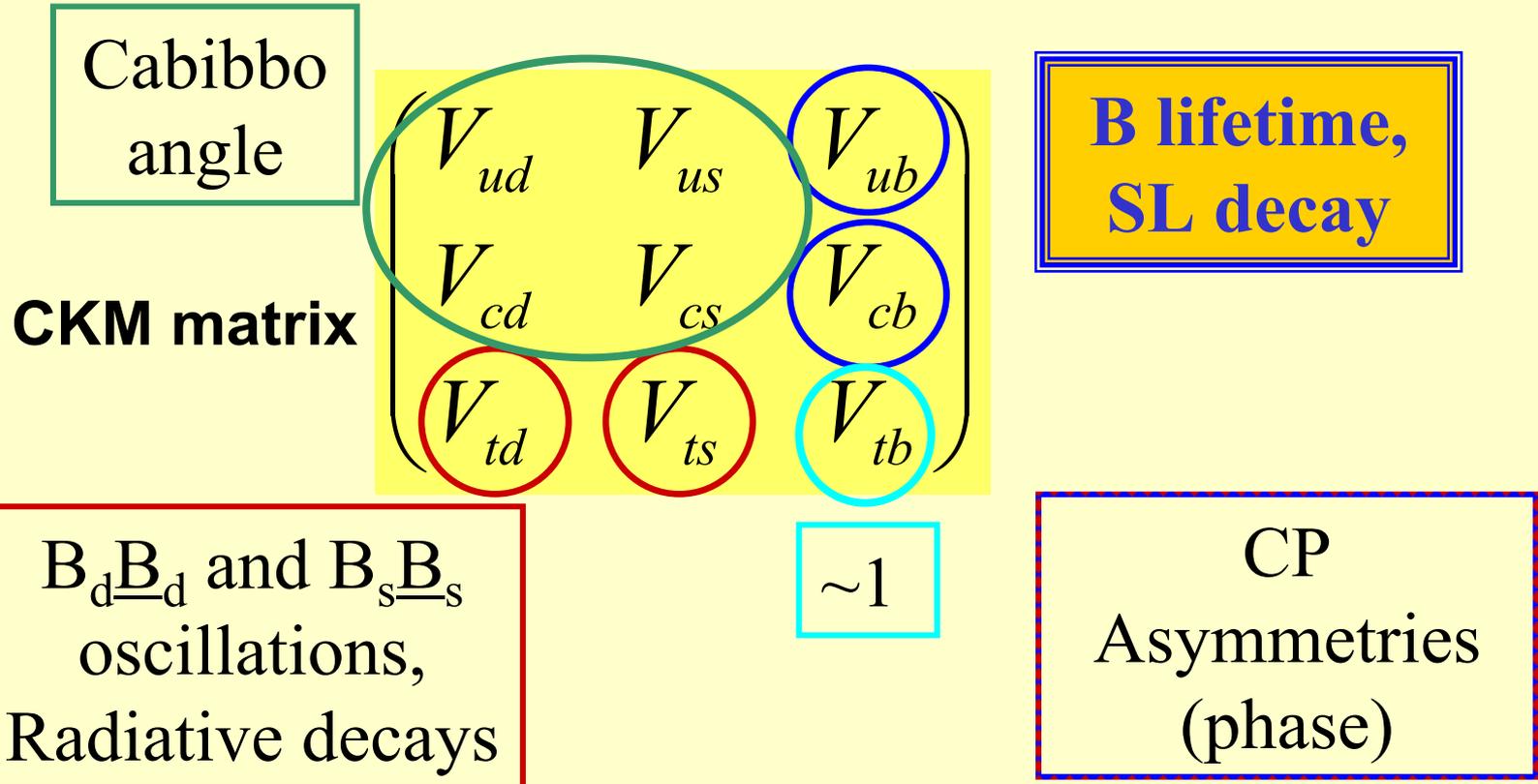


Outline

- Context – B decays and the CKM sector
 - Theoretical framework for inclusive B decays
 - Inclusive $b \rightarrow c \ell \nu$ decays and $|V_{cb}|$
 - Inclusive $b \rightarrow u \ell \nu$ decays and $|V_{ub}|$
 - $B \rightarrow D^* \ell \nu$: FF and $|V_{cb}|$
 - $B \rightarrow \pi \ell \nu$ and $|V_{ub}|$
- } If I have time....

B decays – a window on the quark sector

- The only 3rd generation quark we can study in detail
- Access 3 of the 4 CKM parameters



CKM picture → Unitarity Triangle

λ , A , $\bar{\rho}$ and $\bar{\eta}$

At the 1% level : $|V_{us}|$

$$\lambda = |V_{us}| = \sin \theta_C$$

$$\lambda = 0.2196 \pm 0.0023$$

At the 2% level : $|V_{us}|$

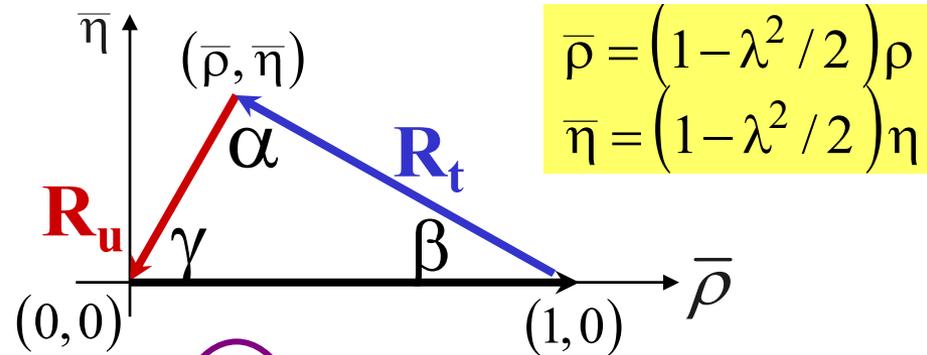
$$A = |V_{cb}| / \lambda^2$$

$$A = 0.84 \pm 0.02$$

$|V_{ub}|$ and $|V_{cb}|$

→ $\bar{\rho} - \bar{\eta}$ plane

Unitarity: $1 + R_t + R_u = 0$



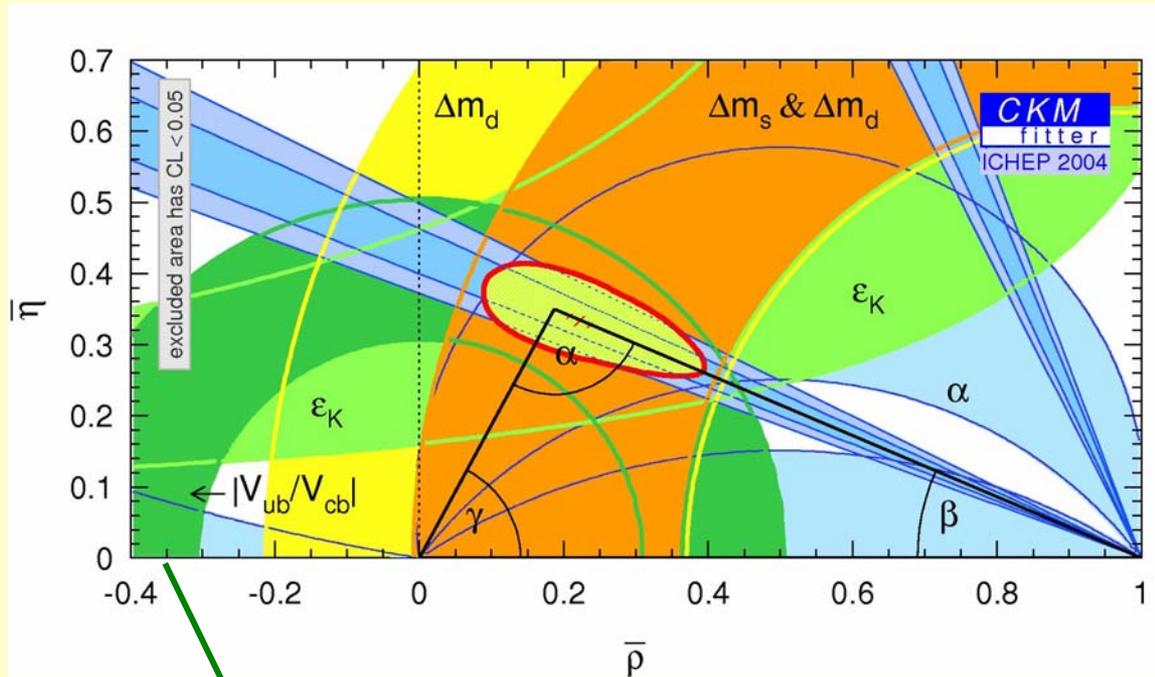
$$R_u = \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \approx -\sqrt{\bar{\rho}^2 + \bar{\eta}^2} e^{i\gamma}$$

$$R_t = \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \approx -\sqrt{(1 - \bar{\rho})^2 + \bar{\eta}^2} e^{-i\beta}$$

$$\gamma = \arg V_{ub}^*, \quad \alpha = \pi - \gamma - \beta$$

Current status in ρ - η space

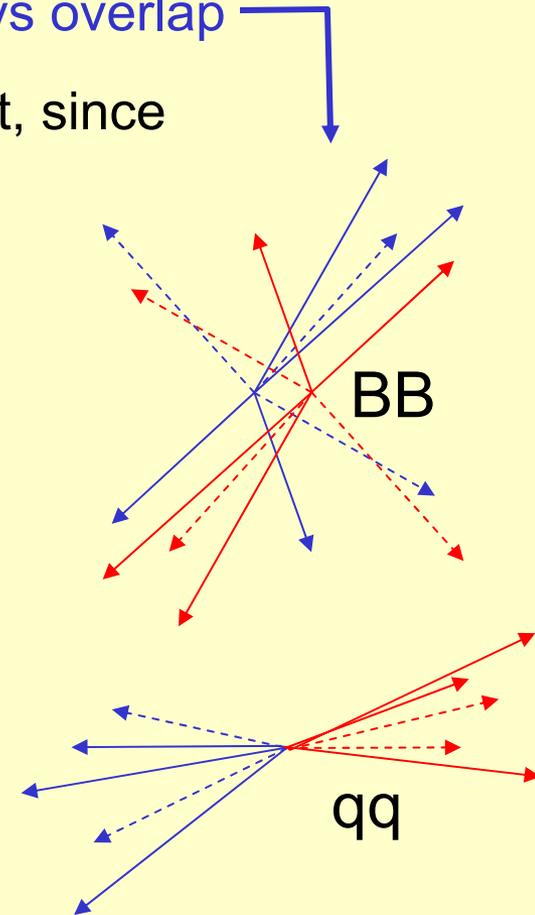
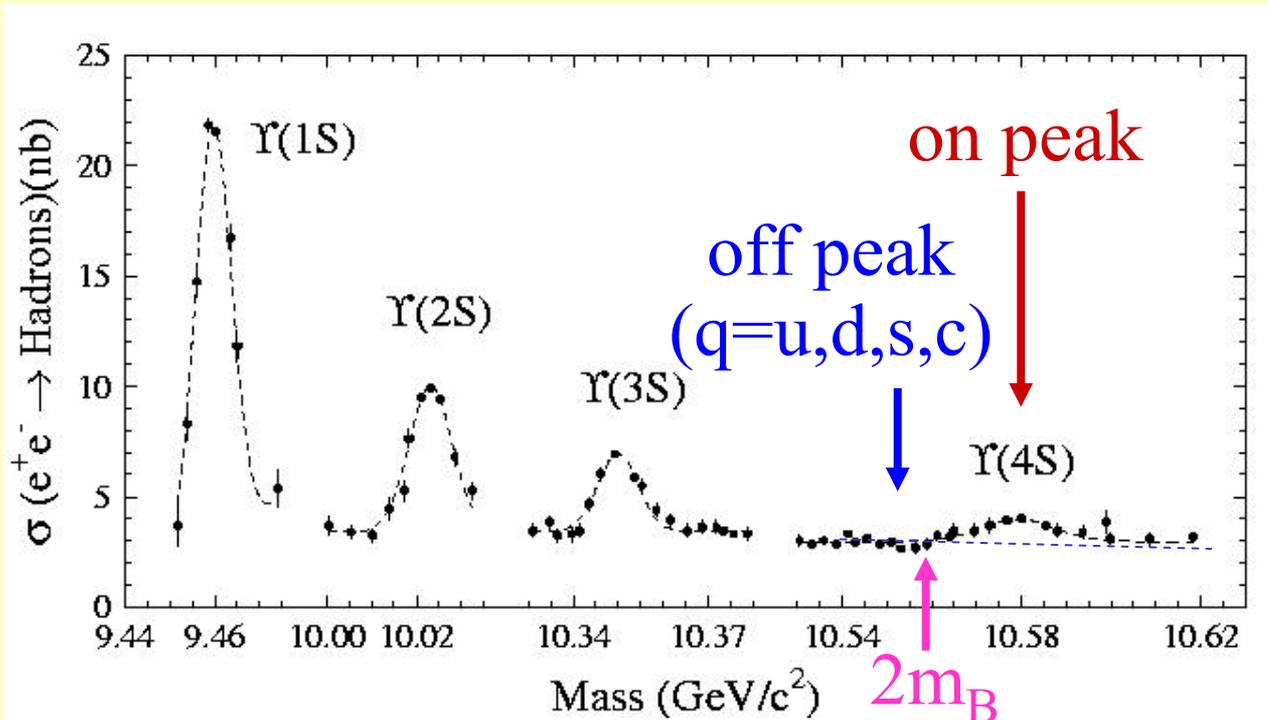
- Measurements are consistent with SM
- CP asymmetries from B factories dominate the determination of η
- Improved precision needed on $|V_{ub}|$ and other angles (α, γ)
- Also need information on B_s oscillations!



$|V_{ub}|/|V_{cb}|$ band ($\pm 2\sigma$)
corresponds to $\sigma=12\%$

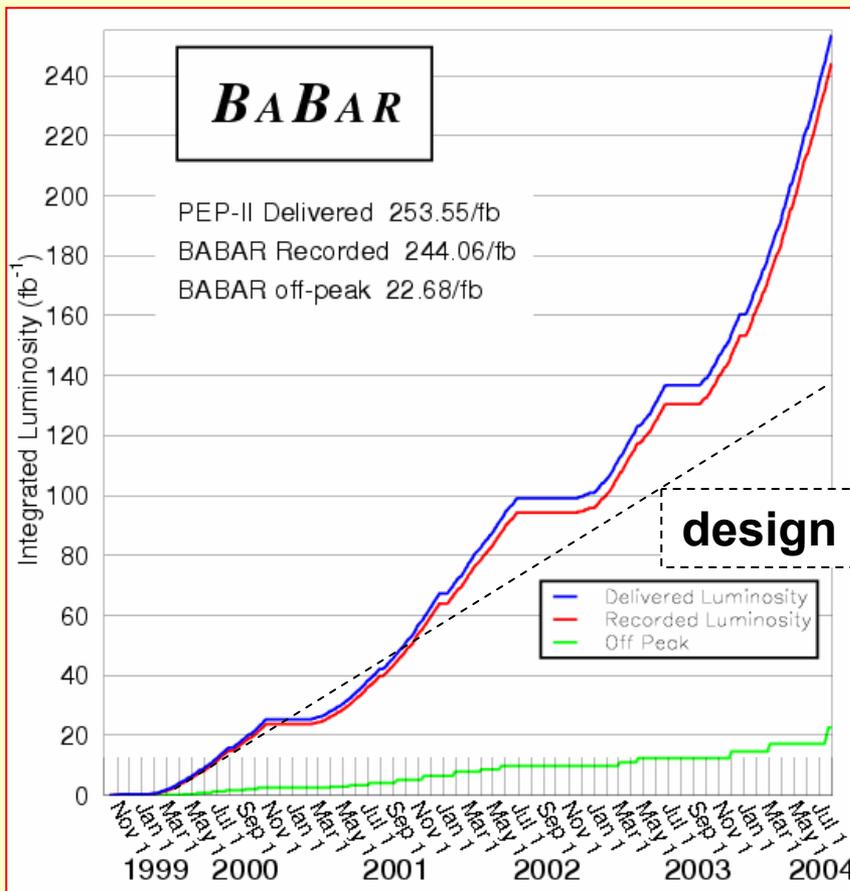
Y(4S) experiments

- $e^+e^- \rightarrow Y(4S) \rightarrow B^+B^-$ or $B^0\bar{B}^0$; roughly 50% each
- B nearly at rest ($\beta\gamma \sim 0.06$) in 4S frame; decays overlap
- B energy = $\frac{1}{2}$ c.m. energy; valuable constraint, since $\sigma_E \sim 5$ MeV for e^+e^- beams



Our research tools

- PEP-2 performance has been marvelous



L_{max} ($10^{33}/\text{cm}^2/\text{s}$)

BaBar

9.2

best day (pb^{-1})

681

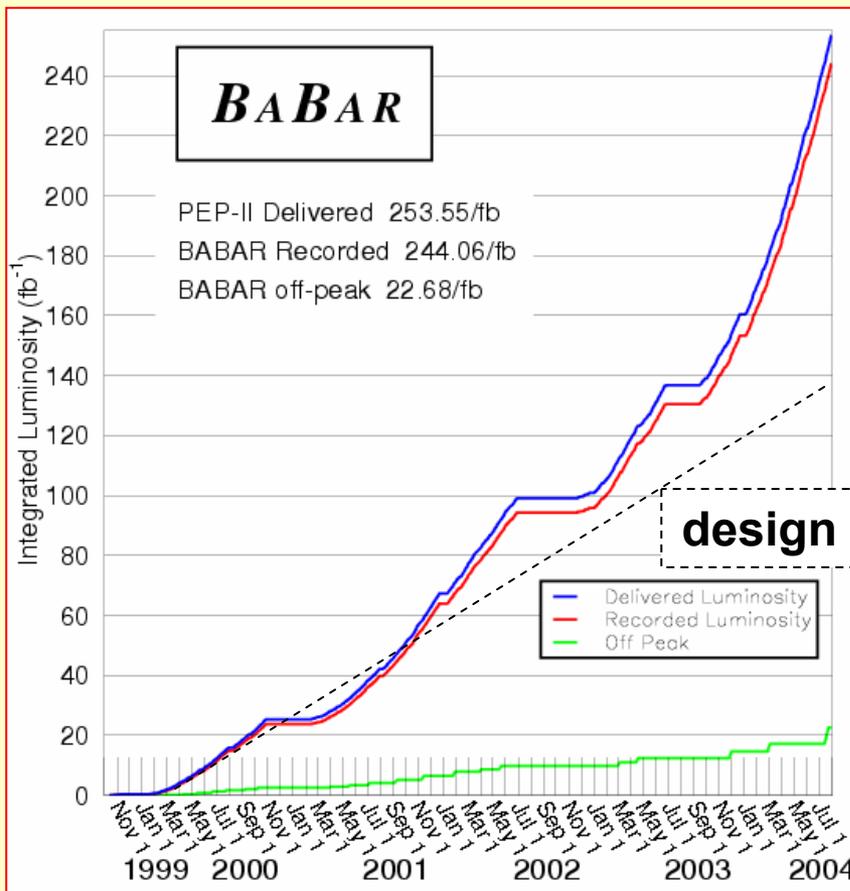
total (fb^{-1})

244

- Design was $30 \text{ fb}^{-1}/\text{year}$...

Our research tools

- PEP-2 performance has been marvelous; almost as good as KEK-B...



L_{max} ($10^{33}/\text{cm}^2/\text{s}$)

BaBar

9.2

Belle

13.9

best day (pb^{-1})

681

944

total (fb^{-1})

244

338

- Design was $30 \text{ fb}^{-1}/\text{year}$...

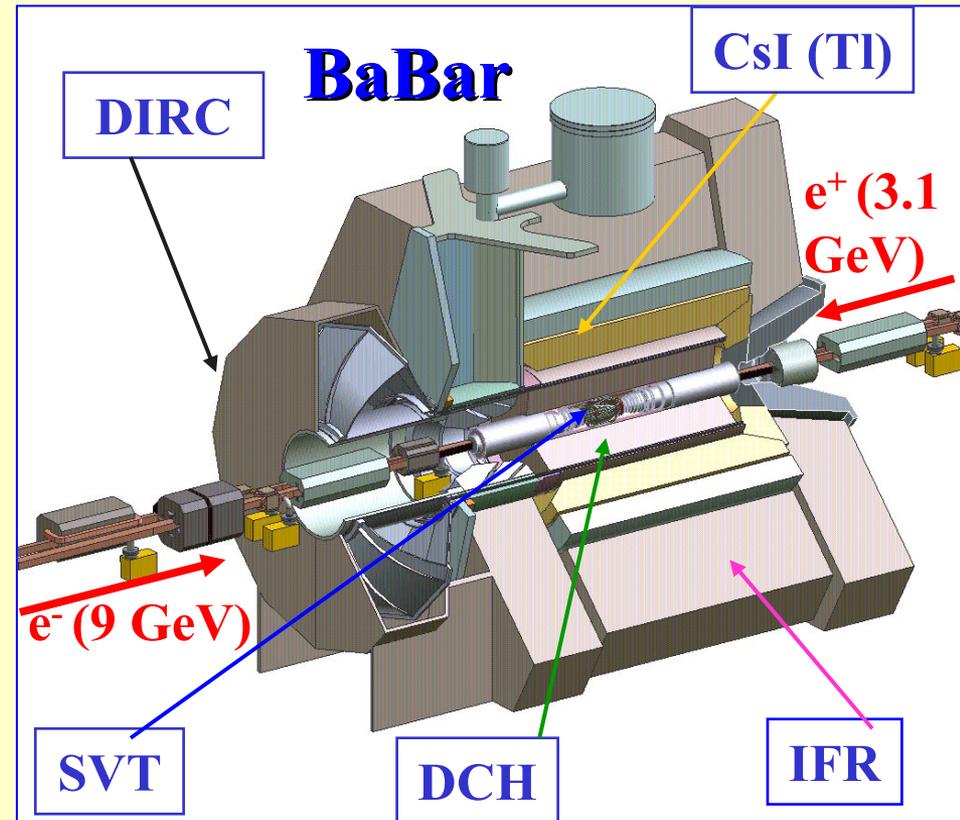
PEP-II luminaries



Jonathan Dorfan
Pier Oddone

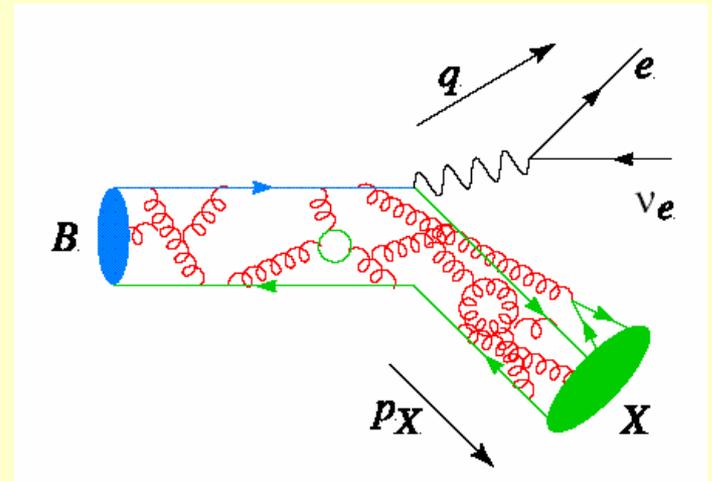
Our research tools

- BaBar has recorded >96% of delivered luminosity
 - Trigger efficiency for $B\bar{B}$ events $\sim 100\%$
-
- 5-layer SVT tracker
 - 40-layer Drift Chamber $\rightarrow dE/dx$
 - Novel RICH based on total internal reflection (DIRC)
 - CsI(Tl) crystal calorimeter (e^\pm, γ)
 - RPC and LST chambers in flux return for muon ID
 - Angular coverage $\sim 92\%$ of 4π in cm frame (challenge for ν reco)
 - Boost: $\beta_{4S} = 0.56$ in lab

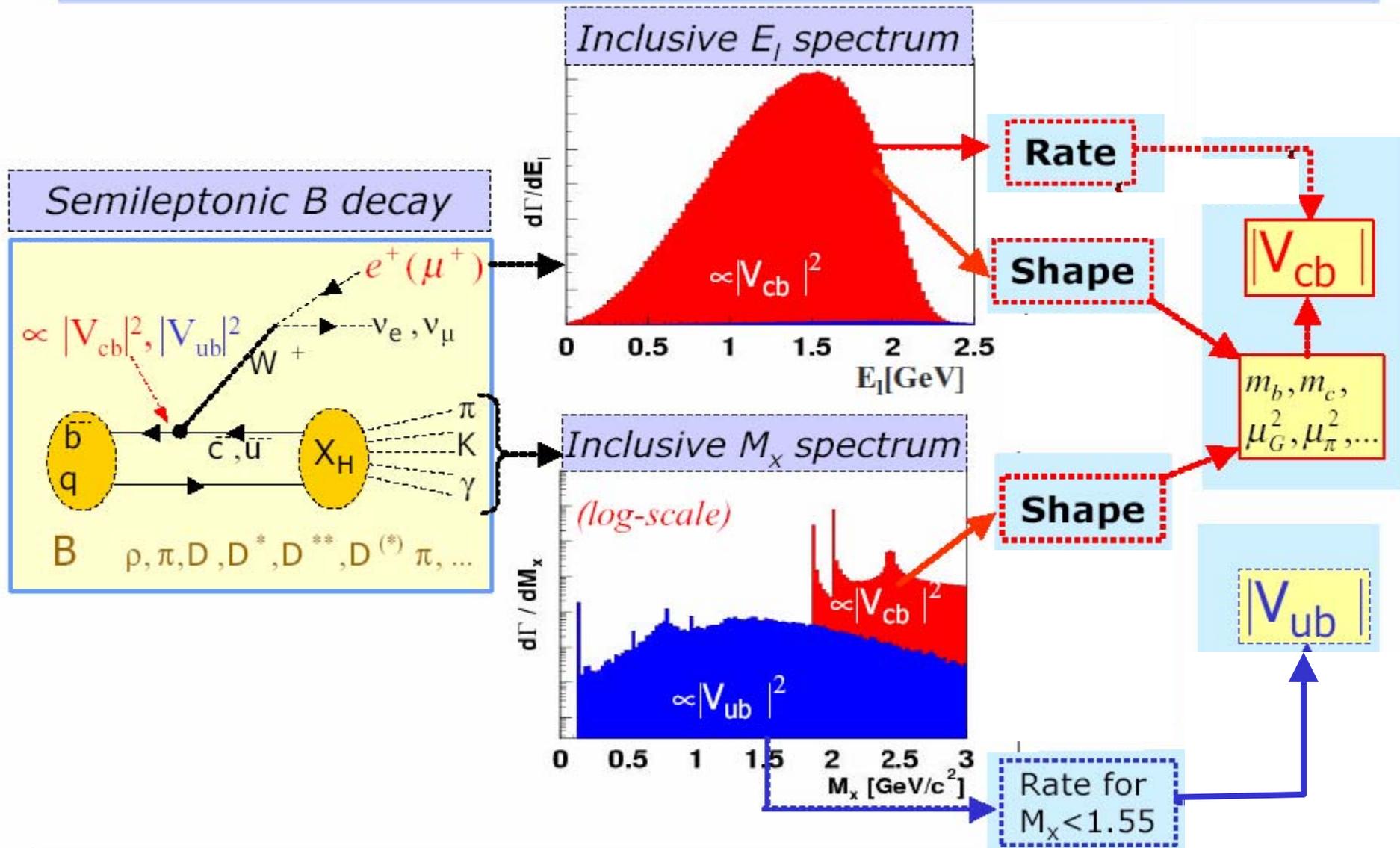


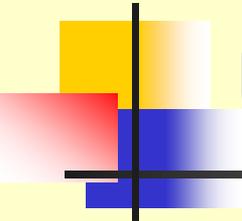
Why we study SL decays

- $|V_{ub}|$ and $|V_{cb}|$ are crucial in testing CKM unitarity and SM mechanism for CP violation
- Presence of a single hadronic current allows control of theoretical uncertainties
 - precise determinations of $|V_{ub}|$ and $|V_{cb}|$
- SL decays also provide a laboratory for probing our ability to calculate hadronic quantities in the presence of a mix of scales in QCD



Inclusive Decays – the Big Picture





Understanding inclusive SL decays

- The Operator Product Expansion provides a systematic method of separating perturbative from non-perturbative scales
- OPE + Heavy Quark symmetry^[1] \rightarrow HQE
- Heavy Quark Expansion now calculated to α_s^2 , m_B^{-3}

Essentially all we need to know for $b \rightarrow c\ell\nu$

- Coefficients of operators calculated perturbatively (EW and QCD); non-perturbative physics enters through matrix elements of operators

[1] soft gluons cannot probe heavy quark properties

Semileptonic B Decays & HQE

$$\Gamma(B \rightarrow X_c \ell \nu) = \frac{G_F^2 m_b^5}{192 \pi^3} |V_{cb}|^2 (1 + A_{EW}) \times \left[\mathbf{z}_0(r) \left[1 + A_3^{pert}(r, \mu) \right] \left(1 - \frac{\mu_\pi^2 - \mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{2m_b^2} \right) - (1 + A_5^{pert}(r, \mu)) 2(1-r)^4 \frac{\mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{m_b^2} + \mathbf{d}(r) \frac{\rho_D^3}{m_b^3} + O\left(\frac{1}{m_b^4}\right) \right]$$

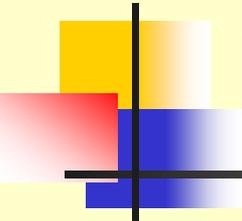
free-quark rate

$\mu =$ scale which separates effects from long- and short-distance dynamics

$r = m_c/m_b$; $\mathbf{z}_0(r)$, $\mathbf{d}(r)$: phase space factors; A_{EW} = EW corrections; A^{pert} = pert. corrections (α_s^j , $\alpha_s^k \beta_0$)

- contains b- and c-quark masses, m_b and m_c No $1/m_b$ term!
- μ_π^2 related to kinetic energy of b-quark
- μ_G^2 related to chromomagnetic operator: B / B* mass splitting
- Darwin term (Q_D^3) and spin-orbit interaction (Q_{LS}^3) enter at $1/m_b^3$

Several HQE schemes exist; op's and coeff's are scheme dependent



Inclusive $b \rightarrow c \ell \nu$

- Measure electron momentum spectrum and mass of hadronic system in SL decay
- Determine *moments* to allow comparison with parton-level calculations (duality assumed)
- Calculations exist for the following:

Lepton energy spectrum

$$\langle E_l^n \rangle_{E_l > E_0} = \tau_B \int_{E_0} E_l^n d\Gamma = f_n^\ell(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_D^3, \rho_{LS}^3)$$

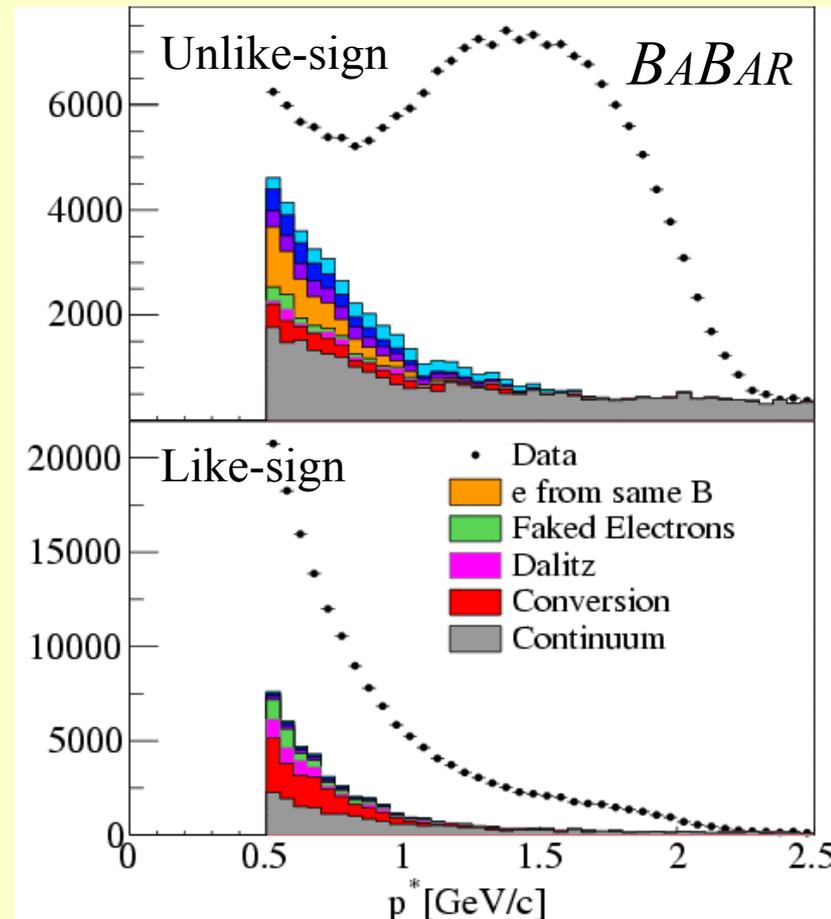
Mass of hadronic system

$$\langle M_x^n \rangle_{E_l > E_0} = \tau_B \int_{E_0} M_x^n d\Gamma = f_n^x(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_D^3, \rho_{LS}^3)$$

- Fit for HQE parameters and $|V_{cb}|$

Electron Energy Spectrum

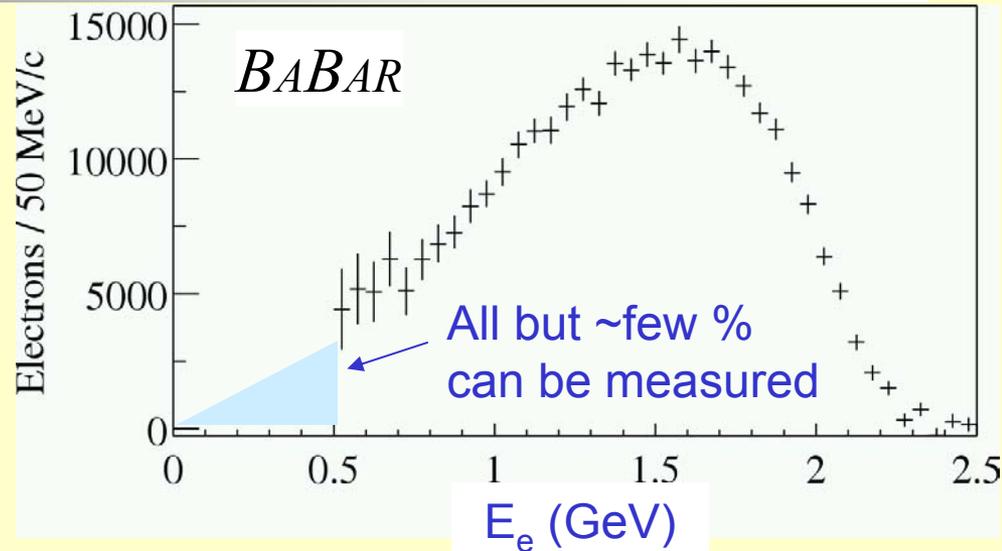
- BABAR data, 47.4 fb^{-1} at $Y(4S)$ + 9.1 fb^{-1} off-peak
- Select events with an electron having $p^* > 1.4 \text{ GeV}$; study spectrum of 2nd electron for $p^* > 0.5 \text{ GeV}$ as fⁿ of charge
 - Unlike-sign events dominated by $B \rightarrow X_c e \nu$
 - Like-sign events from $D \rightarrow X e \nu$, B^0 mixing
- As done by ARGUS, CLEO...



Electron Energy Spectrum

- Determine E_e spectrum

- Subtract $B \rightarrow X_u e \nu$
- Correct for efficiency
- Correct for the detector material (Bremsstrahlung)

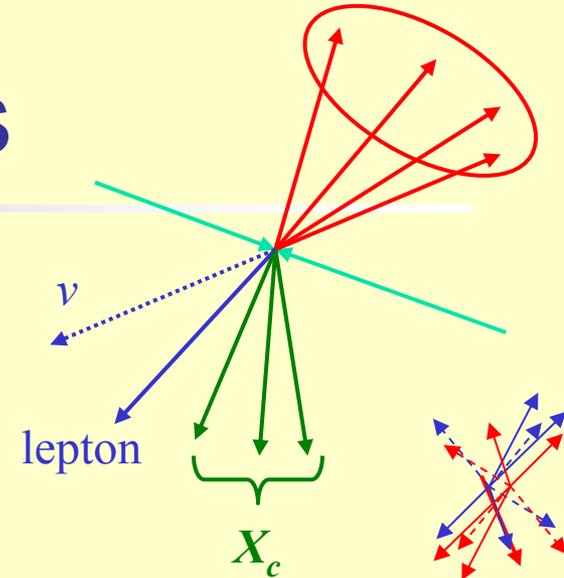


- Move from $Y(4S)$ to B rest frame
- Correct for the final state radiation using PHOTOS

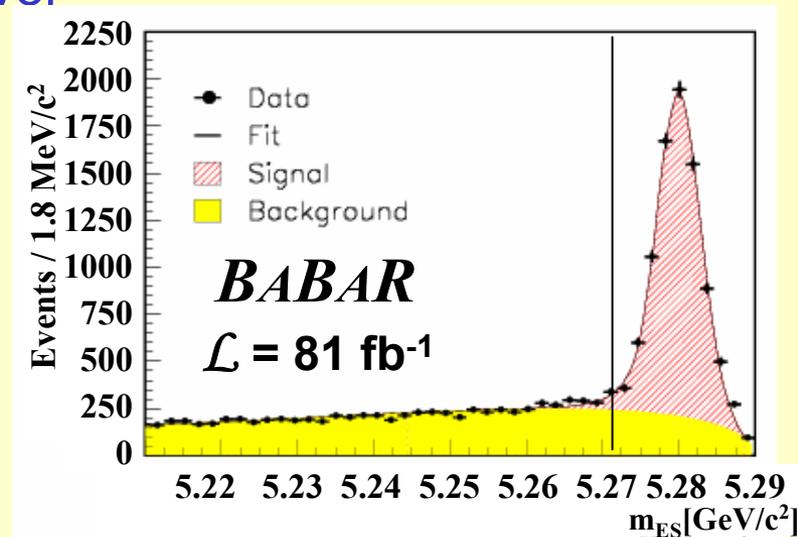
- Calculate 0th-3rd E_e moments for $E_0 = 0.6 \dots 1.5$ GeV

Hadron Mass Moments

- Select events with a **fully-reconstructed B**
 - Use ~ 1000 decay chains $\underline{B} \rightarrow D[(n\pi)(mK)]^-$
 - Flavor and momentum of “recoil” B known
- Find a **lepton** with $E > E_0$ in the recoil- B
 - Lepton charge consistent with the B flavor
 - m_{miss} consistent with a neutrino
- All remaining particles belong to X_c
 - Improve m_X with a kinematic fit (require $m_{B2} = m_{B1}$ and $m_{\text{miss}} = 0$)
 - Gives $\sigma(m_X) = 350 \text{ MeV}$

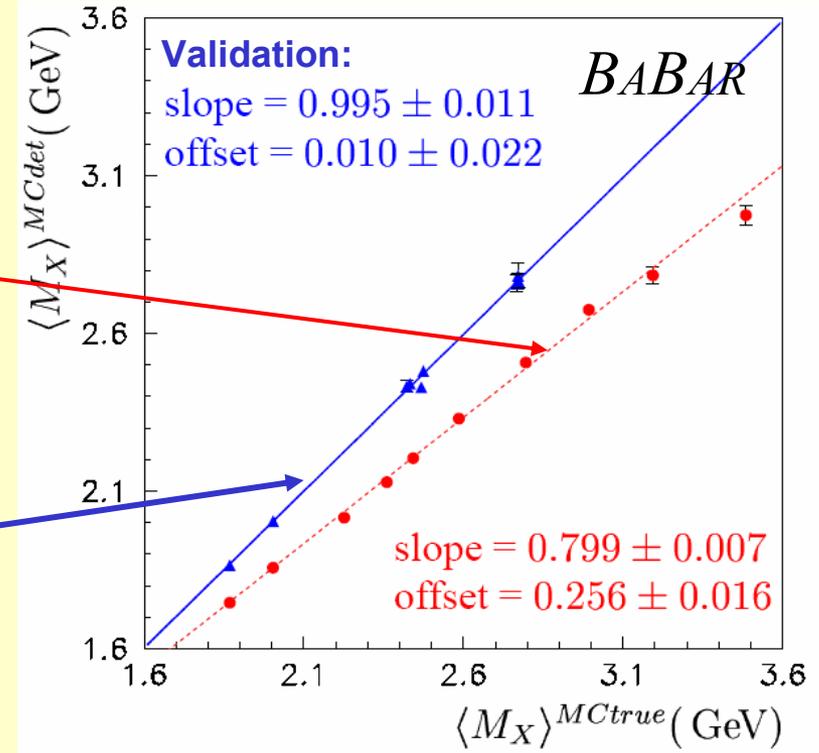


Fully reconstructed
 $B \rightarrow \text{hadrons}$



Hadron Mass Moments

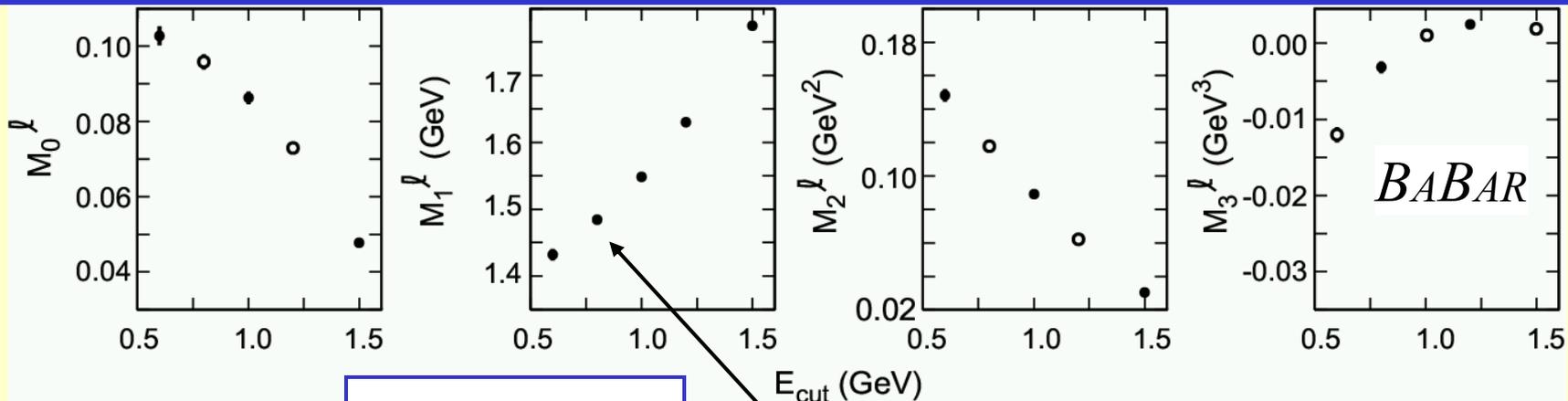
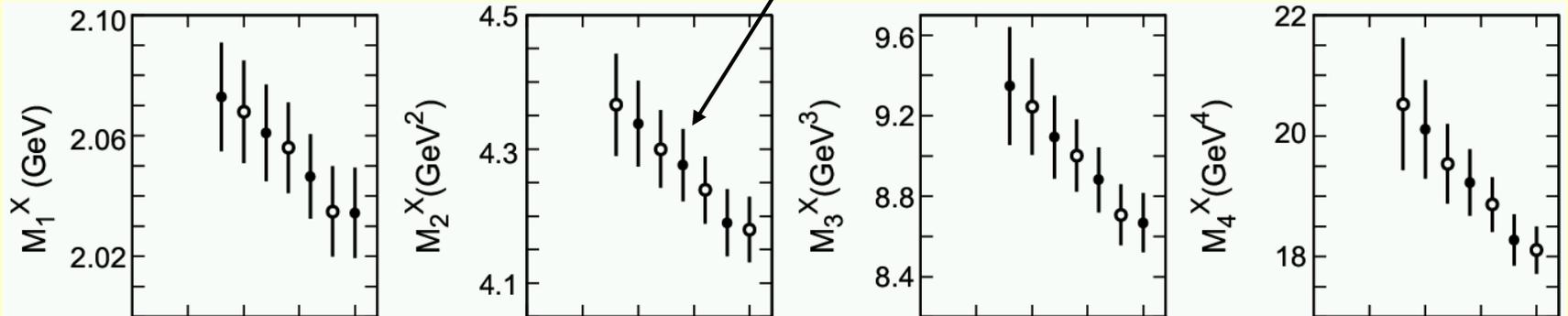
- Unmeasured particles → measured $m_X < \text{true } m_X$
 - Calibrate using simulation
 - Depends (weakly) on decay multiplicity and m_{miss}
 - Validate in MC after applying correction
 - Validate on data using partially reconstructed $D^{*\pm} \rightarrow D^0 \pi^\pm$, tagged by the soft π^\pm and lepton
- Calculate 1st-4th mass moments with $E_0 = 0.9 \dots 1.6$ GeV



Inputs to OPE Fit

m_X moments

Error bars are stat. & syst.
with comparable sizes



E_ℓ moments

Error bars (sys+stat) are
smaller than point size

Fit Parameters

- Calculation by Gambino & Uraltsev (hep-ph/0401063, 0403166)

- Kinetic mass scheme to $O(1/m_b^3)$

- E_ℓ moments $O(\alpha_s^2)$

- m_X moments $O(\alpha_s)$

- 8 parameters to determine

$|V_{cb}|$ m_b m_c $B(B \rightarrow X_c \ell \nu)$ μ_π^2 μ_G^2 ρ_D^3 ρ_{LS}^3

kinetic

chromomagnetic

 $O(1/m_b^2)$

spin-orbit

Darwin

 $O(1/m_b^3)$

- 8 moments available with several E_0

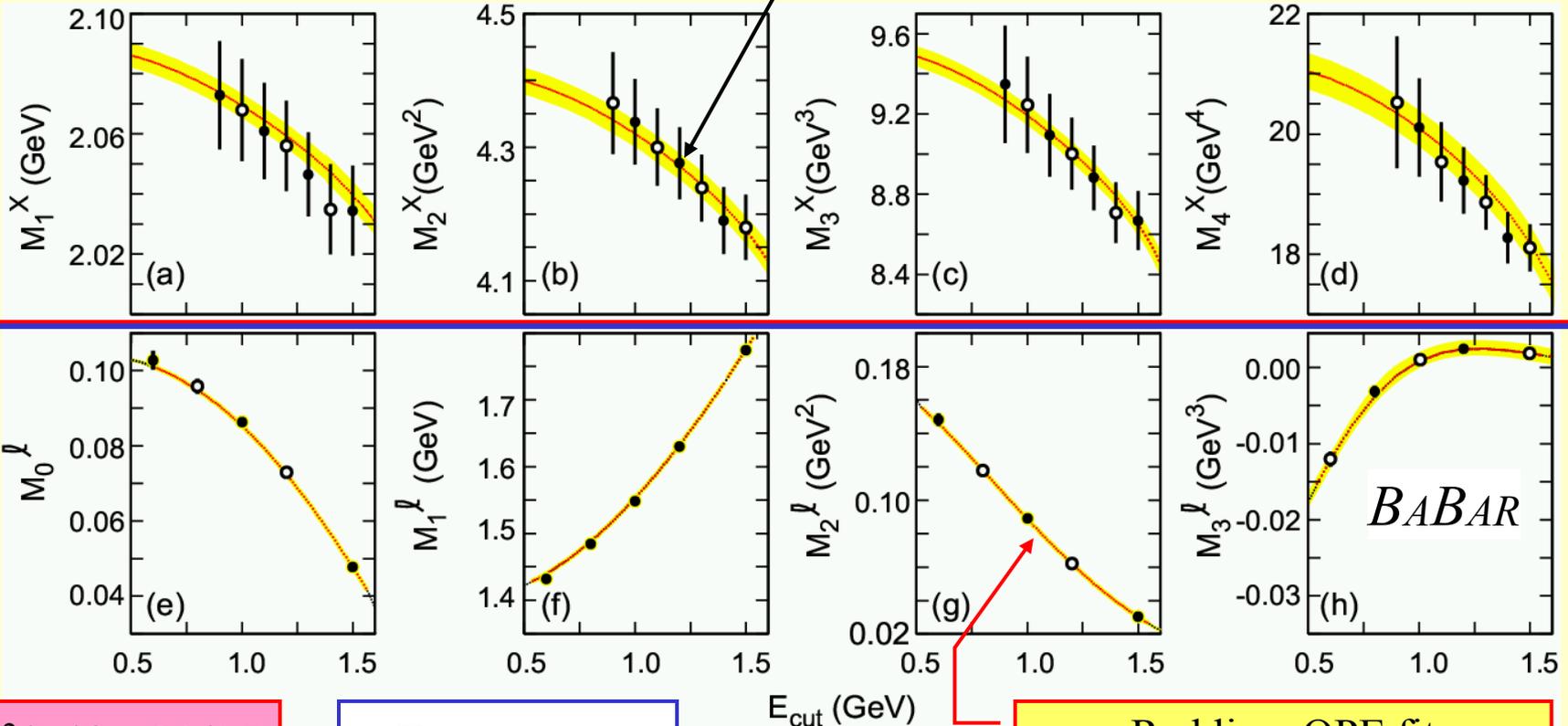
- Sufficient degrees of freedom to determine all parameters without external inputs

- Fit quality tells us how well OPE works

Fit Results

m_X moments

● = used, ○ = unused
in the nominal fit



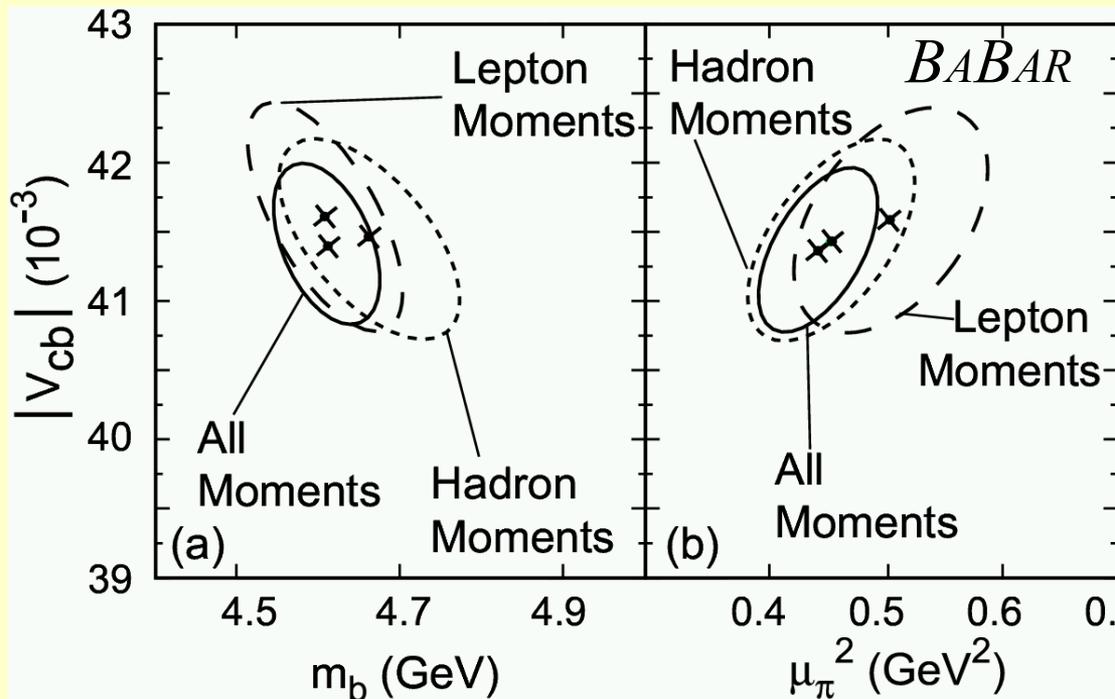
$\chi^2/ndf = 20/15$

E_{ℓ} moments

Red line: OPE fit
Yellow band: theory errors

Fit Consistency

- OPE describes BABAR data very well
 - $\chi^2/\text{ndf} = 20/15$
 - Separate fits of E_e and m_x moments agree



Fit Results

precision on
 $|V_{cb}| = 2\%$

$$|V_{cb}| = (41.4 \pm 0.4_{\text{exp}} \pm 0.4_{\text{HQE}} \pm 0.6_{\text{th}}) \times 10^{-3}$$

$$B_{cl\nu} = (10.61 \pm 0.16_{\text{exp}} \pm 0.06_{\text{HQE}})\%$$

precision on
 $m_b = 1.5\%$

$$m_b = (4.61 \pm 0.05_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV}$$

$$m_c = (1.18 \pm 0.07_{\text{exp}} \pm 0.06_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV}$$

$$\mu_\pi^2 = (0.45 \pm 0.04_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.01_{\alpha_s}) \text{ GeV}^2$$

$$\mu_G^2 = (0.27 \pm 0.06_{\text{exp}} \pm 0.03_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV}^2$$

$$\rho_D^3 = (0.20 \pm 0.02_{\text{exp}} \pm 0.02_{\text{HQE}} \pm 0.00_{\alpha_s}) \text{ GeV}^3$$

$$\rho_{LS}^3 = (-0.09 \pm 0.04_{\text{exp}} \pm 0.07_{\text{HQE}} \pm 0.01_{\alpha_s}) \text{ GeV}^3$$

Uncalculated
corrections to Γ

kinetic mass scheme
with $\mu=1 \text{ GeV}$

Fitted values
consistent with
external knowledge

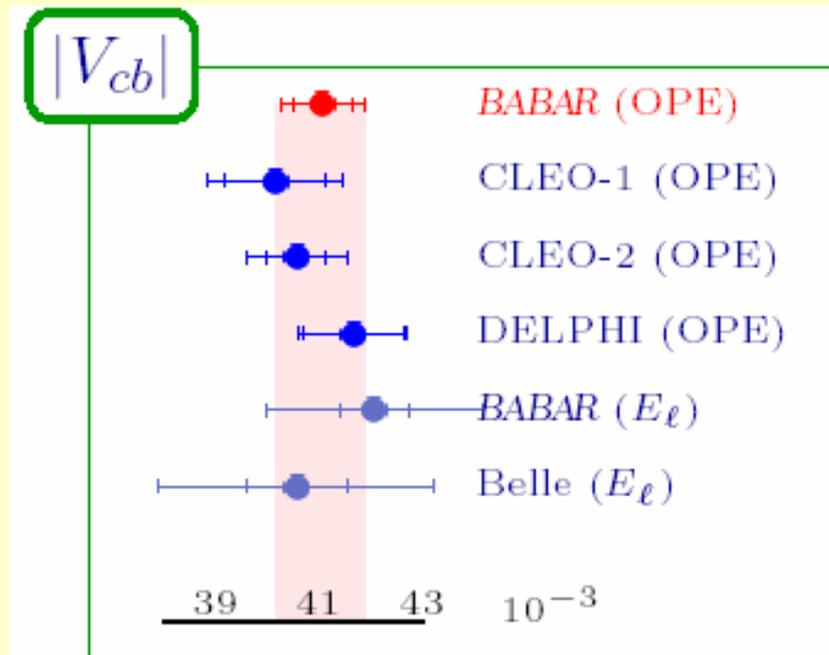
$$\chi^2/\text{ndf} = 20/15$$

- Impressive agreement between data and theory
- \approx identical results obtained in another renorm. scheme:

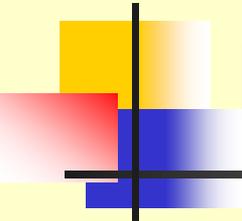
Bauer, Ligeti, Luke, Manohar, Trott in hep-ph/0408002

Inclusive $|V_{cb}|$ status

- BaBar result compared with previous measurements:



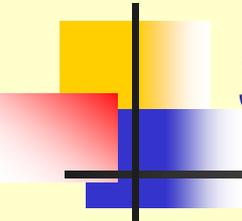
- Agrees with value coming from exclusive $B \rightarrow D^* \ell \nu$ decays (from HFAG): $|V_{cb}| = (41.4 \pm 1.0_{\text{expt}} \pm 1.8_{\text{theo}}) \times 10^{-3}$



Inclusive $b \rightarrow u$

- Limiting factor in CKM precision tests; known much less well than $|V_{cb}|$
- CKM suppressed – therefore harder to measure
- Challenge for experiment and theory

- Overview of theory uncertainties
- Overview of measurements
- Prospects



Starting point: HQE

- Just like $b \rightarrow c \ell \nu \dots$, and with similar accuracy

$$\Gamma(B \rightarrow X_u \ell \nu) = (1 + A_{EW}) \frac{G_F^2 m_b^5}{192 \pi^3} |V_{ub}|^2 \left[\left[1 + A_3^{pert}(\mu) \right] \left(1 - \frac{\mu_\pi^2 - \mu_G^2}{2m_b^2} \right) - (1 + A_5^{pert}(\mu)) 2 \frac{\mu_G^2}{m_b^2} + O\left(\frac{1}{m_b^3}\right) \right]$$

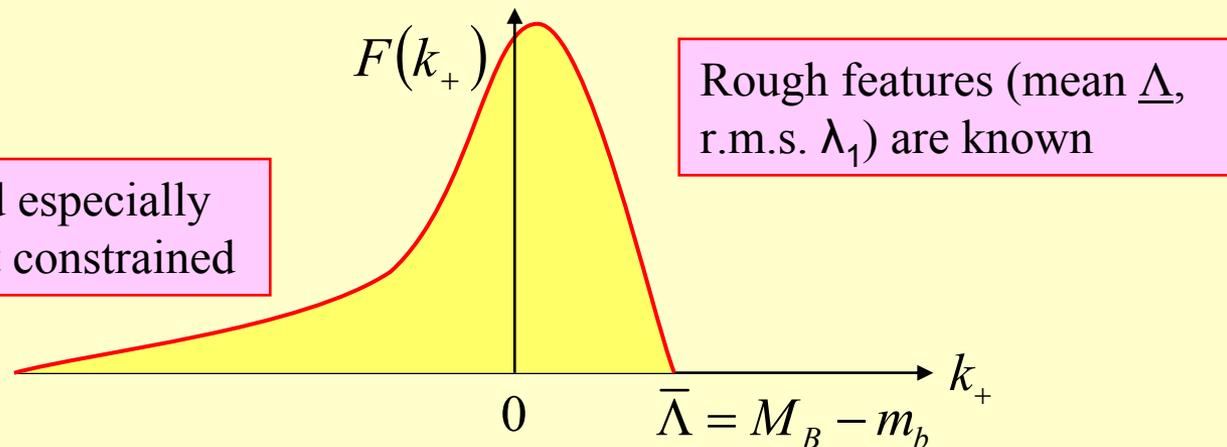
μ = scale which separates effects from long- and short-distance dynamics

A_{EW} = EW corrections; A^{pert} = pert. corrections ($\alpha_s^j, \alpha_s^k \beta_0$)

- ...until limited expt'l acceptance is considered
- Poor convergence of OPE in region where $b \rightarrow c \ell \nu$ decays are kinematically forbidden
- Non-perturbative **Shape Function** must be used to calculate partial rates

Shape Function – what is it?

- light-cone momentum distribution of b quark: $F(k_+)$
- Property of a B meson; universal...but new “sub-leading” SFs arise at each order in $1/m_b$
- Consequences: changes effective m_b , smears spectra



Measuring the Shape Function

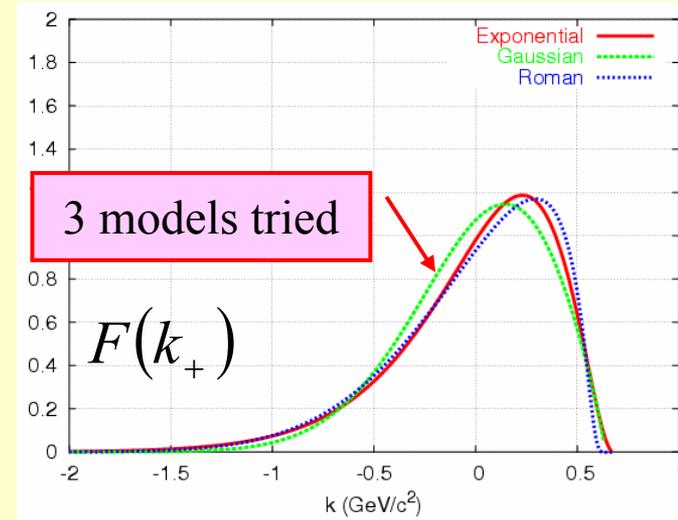
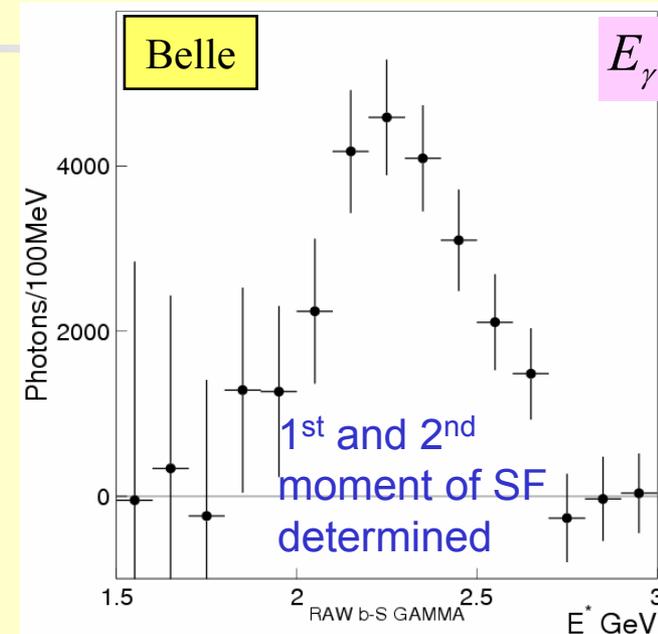
- SF can't be calculated: **measure it!**
- Photon energy distribution in $b \rightarrow s\gamma$ probes b quark directly; same is in $b \rightarrow u\ell\nu$ to $O(1/m_b)$

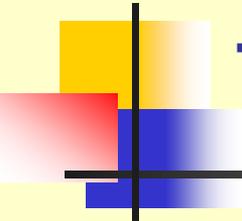
It's a hard measurement...

NEW!

SF moments are related to HQE parameters: Bosch-Lange-Neubert-Paz, hep-ph/0402094; Benson-Bigi-Uraltsev, hep-ph/0410080.

Further constrains SF models



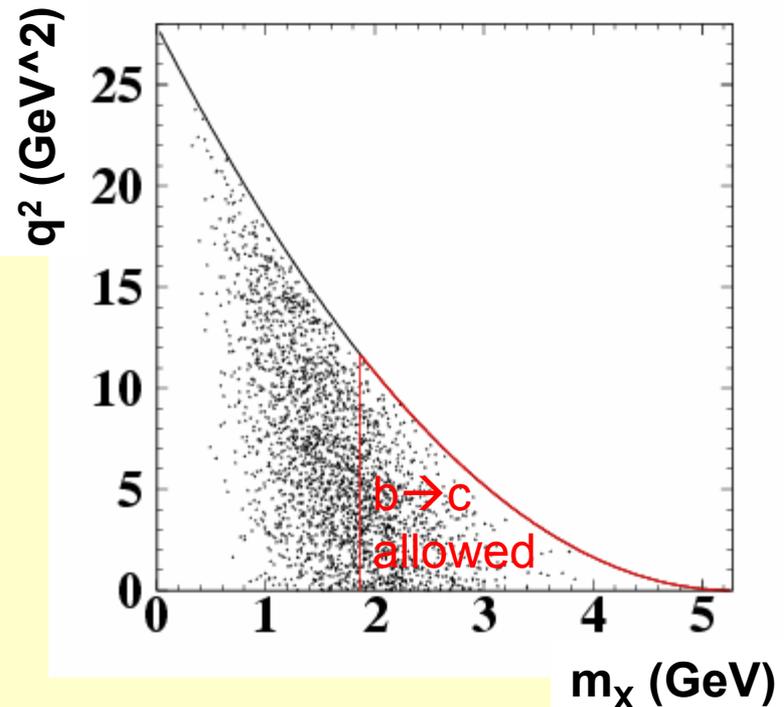
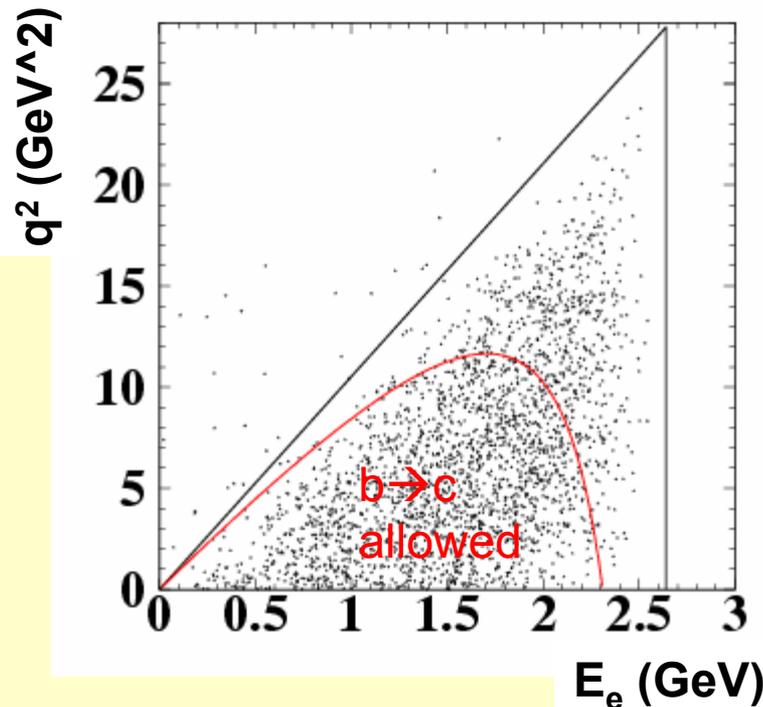


Theory input for $|V_{ub}|$

- At present, all $|V_{ub}|$ measurements based on inclusive SL decays use fully differential SL rate calculated to $O(\alpha_S, m_b^{-2})$ (DeFazio and Neubert, JHEP 06:017 (1999))
- Input required includes values for the mean and r.m.s. of the Shape Function.
- In what follows we use as input the parameters determined by a fit (hep-ex/0407052) to the Belle $b \rightarrow s\gamma$ spectrum:
 $\underline{\Delta} = 0.66 \text{ GeV}$, $\lambda_1 = -0.40 \text{ GeV}^2$ + associated covariance; $\delta\underline{\Delta} \sim \delta m_b \approx 80 \text{ MeV}$

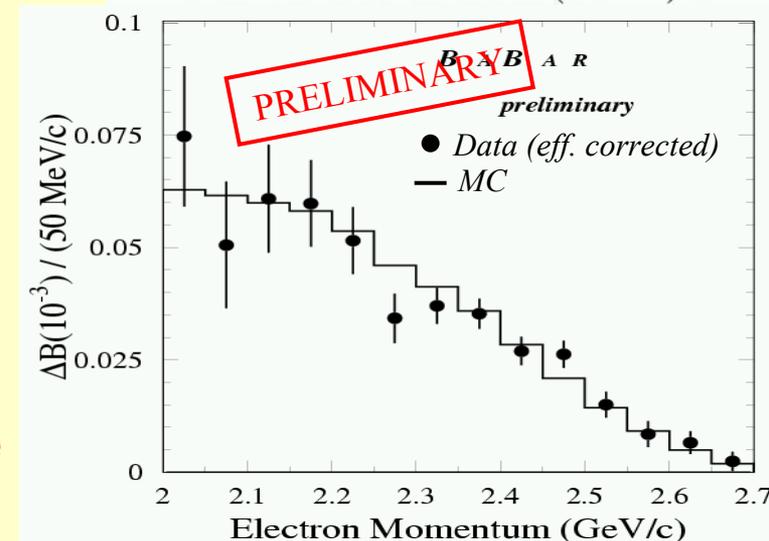
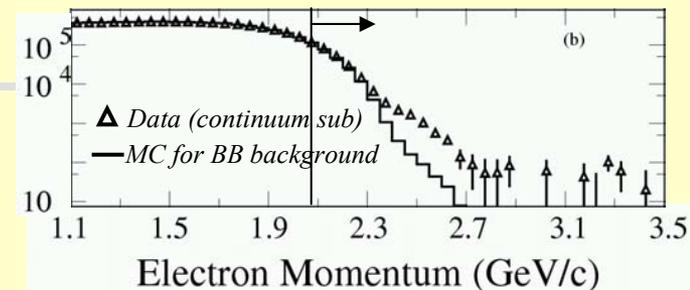
Experimental approaches

- Must suppress $b \rightarrow c \ell \nu$; rate is 50x higher than signal
- Kinematic variables: E_e , $q^2 = (\mathbf{p}_e + \mathbf{p}_\nu)^2$ and m_{X_u}
- E_e easy, q^2 more difficult, m_{X_u} hardest



Electron Endpoint

- 80 fb^{-1} on $Y(4S)$ resonance
- Select e^\pm in $2.0 < E_\ell < 2.6 \text{ GeV}$
 - Larger signal acceptance \rightarrow smaller theoretical error
- Accurate model of background is crucial ($S/N \sim 1/14$)
 - Data taken below the $Y(4S)$ resonance determine the light-flavor background
 - Fit E_e spectrum with $b \rightarrow ulv$, $B \rightarrow Dlv$, $B \rightarrow D^*lv$, $B \rightarrow D^{**}lv\dots$
Entries $>2.2 \text{ GeV}$ put in 1 bin to reduce signal model dependence
 - Fully correct spectrum for efficiency, resolution, radiation, etc.



Electron Endpoint

- Fully corrected partial BF in Y(4S) frame:

$$\Delta B(B \rightarrow X_u e \nu, E_e > 2.0 \text{ GeV}) = (4.85 \pm 0.29_{\text{stat}} \pm 0.53_{\text{sys}}) \times 10^{-4}$$

- Translate ΔB into $|V_{ub}|$:

	E_e (GeV)	ΔB (10^{-4})	$ V_{ub} $ (10^{-3})
BABAR	2.0–2.6	$4.85 \pm 0.29_{\text{stat}} \pm 0.53_{\text{sys}}$	$4.40 \pm 0.13_{\text{stat}} \pm 0.25_{\text{sys}} \pm 0.38_{\text{theo}}$
CLEO	2.2–2.6	$2.30 \pm 0.15_{\text{exp}} \pm 0.35_{\text{sys}}$	$4.69 \pm 0.15_{\text{stat}} \pm 0.40_{\text{sys}} \pm 0.52_{\text{theo}}$
Belle	2.3–2.6	$1.19 \pm 0.11_{\text{exp}} \pm 0.10_{\text{sys}}$	$4.46 \pm 0.20_{\text{stat}} \pm 0.22_{\text{sys}} \pm 0.59_{\text{theo}}$

- Significant decrease in **theory uncertainty** at lower E_e (SF sensitivity is substantially reduced)

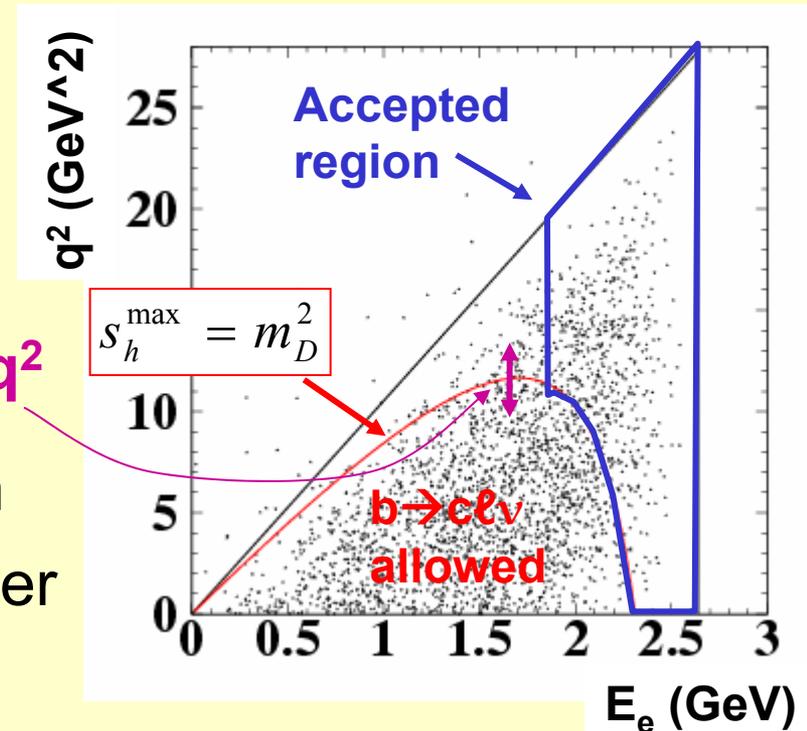
E_e vs. q^2

- Use $\mathbf{p}_\nu = \mathbf{p}_{\text{miss}}$ in addition to $\mathbf{p}_e \rightarrow$ Calculate q^2
 - Given E_e and q^2 , maximum possible m_x^2 is (in B frame)

$$s_h^{\text{max}} = m_B^2 + q^2 - 2m_B \left(E_e + \frac{q^2}{4E_e} \right)$$

+small modifications for Y(4S) frame

- Resolution on \mathbf{p}_ν modest; some $b \rightarrow c\ell\nu$ decays smeared to higher q^2
- Acceptance $\sim 25\%$ less than cut on E_e alone, but $S/N=1/2$ is much better



E_e vs. q^2

- 80 fb⁻¹ on Y(4S) resonance
 - Subtract off-peak data
 - $B \rightarrow D^{(*)}e\nu$ control samples used to validate ν reco
 - Subtract BB background normalized by sideband

- Unfolded partial BF:

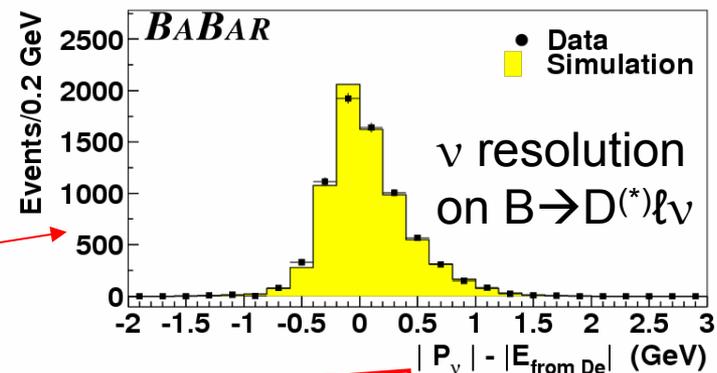
$$\Delta B = (4.46 \pm 0.93) \times 10^{-4}$$

- Total $b \rightarrow u\ell\nu$ BF:

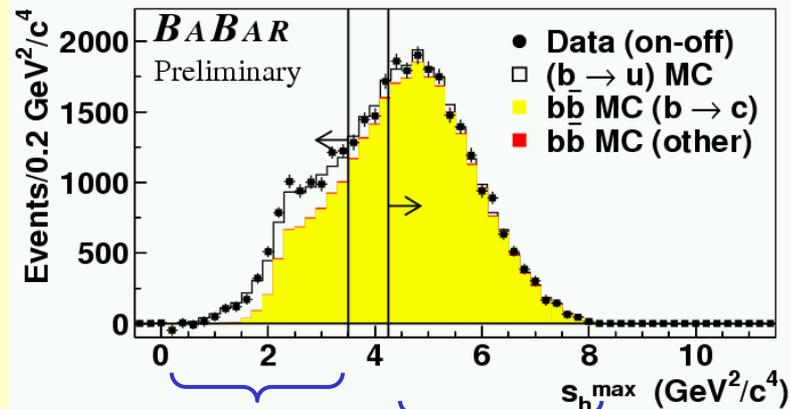
$$B = (2.76 \pm 0.26_{\text{stat}} \pm 0.50_{\text{syst}} \pm 0.21_{\text{SF}}) \times 10^{-3}$$

- Translate to $|V_{ub}|$

$$|V_{ub}| = (4.99 \pm 0.48_{\text{exp}} \pm 0.18_{\text{SF}} \pm 0.22_{\text{OPE}}) \times 10^{-3}$$



PRELIMINARY

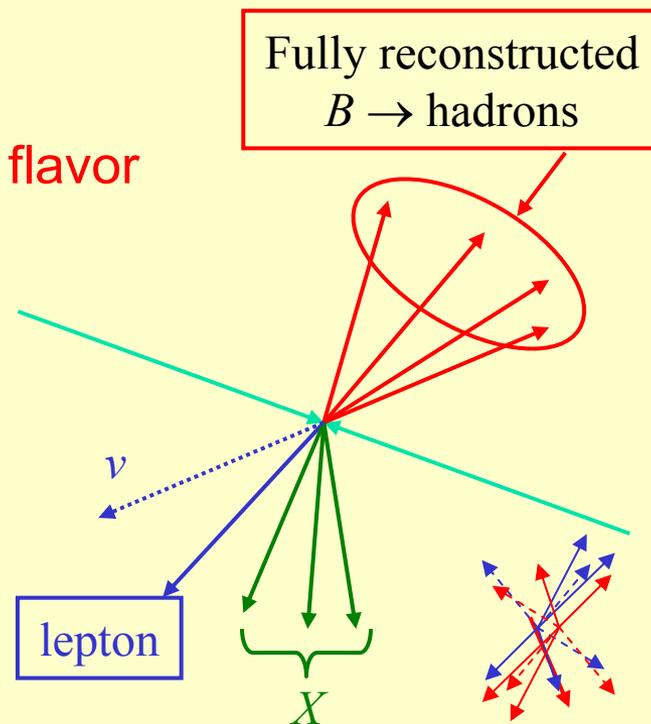


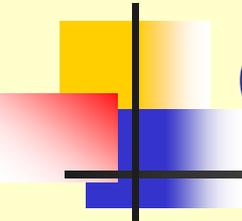
extract
signal

normalize
bkg

$b \rightarrow u\ell\nu$ in tagged events

- Same recoil technique as for $b \rightarrow c\ell\nu$ $\langle m_X \rangle$ moments
 - Find a lepton ($p_\ell > 1\text{GeV}$) in recoil B
 - Lepton charge consistent with the B flavor
 - m_{miss} consistent with a neutrino
- All left-over particles belong to X
 - Improve m_X with a kinematic fit
 - Calculate q^2 of lepton-neutrino
 - Calculate anything you want!

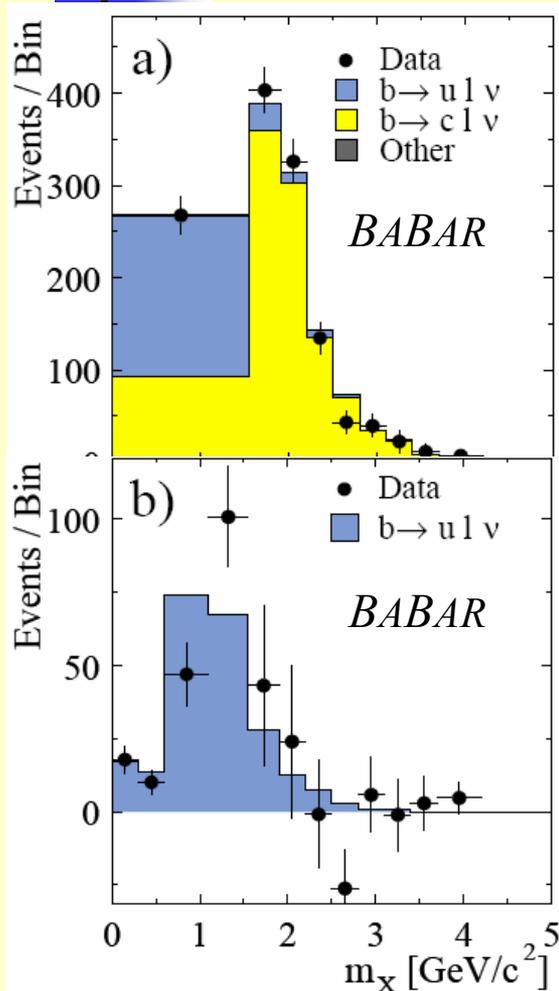




Charm suppression cuts

- Suppress $b \rightarrow c\ell\nu$ by vetoing $D^{(*)}$ decays
 - D decays usually produce at least one kaon
 - ➔ Reject events with K^\pm and K_S
 - $B^0 \rightarrow D^{*+}(\rightarrow D^0\pi^+)\ell^-\nu$ has peculiar kinematics
 - D^{*+} momentum can be estimated from π^+ alone
 - Calculate $m_\nu^2 = (p_B - p_{D^*} - p_\ell)^2$ for all π^+
 - ➔ Reject events consistent with $m_\nu^2 = 0$
- Vetoed events are depleted in $b \rightarrow u\ell\nu$
 - Use them to validate simulation of background distributions

Fitting m_X



- BABAR data, 80 fb⁻¹ on resonance
 - Simple fit in m_X shows clear $b \rightarrow u l \nu$ signal (S/N ~ 2/1 for $m_X < 1.55$ GeV)
- Inclusive BF measured to be

$$B(B \rightarrow X_u l \nu) = (2.81 \pm 0.32_{\text{stat}} \pm 0.31_{\text{syst}} \pm 0.23_{\text{theo}}) \times 10^{-3}$$



$$|V_{ub}| = (5.22 \pm 0.30_{\text{stat}} \pm 0.31_{\text{syst}} \pm 0.43_{\text{theo}}) \times 10^{-3}$$

m_X vs. q^2

- 2-D fit to measure ΔB in $\{m_X < 1.7, q^2 > 8\}$

- Different theory uncertainty than pure m_X cut
- Good resolution allows clean extraction of ΔB

$$\Delta B = (0.90 \pm 0.14_{\text{stat}} \pm 0.14_{\text{syst}} \pm 0.01_{\text{theo}}) \times 10^{-3}$$

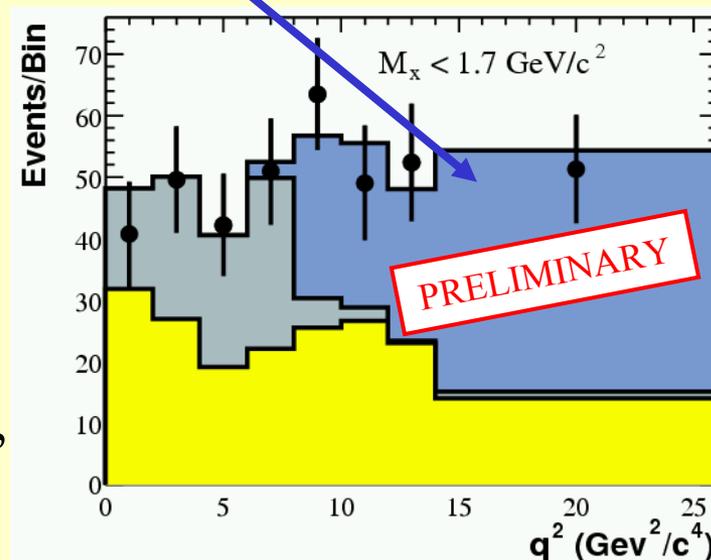
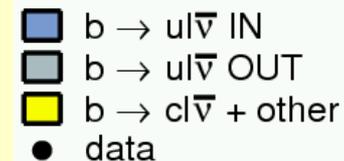
- Signal event fraction into the “box” taken from theory

$$|V_{ub}| = (4.98 \pm 0.40_{\text{stat}} \pm 0.39_{\text{syst}} \pm 0.47_{\text{theo}}) \times 10^{-3}$$

$$|V_{ub}| = (5.18 \pm 0.41_{\text{stat}} \pm 0.40_{\text{syst}} \pm 0.25_{\text{theo}}) \times 10^{-3}$$

■ Bauer *et al.* hep-ph/0111387

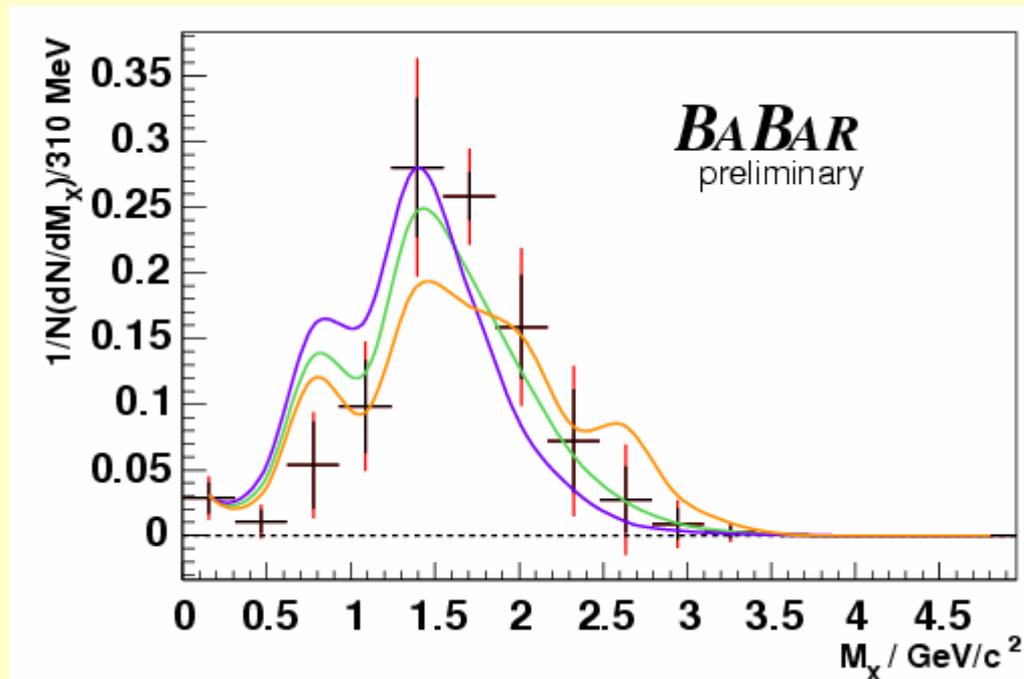
■ DeFazio-Neubert, JHEP 06:017 (1999)



Unfolding the m_x distribution

- The shape of the m_x distribution in $b \rightarrow u \ell \nu$ decays carries information about SF parameters ($b \rightarrow uW$ akin to $b \rightarrow s\gamma$)
- Moments can also be used to test OPE, as in $b \rightarrow c \ell \nu$
- Unfolding accounts for resolution, uncertainties in theory input...
- Measured moments:
 $M_2' = 2^{\text{nd}}$ central moment

	$M_0(\text{GeV})$	Value
M_1	1.86	$1.355 \pm 0.084 \text{ GeV}$
M_2'	1.86	$0.147 \pm 0.034 \text{ GeV}^2$
M_1	5.0	$1.584 \pm 0.233 \text{ GeV}$
M_2'	5.0	$0.270 \pm 0.099 \text{ GeV}^2$



BaBar Inclusive $|V_{ub}|$ Results

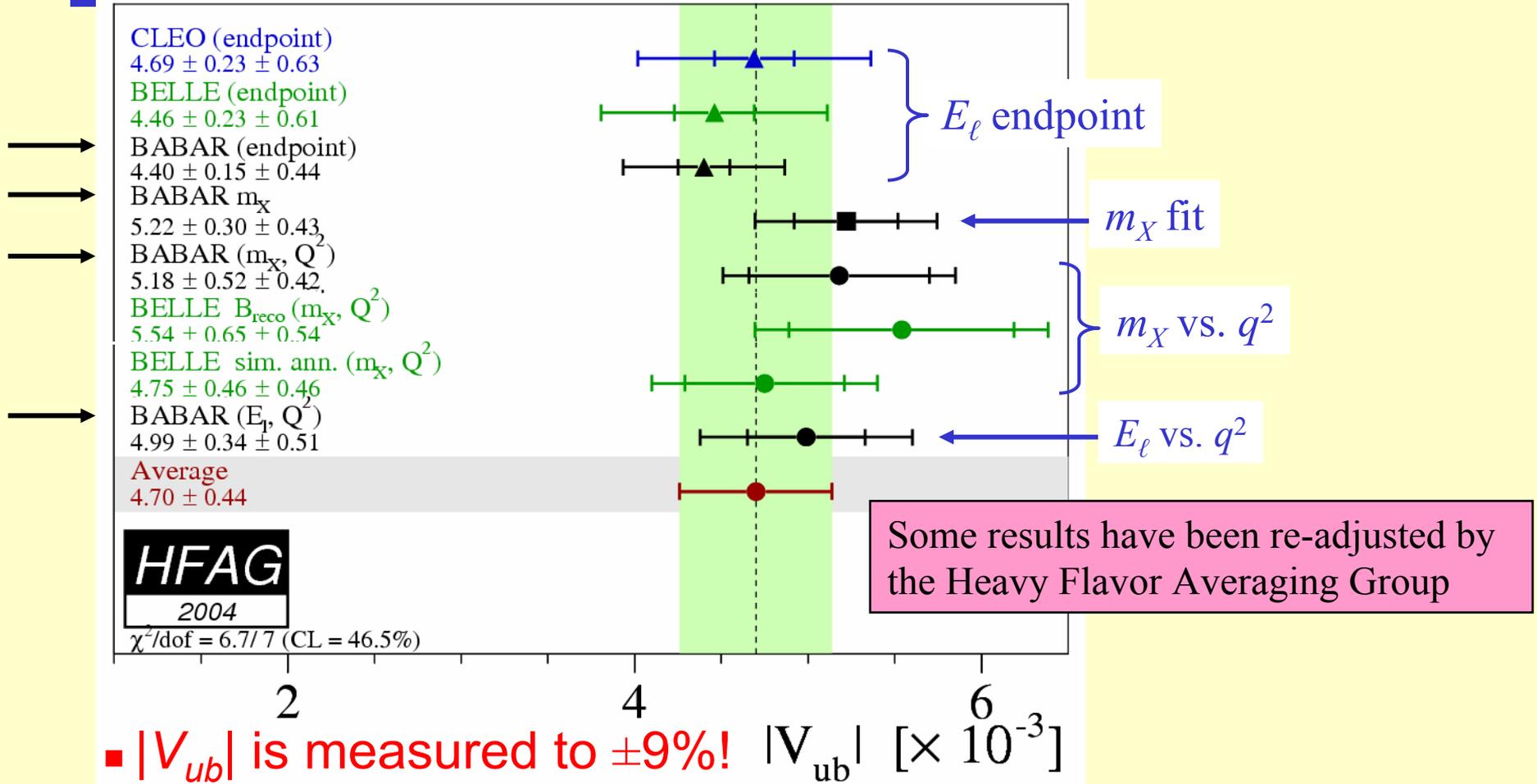
S/N increasing \downarrow
 acceptance increasing \downarrow
 statistics decreasing \downarrow

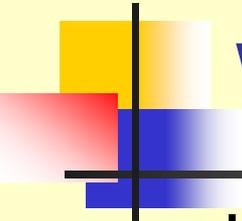
Technique	$ V_{ub} \times 10^3$
$E_\ell > 2.0$ GeV	$4.40 \pm 0.13_{\text{stat}} \pm 0.25_{\text{sys}} \pm 0.38_{\text{theo}}$
E_ℓ vs. q^2	$4.99 \pm 0.23_{\text{stat}} \pm 0.42_{\text{sys}} \pm 0.32_{\text{theo}}$
m_X vs. q^2	$5.18 \pm 0.41_{\text{stat}} \pm 0.40_{\text{sys}} \pm 0.23_{\text{theo}}$
$m_X < 1.55$ GeV	$5.22 \pm 0.30_{\text{stat}} \pm 0.31_{\text{sys}} \pm 0.43_{\text{theo}}$
average	4.80 ± 0.47, $\chi^2 = 3.5/3$

- Statistical correlation between the m_X and m_X - q^2 results is 72%. Others correlations negligible
- Each measurement has a somewhat different sensitivity to SF
- Average accounts for correlated systematic/theory errors

BABAR hep-ex/0408075
BABAR hep-ex/0408045
BABAR hep-ex/0408068

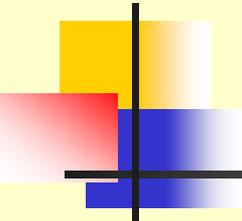
Inclusive $|V_{ub}|$ in Perspective





What to look for in future

- Improved precision of $|V_{ub}|$ requires **re-evaluation of theoretical uncertainties**
 - Precision on SF parameters $\underline{\Delta}$ and λ_1 will improve, due to
 - better $b \rightarrow s\gamma$ spectra and
 - the use of OPE parameters determined in $b \rightarrow c\ell\nu$ transitions
 - Power ($1/m_b$) corrections differ between $b \rightarrow u\ell\nu$ and $b \rightarrow s\gamma$
 - Quantitative estimates have appeared in literature
 - Weak annihilation may have a large (20%?) effect at high q^2
 - Difference between B^0 and B^+ needs to be measured
- Expect $|V_{ub}|$ averages to approach 5% uncertainty soon

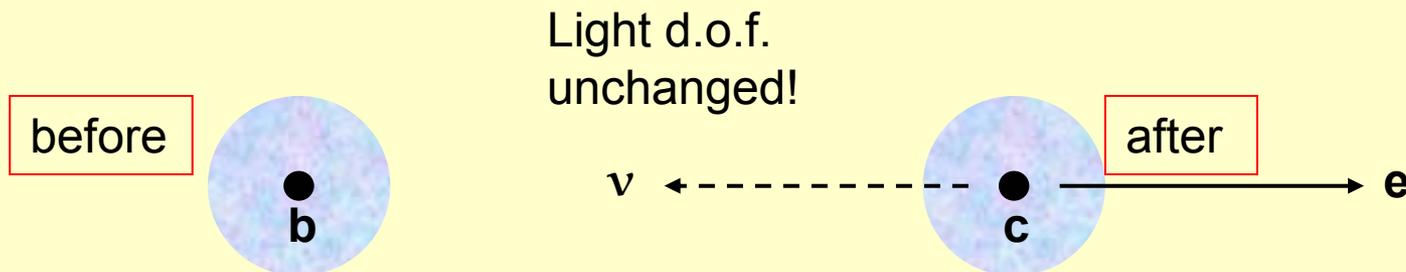


Exclusive $B \rightarrow X_c \ell \nu$ decays

- Measure $|V_{cb}|$ using a completely independent theoretical framework from that of inclusive decays
- Test HQET
- Reduce background uncertainty for other measurements, notably $|V_{ub}|$

$B \rightarrow D^* \ell \nu$ BF and $|V_{cb}|$

- Heavy Quark Effective Theory gives us a framework for understanding $B \rightarrow X_c \ell \nu$ transitions:
 - FF for decay depends only on q^2 : universal Isgur-Wise f^n
 - FF unknown, but normalization is unity in heavy quark limit ($m_b = m_c = \infty$) at “zero-recoil” point:



- Can be used with both $B \rightarrow D^* \ell \nu$ and $B \rightarrow D \ell \nu$ decays

What we measure

- $B \rightarrow D^* \ell \nu$ decay rate is given by

$$\frac{d\Gamma(B \rightarrow D^* \ell \nu)}{dw} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} F(w)^2 G(w)$$

Annotations:

- $d\Gamma/dw$: D^* boost in the B rest frame
- $F(w)^2$: form factor
- $G(w)$: phase space

- $\Phi(1) = 1$ in the heavy-quark limit; Lattice calculation gives

$$F(1) = 0.919^{+0.030}_{-0.035}$$

Hashimoto et al,
PRD 66 (2002) 014503

- Form of $\Phi(w)$ unknown

- Parameterized with ρ^2 (slope at $w = 1$) and ratios R_1 and R_2 of FFs that are \sim independent of w
- Use R_1 and R_2 determined by CLEO, PRL 76 (1996) 3898

- Measure $d\Gamma/dw$ to fit $\Phi(1)|V_{cb}|$ and ρ^2

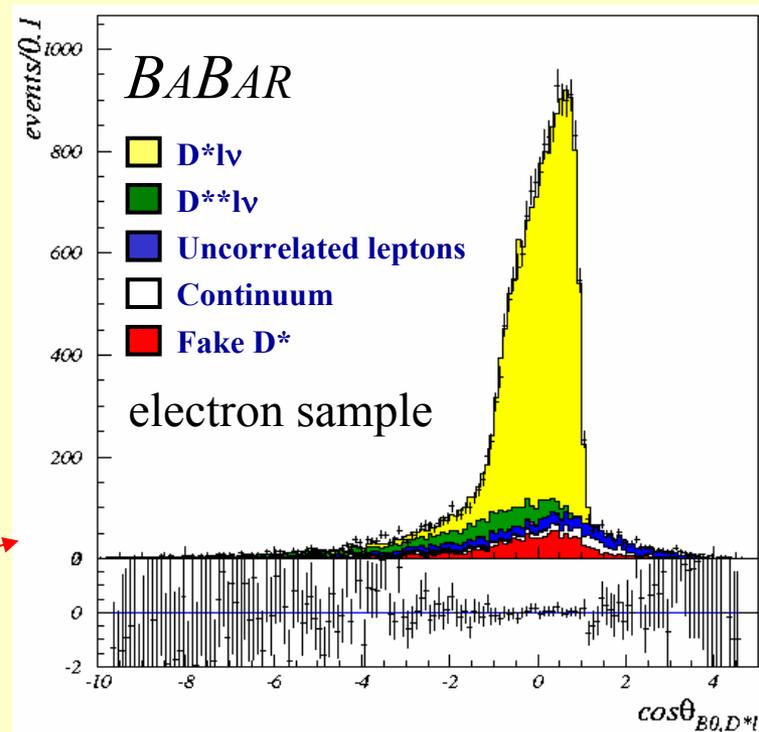
$B \rightarrow D^* \ell \nu$ Sample

- BABAR data, 80 fb⁻¹ on Y(4S)
- Find events with a D^{*+} and a lepton
 - $D^{*+} \rightarrow D^0 \pi^+$ with $D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^- \pi^+, K^- \pi^+ \pi^0$
 - $1.2 < p_\ell < 2.4$ GeV/c

■ Background

- Fake D^* : use $D^* - D$ mass difference
- True D^* but not $B \rightarrow D^* \ell \nu$: use variable sensitive to what accompanies $D^* \ell$:

$$\cos \theta_{BY} = \frac{2E_B E_{D^* \ell} - m_B^2 - m_{D^* \ell}^2}{2p_B p_{D^* \ell}}$$



Determination of $F(1)|V_{cb}|$

- Correct for efficiency $\rightarrow w$ distribution
 - Slow pion (from D^* decays) efficiency depends on w

- Fitting dN/dw gives

$$F(1)|V_{cb}| = (34.03 \pm 0.24_{\text{stat}} \pm 1.31_{\text{syst}}) \times 10^{-3}$$

$$\rho^2 = 1.23 \pm 0.02_{\text{stat}} \pm 0.28_{\text{syst}}$$

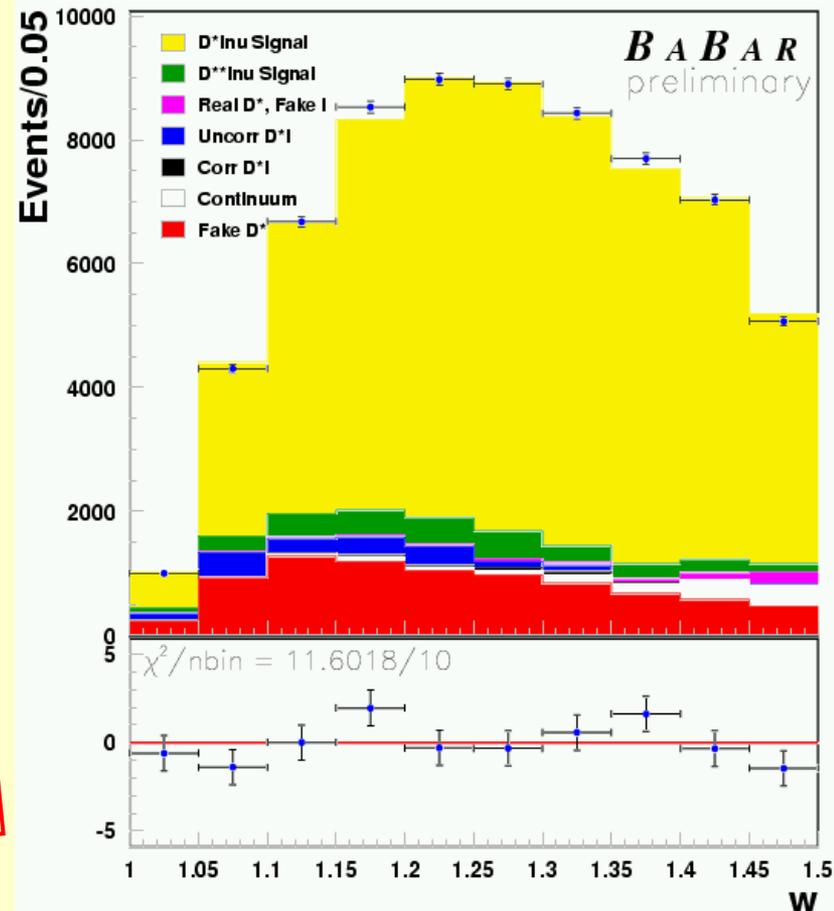
$$B_{D^*\ell\nu} = (4.68 \pm 0.03_{\text{stat}} \pm 0.29_{\text{syst}})\%$$

- FF ratios also under study: from ICHEP, being refined

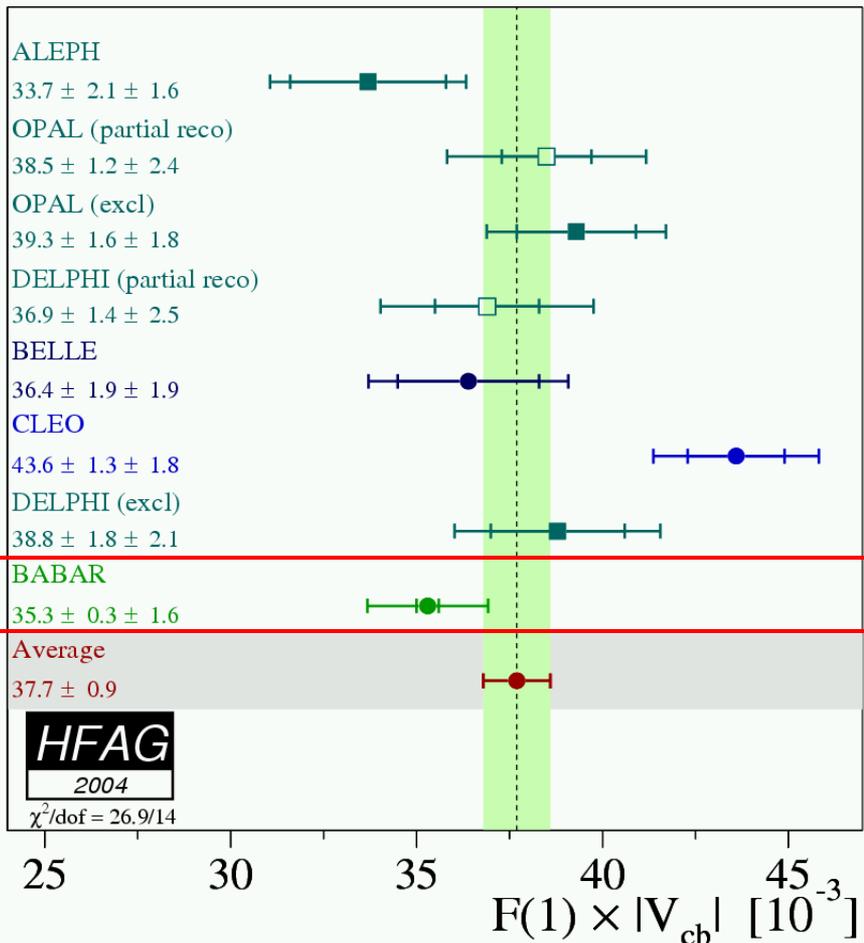
$$R_1 = 1.328 \pm 0.060 \pm 0.025$$

$$R_2 = 0.920 \pm 0.048 \pm 0.013$$

PRELIMINARY

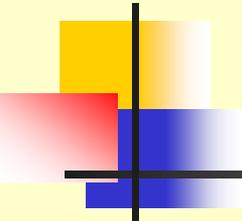


Determination of $|V_{cb}|$



- BABAR result compares well with existing measurements
 - ← Results adjusted to use common inputs
- Using $\Phi(1) = 0.91 \pm 0.04$, the world average is

$$|V_{cb}| = (41.4 \pm 1.0_{\text{expt}} \pm 1.8_{\text{theo}}) \times 10^{-3}$$
 - Agrees with the inclusive measurement



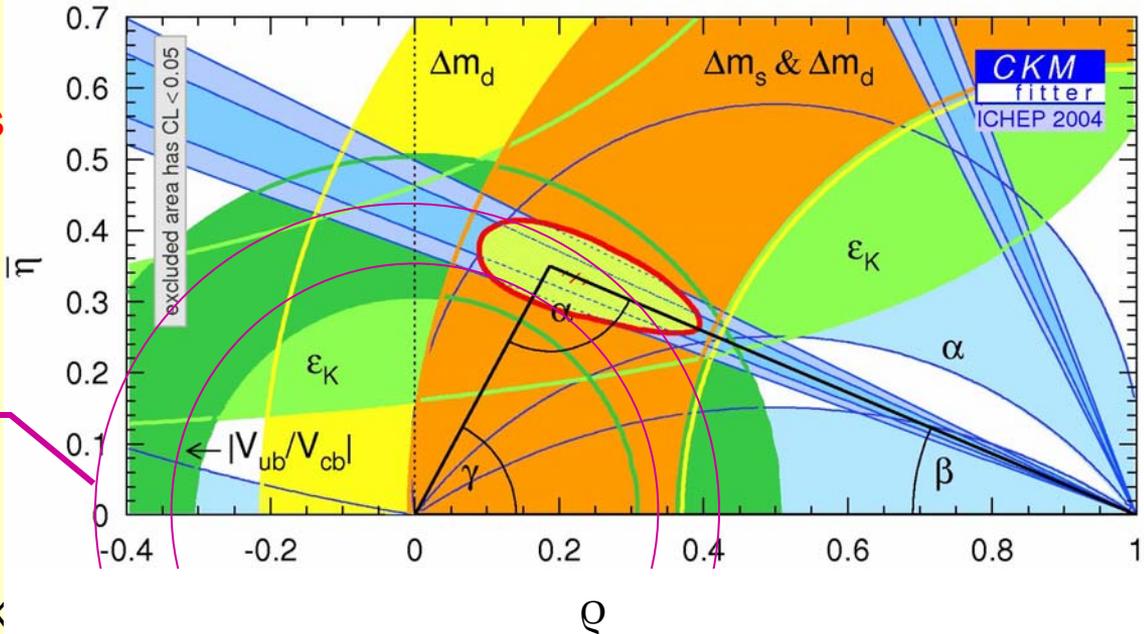
Exclusive $B \rightarrow X_u \ell \nu$

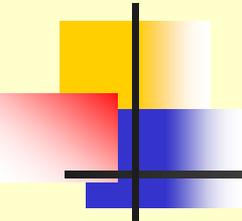
- New unquenched Lattice calculations of $B \rightarrow \pi \ell \nu$ FF now available
- New measurement techniques give much better S/N by reconstructing some/all of the non-signal B
- **Expect improvements soon**
- It will be interesting to compare inclusive and exclusive determinations of $|V_{ub}|$

Conclusion

- **BaBar** measurements on semileptonic decays are improving our knowledge of $|V_{cb}|$ and $|V_{ub}|$:
 - $|V_{cb}|$ from inclusive decays: $\pm 2\%$, HQE validated!
 - $|V_{ub}|$ from inclusive decays: error $< 10\%$, can still improve
- Expect significant progress this year on
 - Inclusive $b \rightarrow u \ell \nu$ decays
 - Exclusive $B \rightarrow X_u \ell \nu$ decays

$|V_{ub}|/|V_{cb}|$ band ($\pm 2\sigma$)
corresponding to $\sigma=5\%$





Backup Slides

Performance snapshot

- Tracking: $[\sigma(p_t)/p_t]^2 = (.0013 p_t)^2 + .0045$
- Ecal: $\sigma_E = 3\%$ at 1 GeV, 4.5% at 0.1 GeV
- PID: control samples used to evaluate ϵ and fake rate

