P214 Midterm Practice Problems (note that these are a little bit harder than the problems on the actual midterm will be, but are very good practice for them)

- 1. Show that, if you have a 15 volt battery, it is *not* possible to exceed the power rating of a $\frac{1}{4}$ watt resistor of resistance greater than 1 k Ω (no matter how you connect it).
- 2. (A quite hard [especially parts b) d)] but good problem!) Let's say that, instead of a voltage source (like a battery) or a constant-current source, we have a constant-*power* source. A constant-power source will do whatever it can to make sure that the voltage across its terminals, *multiplied by* the current it provides, is kept at a constant value (say, for example, 10 watts, or alternatively 100 milliwatts, etc). We know that the symbols for a voltage source and for a current source are as follows:

Voltage source:
$$\frac{\bot}{T}$$
 Current source:

Let us let the symbol for a constant-power source be:

Power source:

And let's say we have the following circuit:



- a) Find the voltage V_A , as a function of P, R_1 , R_2 , and R_{load} .
- b) If we decide to "formally" define the Thevenin equivalent voltage V_{EQ} , and Thevenin equivalent resistance R_{EQ} , as: 1) $V_{EQ} = V_A$ " = V_A in both of the circuits below and above respectively when taking the limit that $R_{\text{load}} \rightarrow \infty$, and 2) $R_{EQ} = R_{\text{load}}((V_{EQ}/V_A) 1) = R_{\text{load}}((V_{EQ}/V_A) 1)$ in both of the circuits above and below respectively when taking the limit that $R_{\text{load}} \ll \infty$, and 2) $R_{EQ} = R_{\text{load}}((V_{EQ}/V_A) 1) = R_{\text{load}}((V_{EQ}/V_A) 1)$ in both of the circuits above and below respectively when taking the limit that $R_{\text{load}} \ll R_{EQ}$, then find the Thevenin equivalents V_{EQ} and R_{EQ} as functions of P, R_1 , and R_2 .



c) If we decide to "formally" define the Norton equivalent current I_{EQ} , and Norton equivalent resistance R_{EQ} , as: 1) $I_{EQ} = V_A / R_{\text{load}} = V_A / R_{\text{load}}$ in both of the circuits below and above respectively when taking the limit that $R_{\text{load}} \ll R_{EQ}$, and 2) $R_{EQ} = V_A / I_{EQ} =$

 V_A'/I_{EQ} in both of the circuits above and below respectively when taking the limit that $R_{\text{load}} \rightarrow \infty$, then find the Norton equivalents I_{EQ} and R_{EQ} as functions of P, R_1 , and R_2 .



- d) Does the Thevenin equivalent resistance R_{EQ} equal the Norton equivalent resistance R_{EQ} in your calculations above? Does $V_{EQ} = I_{EQ}R_{EQ}$, where R_{EQ} is the Thevenin equivalent resistance above?
- 3. At time t = 0, someone closes the switch of the circuit below. If we define the rise time of the circuit to be the time the circuit takes to go from 10% to 90% of its final value, show that the rise time of this circuit equals 2.2*RC*.



4. Bugg problems 1.10.3, 1.10.6, 1.10.7, 1.10.9, 2.10.7, 2.10.8, 2.10.12, 2.10.13, 3.12.6, 3.12.13.