

# Global Fit for Branching Fractions and Form Factor Slope of $B \rightarrow D^{(*)} \ell \nu$ Decays

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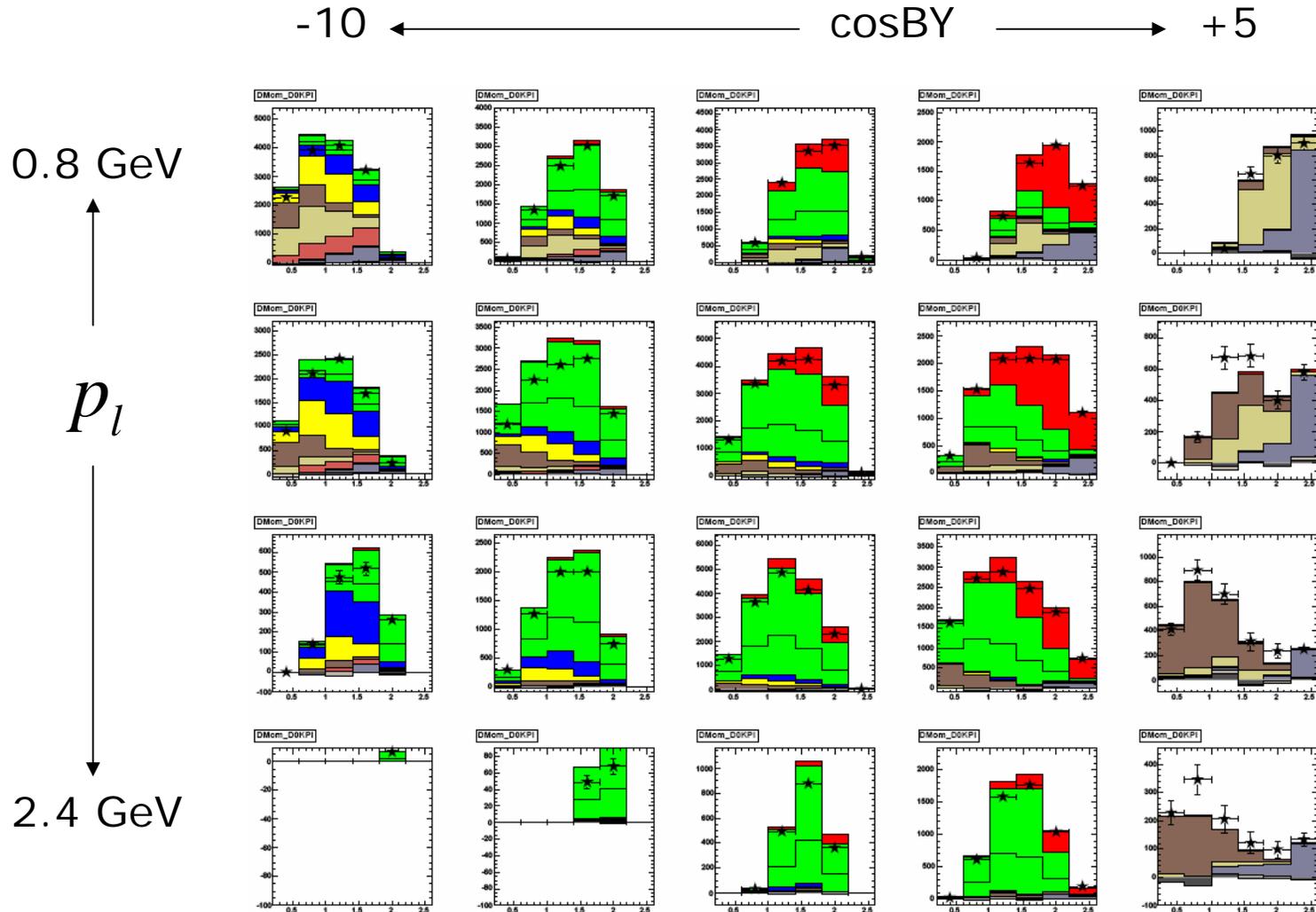
Fitting method and FF re-weighting

# Changes since last September

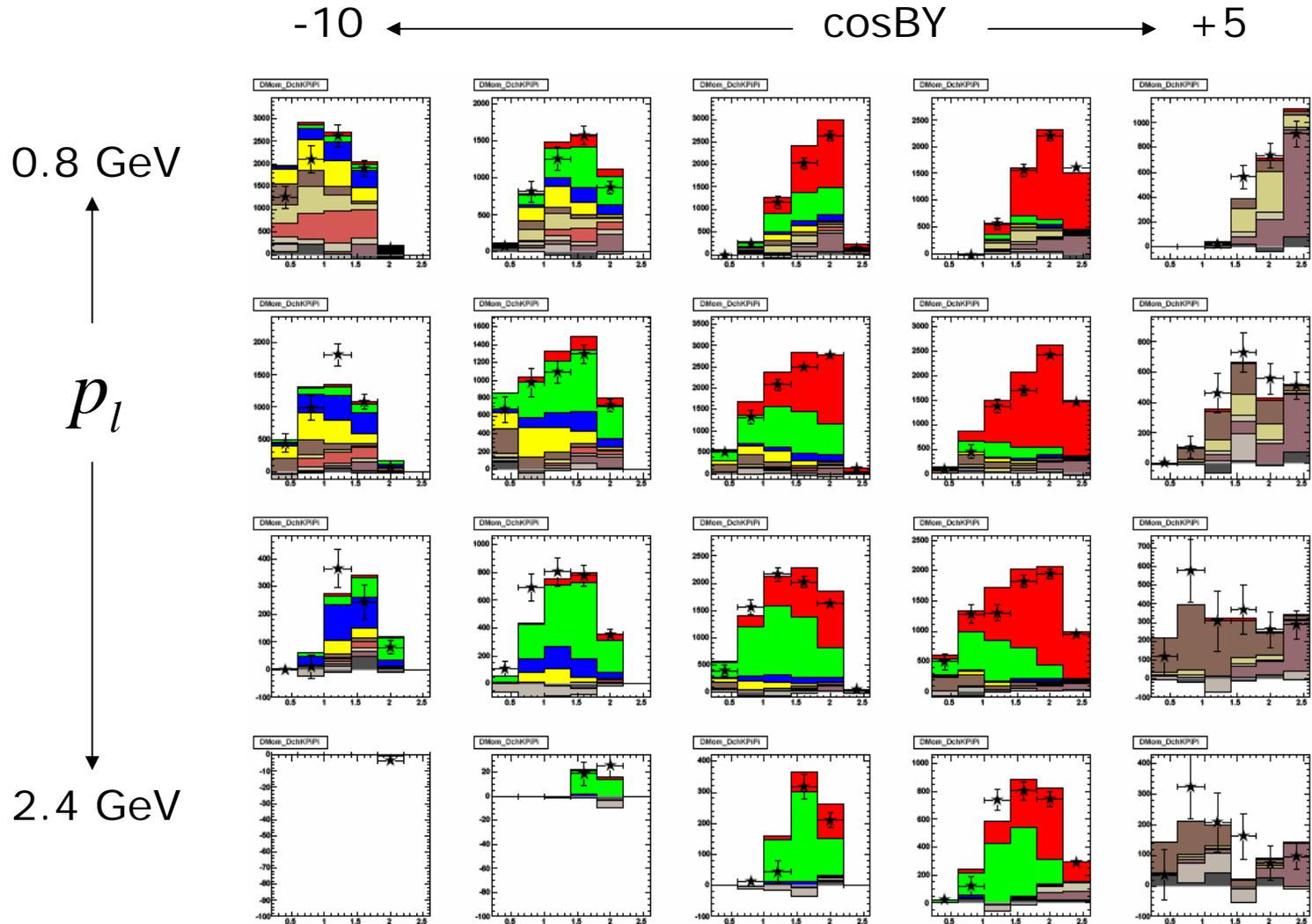
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- Use OffPeak data instead of ccbar, uds and tautau MC
- Use Run2 (59.4 fb<sup>-1</sup> of data) to get more OffPeak statistics.
- Fixed relative size of background components to get more realistic results.
- D\*\* FF re-weighting

# Bin by bin plot : D0 momentum



# Bin by bin plot : D+ momentum



# Fitting Method

- Binned chi-square fitting

$$\chi^2 = \sum_{i=bin}^{D^0} \frac{\left( N_i^{\text{OnPeak data}} - N_i^{\text{OffPeak data}} - \sum C N_i^{B\bar{B}MC} \right)^2}{\left( \sigma_i^{\text{OnPeak data}} \right)^2 + \left( \sigma_i^{\text{OffPeak data}} \right)^2 + \sum \left( C \sigma_i^{B\bar{B}MC} \right)^2} + \sum_{i=bin}^{D^+} \frac{\left( N_i^{\text{OnPeak data}} - N_i^{\text{OffPeak data}} - \sum C N_i^{B\bar{B}MC} \right)^2}{\left( \sigma_i^{\text{OnPeak data}} \right)^2 + \left( \sigma_i^{\text{OffPeak data}} \right)^2 + \sum \left( C \sigma_i^{B\bar{B}MC} \right)^2}$$

- $N_i^{B\bar{B}MC}$  : expected number of candidates from  $B\bar{B}$  MC.
- $C$  : consists of branching fractions.
- 8 signal modes and 4 background modes (combinatorial background is almost zero after sideband subtraction)
- Isospin symmetry for  $B$  decays.

# $N_i^{B\bar{B}MC}$ and $C$ : Signal

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- $B \rightarrow D l \nu$  :  $C = \text{BF}(B \rightarrow D l \nu)$
- $B \rightarrow D^* l \nu$  :  $C = \text{BF}(B \rightarrow D^* l \nu)$
- $B \rightarrow D^{**} l \nu$  &  $B \rightarrow D^{(*)} \pi l \nu$  :  $\text{BF}(B \rightarrow \text{Other } l \nu)$ 
  - $B \rightarrow D_0^* l \nu$  :  $C = f_1 \times \text{B}(B \rightarrow \text{Other } l \nu)$
  - $B \rightarrow D_1 l \nu$  :  $C = f_2 \times \text{B}(B \rightarrow \text{Other } l \nu)$
  - $B \rightarrow D_1' l \nu$  :  $C = f_3 \times \text{B}(B \rightarrow \text{Other } l \nu)$
  - $B \rightarrow D_2^* l \nu$  :  $C = f_4 \times \text{B}(B \rightarrow \text{Other } l \nu)$
  - $B \rightarrow D \pi l \nu$  :  $C = f_5 \times \text{B}(B \rightarrow \text{Other } l \nu)$
  - $B \rightarrow D^* \pi l \nu$  :  $C = f_6 \times \text{B}(B \rightarrow \text{Other } l \nu)$
- 4 parameters to be determined :
  - 3 BFs and  $B \rightarrow D l \nu$  FF slope.
- Factors  $f_1 - f_6$  are fixed.

# $N_i^{B\bar{B}MC}$ and $C$ : Background

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- Uncorrelated (=  $D$  and  $l$  from different  $B$ ) :  $C = f_a * f_0$
- Uncorrelated (=  $D$  and  $l$  from different  $B$ ) and  $l$  not directly from  $B$  (i.e.  $B \rightarrow D \rightarrow Xl$ ) :  $C = f_b * f_0$
- Cascade (=  $l$  not directly from  $B$ ) and correlated (i.e.  $B \rightarrow D \bar{D}, \bar{D} \rightarrow Xl$ ) :  $C = f_c * f_0$
- Fake lepton = misidentified  $l$  :  $C = f_d * f_0$
- Combinatorial background is almost zero after  $D$  mass sideband subtraction.
- $f_0(D^0)$  and  $f_0(D^+)$  are floated in the fit independently.
- $f_a = f_b = f_c = f_d = 1$ .

# $f_{+0}$ and $c_{+0}$

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- We also included  $f_{+0}$  in the fit with Gaussian constraint

$$f_{+0} = \frac{\text{BR}(e^+ e^- \rightarrow B^+ B^-)}{\text{BR}(e^+ e^- \rightarrow B^0 \overline{B^0})}$$

- To account for possible simulation difference of  $D^0$  and  $D^+$ , we multiplied  $C$  of  $D^+$  MC by  $c_{+0}$  (floated with Gaussian constraint). This also allows the fit to adjust for the uncertainties in the relative BFs for  $D^0 \rightarrow K \pi$  and  $D^+ \rightarrow K \pi \pi$ , and should make us less sensitive to uncertainties from tracking efficiency.

# Form Factor Re-weighting

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- $B \rightarrow D/\nu$  : ISGW2  $\rightarrow$  HQFT

$$h_+(w) = h_+(1)[1 - \rho_D^2(w-1)]$$

- $B \rightarrow D^*/\nu$  : HQET
  - Babar measurement of  $R_1$ ,  $R_2$  and slope  $\rho^2$ .
- $B \rightarrow D^{**}/\nu$  : ISGW2  $\rightarrow$  HQET
  - Based on LLSW paper (Leibovich, Ligeti, Stewart and Wise, PRD57(1998)308, hep-ph/9705467)
- Normalization
  - Total decay rate should stay same

$$\Gamma = \int \frac{d\Gamma(\text{old FF})}{dq^2} dq^2 = R_N \int \frac{d\Gamma(\text{new FF})}{dw} dw$$

- $R_N$  is the normalization factor

# $D_0^*$ FF re-weighting

- Differential decay rate (see also p.14)

$$\frac{d\Gamma}{dw} = \frac{G_F^2 |V_{cb}|^2 m_B^5}{48\pi^3} r^3 (w^2 - 1)^{3/2} F(w)$$

$$F(w) = [(1+r)g_+ - (1-r)g_-]^2$$

- ISGW2 model

$$F(q^2) = R^2 [(1+r)u_+(q^2) - (1-r)u_-(q^2)]^2$$

- LLSW model

$$F(w) = \zeta^2(1) [s_0 + (w-1)s_1]$$

slope ↙

$$s_0 = (1-r)^2 + 3(1-r^2)(\varepsilon_b + \varepsilon_c)(\bar{\Lambda}^* - \bar{\Lambda})$$

$$s_1 = 2(1-r)^2 \hat{\zeta}'$$

# $D_1'$ FF re-weighting

- Differential decay rate (see also p.14)

$$\frac{d\Gamma}{dw} = \frac{G_F^2 |V_{cb}|^2 m_B^5}{48\pi^3} r^3 (w^2 - 1)^{1/2} F(w)$$

$$F(w) = [(w-r)g_{V_1} + (w^2-1)(g_{V_3} + rg_{V_2})]^2 + 2(1-2rw+r^2)[g_{V_1}^2 + (w^2-1)g_A^2]$$

- ISGW2 model

$$g_A \rightarrow Rm_B(1-r)q, \quad g_{V_1} \rightarrow \frac{2}{Rm_B(1-r)}l, \quad g_{V_3} + rg_{V_2} \rightarrow Rm_B(1-r)c_+$$

- LLSW model

$$F(w) = \zeta^2(1) \{ [s_0 + 2(1-2rw+r^2)t_0] \\ + (w-1)[s_1 + 2(1-2rw+r^2)t_1] + (w-1)^2[s_2 + 2(1-2rw+r^2)t_2] \}$$

$$s_0 = (1-r)^2(\varepsilon_c - 3\varepsilon_b)^2(\bar{\Lambda}^* - \bar{\Lambda})^2, \quad t_0 = (\varepsilon_c - 3\varepsilon_b)^2(\bar{\Lambda}^* - \bar{\Lambda})^2$$

$$s_1 = -2(1-r^2)(\varepsilon_c - 3\varepsilon_b)(\bar{\Lambda}^* - \bar{\Lambda}), \quad t_1 = 2 + 4(\varepsilon_c - 3\varepsilon_b)(\bar{\Lambda}^* - \bar{\Lambda})$$

$$s_2 = (1+r^2), \quad t_2 = 2(1+2\hat{\zeta}')$$

# $D_1$ FF re-weighting

- Differential decay rate (see also p.14)

$$\frac{d\Gamma}{dw} = \frac{G_F^2 |V_{cb}|^2 m_B^5}{48\pi^3} r^3 (w^2 - 1)^{1/2} F(w)$$

$$F(w) = [(w-r)f_{V_1} + (w^2 - 1)(f_{V_3} + rf_{V_2})]^2 + 2(1 - 2rw + r^2)[f_{V_1}^2 + (w^2 - 1)f_A^2]$$

- ISGW2 model

$$f_A \rightarrow Rm_B(1-r)v, \quad f_{V_1} \rightarrow \frac{2}{Rm_B(1-r)}r, \quad f_{V_3} + rf_{V_2} \rightarrow Rm_B(1-r)s_+$$

- LLSW model

$$F(w) = \frac{1}{3}\tau^2(1)\{[s_0 + 2(1 - 2rw + r^2)t_0] \\ + (w-1)[s_1 + 2(1 - 2rw + r^2)t_1] + (w-1)^2[s_2 + 2(1 - 2rw + r^2)t_2]\}$$

$$s_0 = 32(1-r)^2 \varepsilon_c^2 (\bar{\Lambda}' - \bar{\Lambda})^2, \quad t_0 = 32\varepsilon_c^2 (\bar{\Lambda}' - \bar{\Lambda})^2$$

$$s_1 = 32(1-r^2)\varepsilon_c (\bar{\Lambda}' - \bar{\Lambda}), \quad t_1 = 4 + 32\varepsilon_c (\bar{\Lambda}' - \bar{\Lambda})$$

$$s_2 = 8(1+r)^2, \quad t_2 = 8(1+\hat{\tau}')$$

# $D_2^*$ FF re-weighting

- Differential decay rate (see also p.14)

$$\frac{d\Gamma}{dw} = \frac{G_F^2 |V_{cb}|^2 m_B^5}{48\pi^3} r^3 (w^2 - 1)^{3/2} F(w)$$

$$F(w) = \frac{2}{3} [(w-r)k_{A_1} + (w^2-1)(k_{A_3} + rk_{A_2})]^2 + 2(1-2rw+r^2)[k_{A_1}^2 + (w^2-1)k_V^2]$$

- ISGW2 model

$$k_V \rightarrow Rm_B(1-r)h, \quad k_{A_1} \rightarrow \frac{2}{Rm_B(1-r)}k, \quad k_{A_3} + rk_{A_2} \rightarrow Rm_B(1-r)b_+$$

- LLSW model

$$F(w) = \frac{1}{3} \tau^2(1) \{ [2s_0 + 3(1-2rw+r^2)t_0] + (w-1)[2s_1 + 3(1-2rw+r^2)t_1] \}$$

$$s_0 = 4(1-r)^2, \quad t_0 = 4$$

$$s_1 = 4(1-r)^2(1+2\hat{\tau}'), \quad t_1 = 2(3+4\hat{\tau}')$$

# Numerical Values for LLSW

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$$r = \frac{m_D}{m_B}, \quad R = \frac{2\sqrt{m_B m_D}}{m_B + m_D}, \quad \varepsilon_c = \frac{1}{2m_c}, \quad \varepsilon_b = \frac{1}{2m_b}$$

$$\tau(1) = 0.71, \quad \zeta(1) = \frac{2}{\sqrt{3}} \tau(1),$$

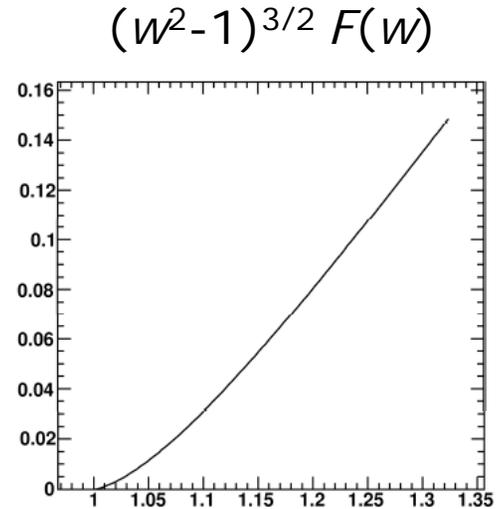
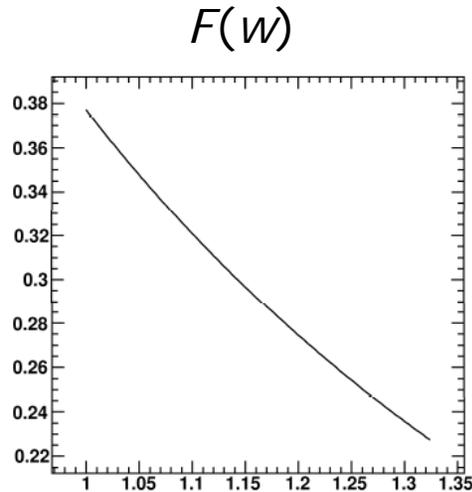
$$\hat{\tau}' = -1.5, \quad \hat{\zeta}' = \frac{1}{2} + \hat{\tau}' = -1$$

$$\varepsilon_c(\bar{\Lambda}' - \bar{\Lambda}) = 0.14, \quad (\bar{\Lambda}' - \bar{\Lambda} = 0.39\text{GeV})$$

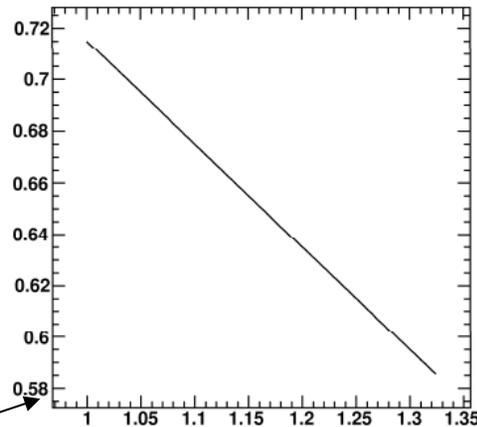
$$\varepsilon_c + \varepsilon_b = 0.92\text{GeV}^{-1}, \quad \varepsilon_c - 3\varepsilon_b = 0.05\text{GeV}^{-1}, \quad \bar{\Lambda}^* - \bar{\Lambda} = 0.35\text{GeV}$$

# $D_0^*$ FF plots : $w$ dependence

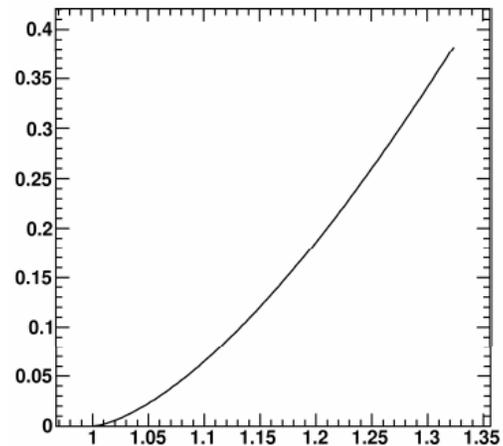
ISGW2



LLSW

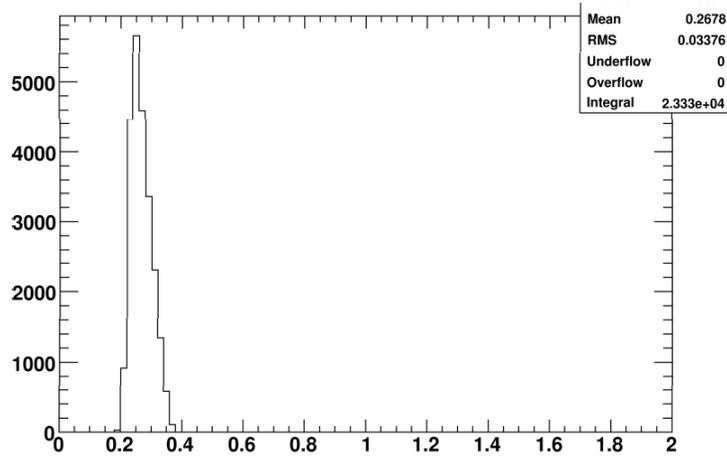


not zero

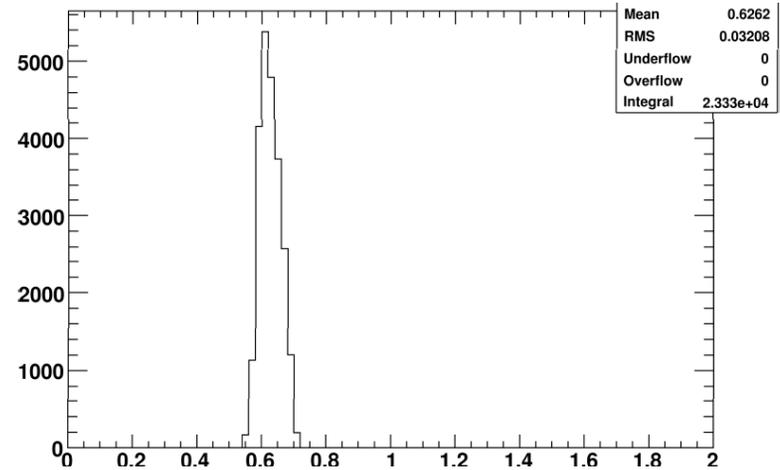


# $D_0^*$ FF plots : FF and weights

ISGW2  $F(w)$

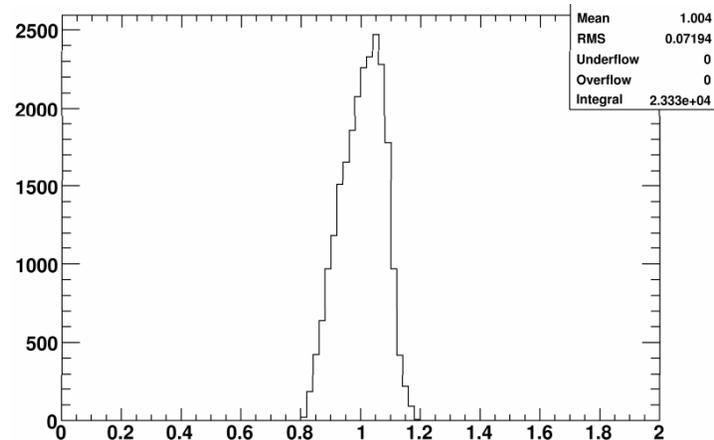


LLSW  $F(w)$

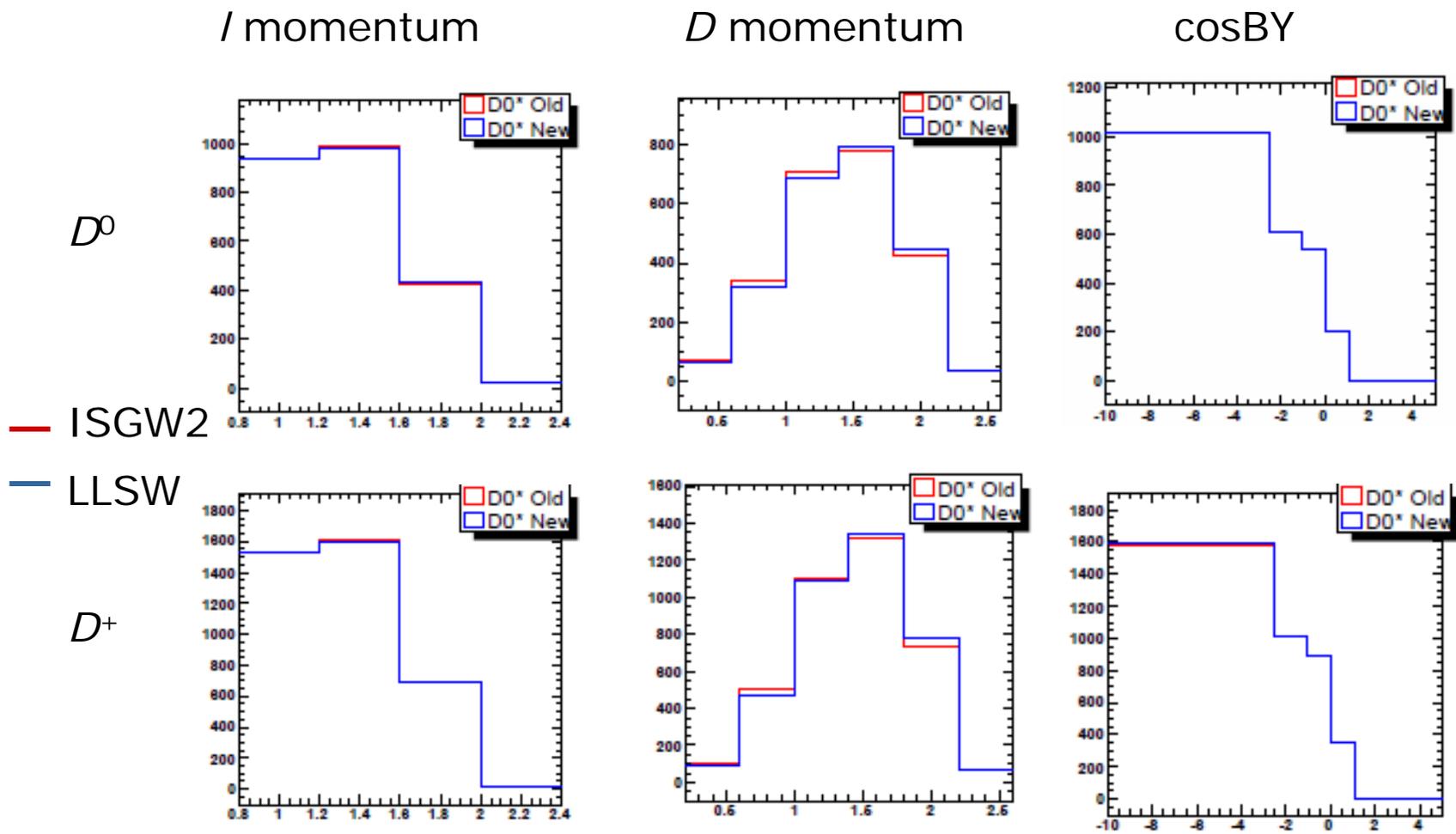


Weight

$$R_N = 0.425$$



# $D_0^*$ kinematic variables

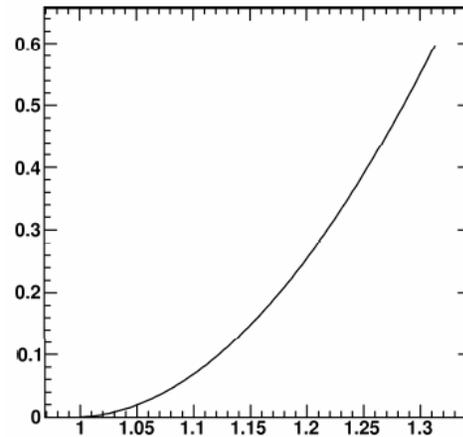


Normalized to OnPeak luminosity.

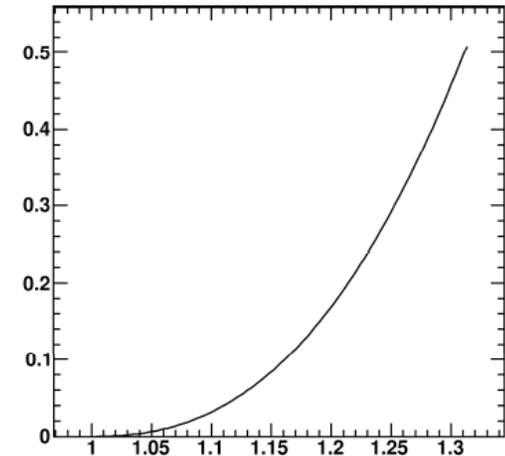
# $D_1'$ FF plots : $w$ dependence

ISGW2

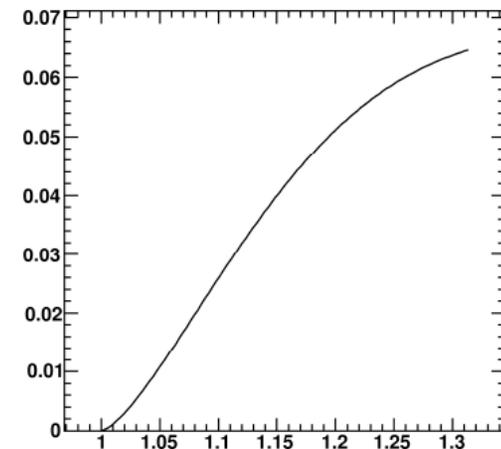
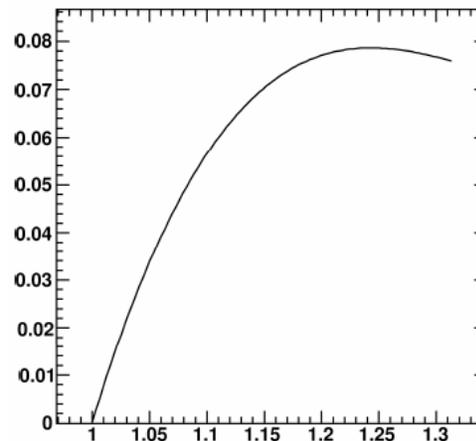
$F(w)$



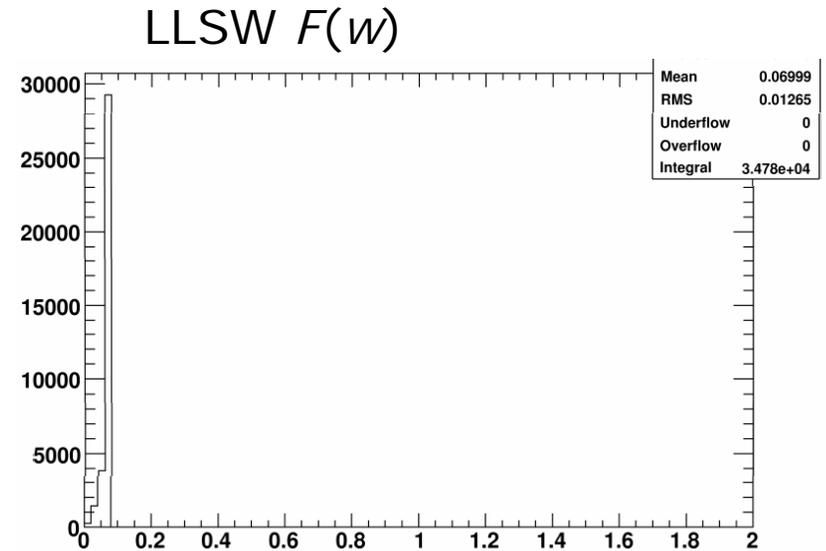
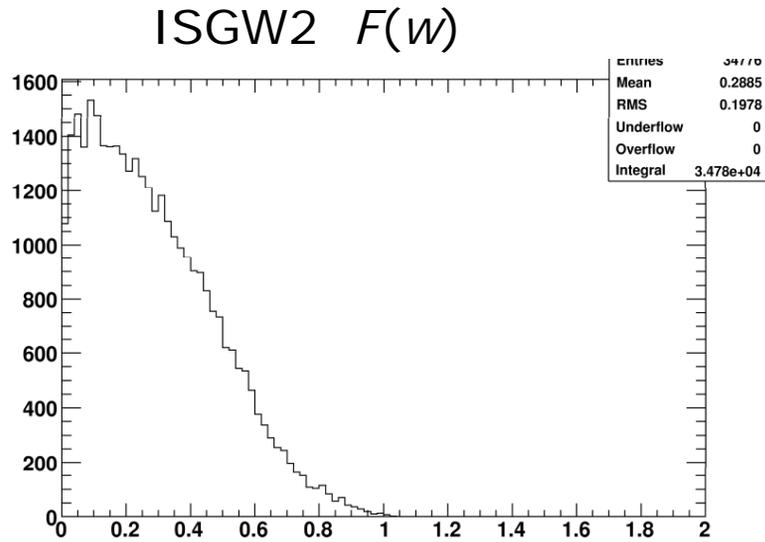
$(w^2-1)^{1/2} F(w)$



LLSW

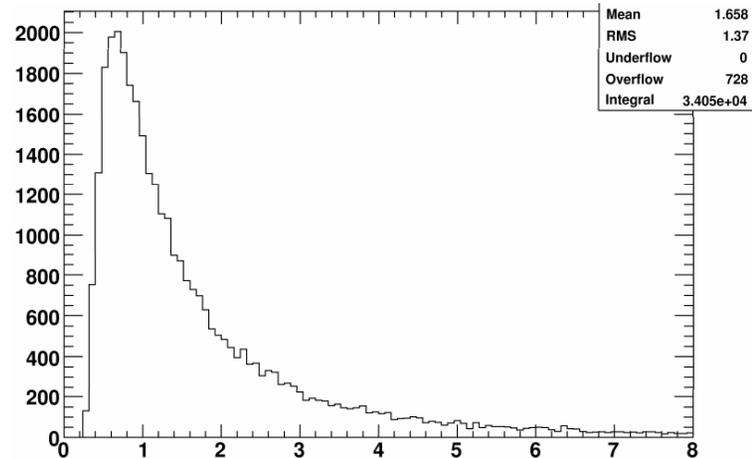


# $D_1'$ FF plots : FF and weights

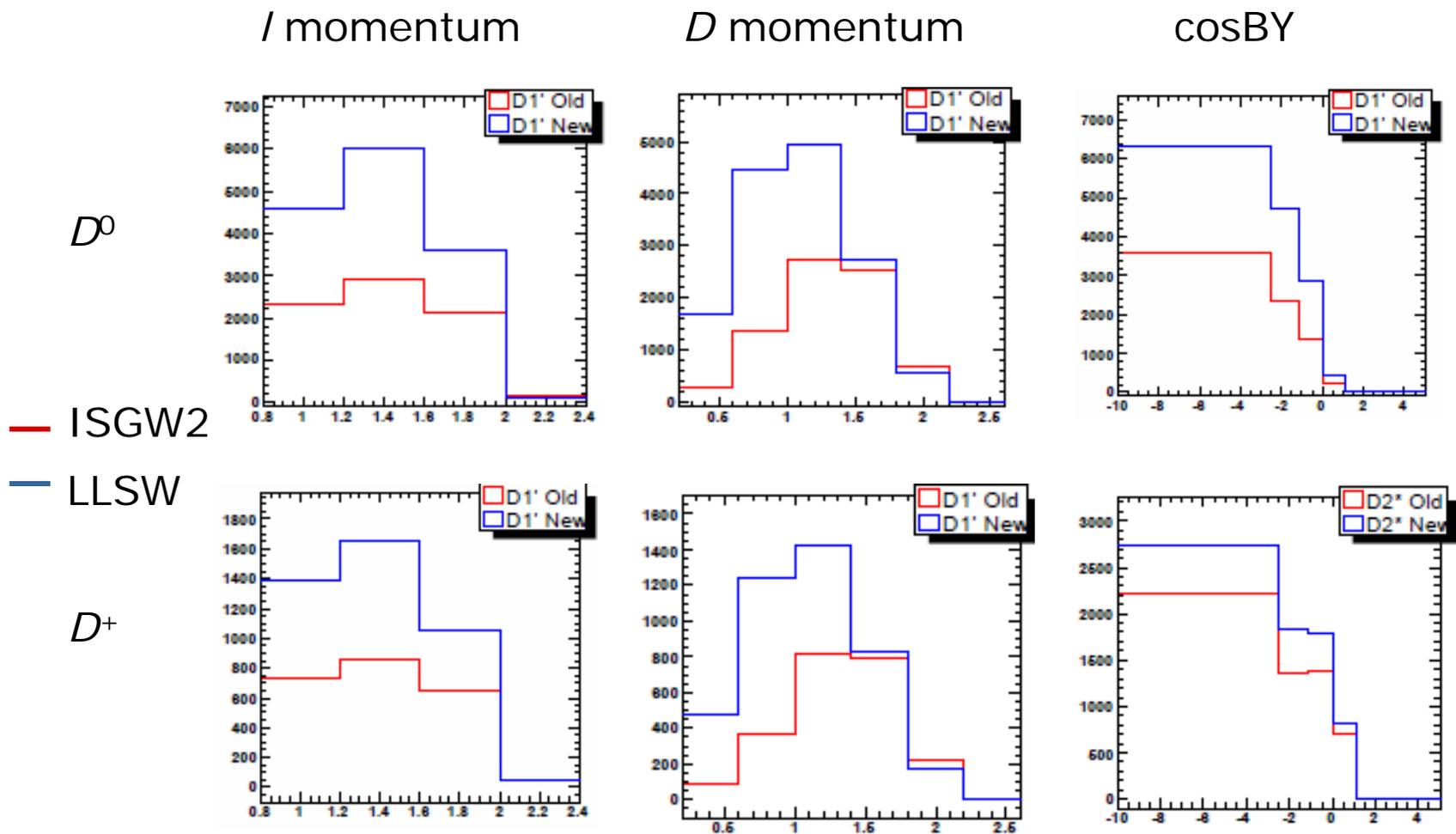


Weight

$$R_N = 4.00$$



# $D_1'$ kinematic variables

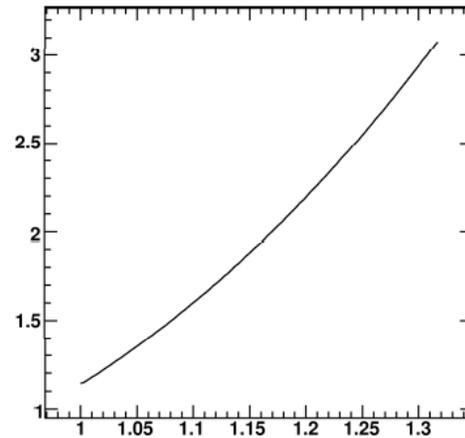


Normalized to OnPeak luminosity.

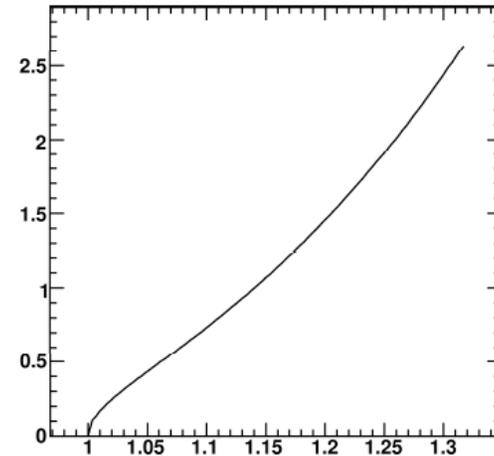
# $D_1$ FF plots : $w$ dependence

ISGW2

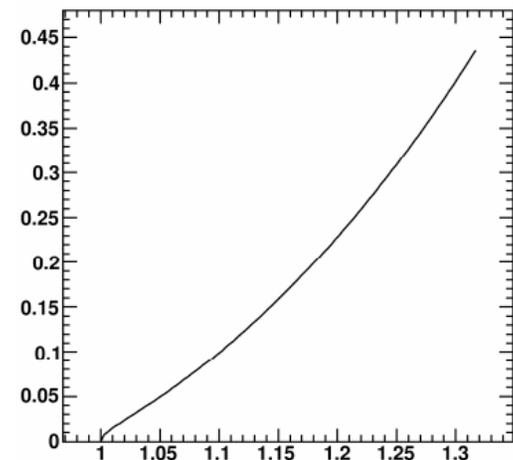
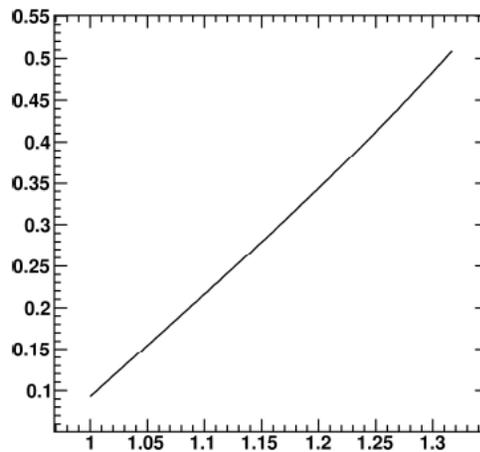
$F(w)$



$(w^2-1)^{1/2} F(w)$

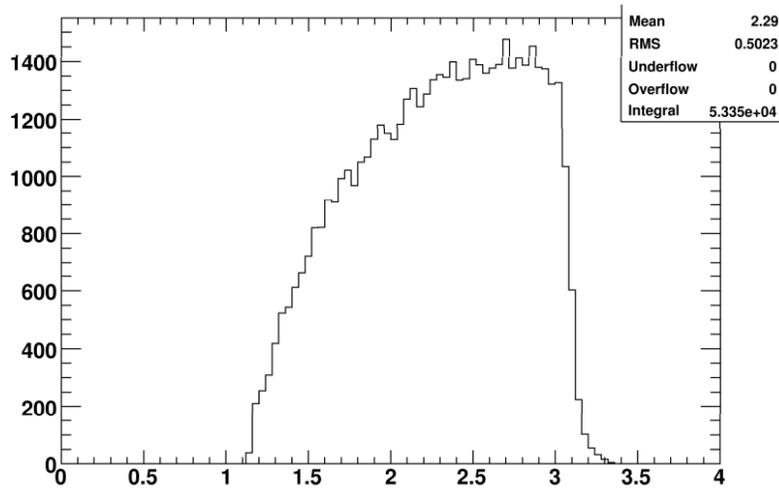


LLSW

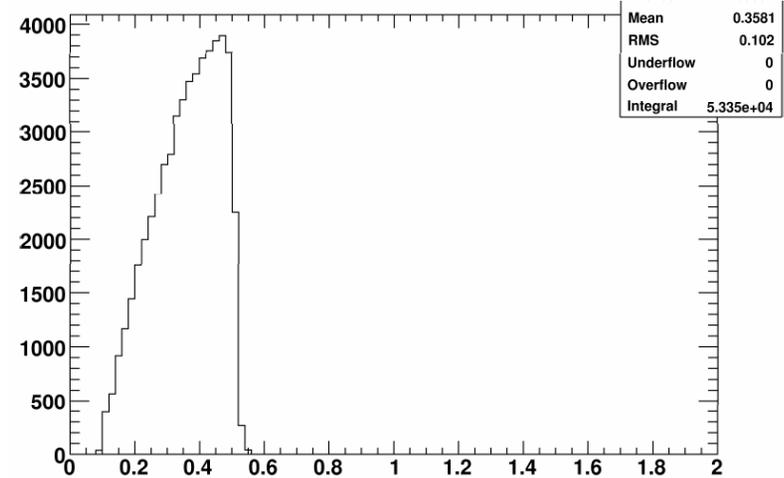


# $D_1$ FF plots : FF and weights

ISGW2  $F(w)$

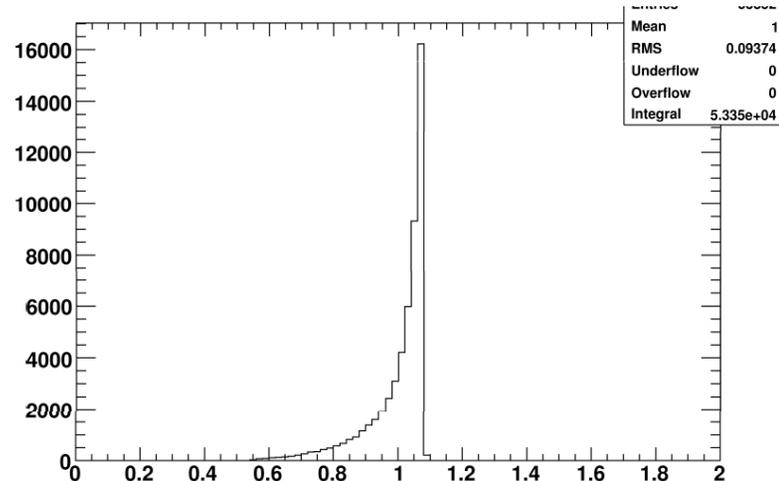


LLSW  $F(w)$

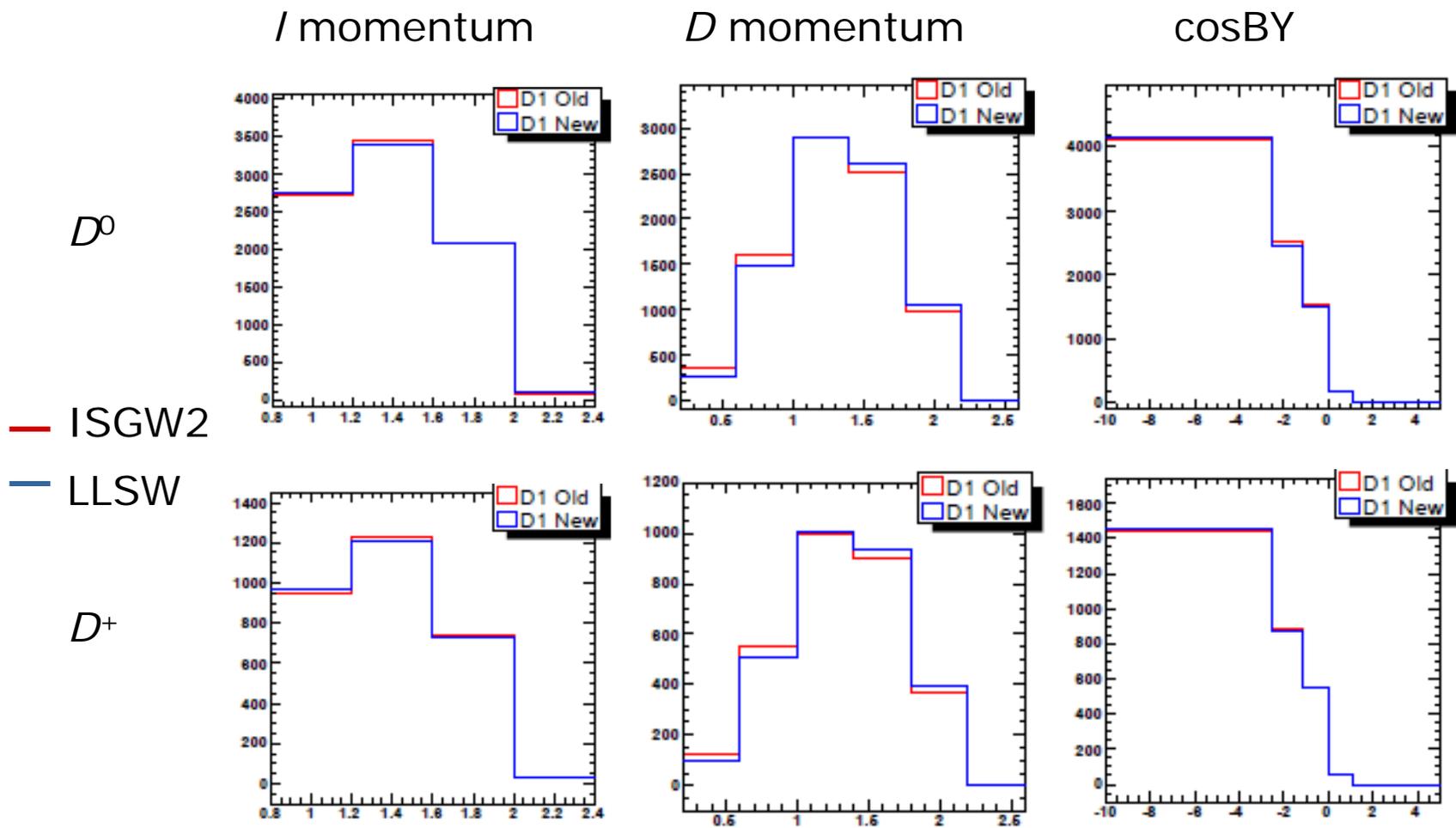


Weight

$$R_N = 6.51$$



# $D_1$ kinematic variables

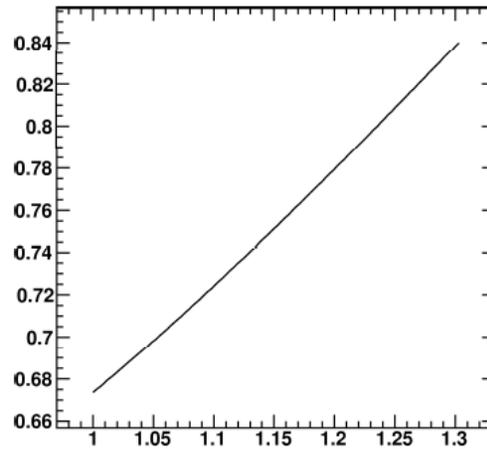


Normalized to OnPeak luminosity.

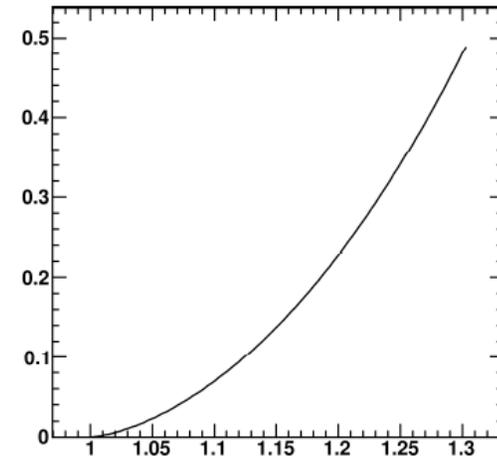
# $D_2^*$ FF plots : $w$ dependence

ISGW2

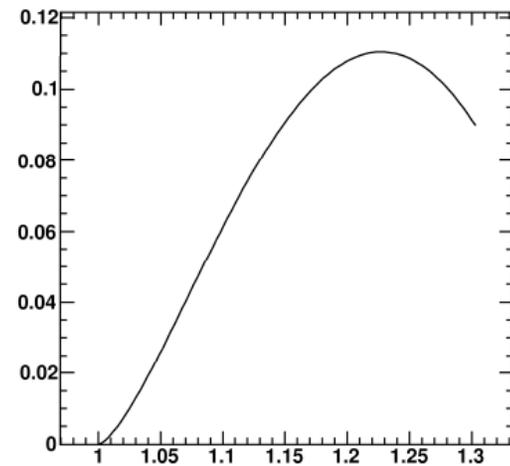
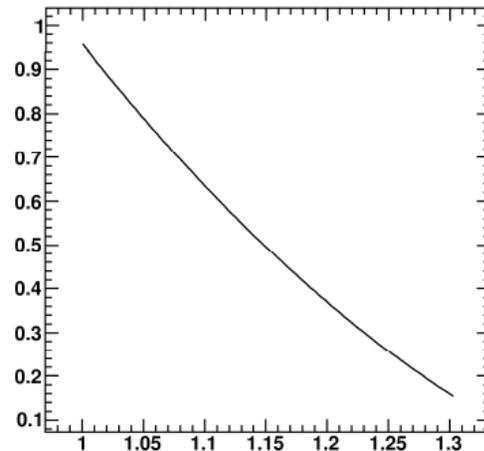
$F(w)$



$(w^2-1)^{3/2} F(w)$

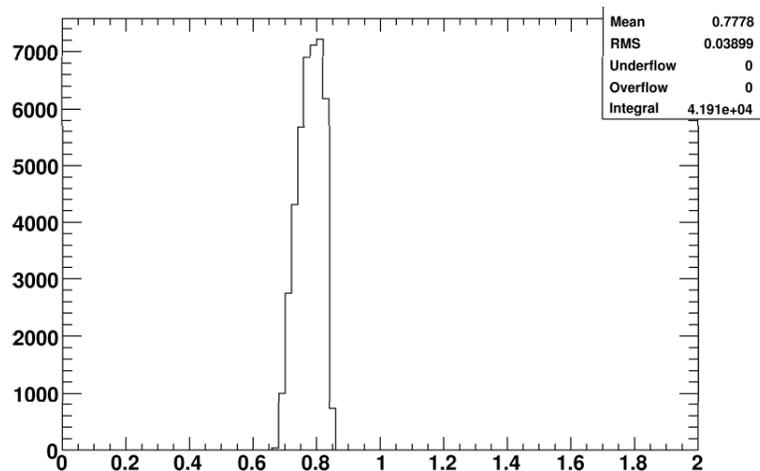


LLSW

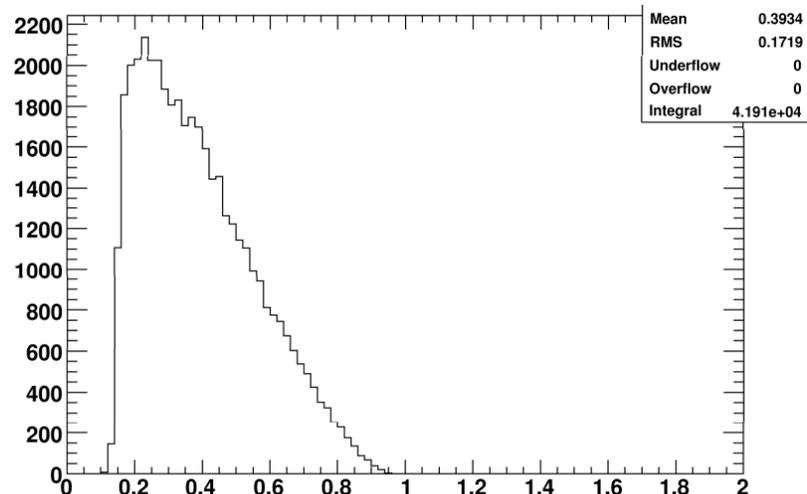


# $D_2^*$ FF plots : FF and weights

ISGW2  $F(w)$

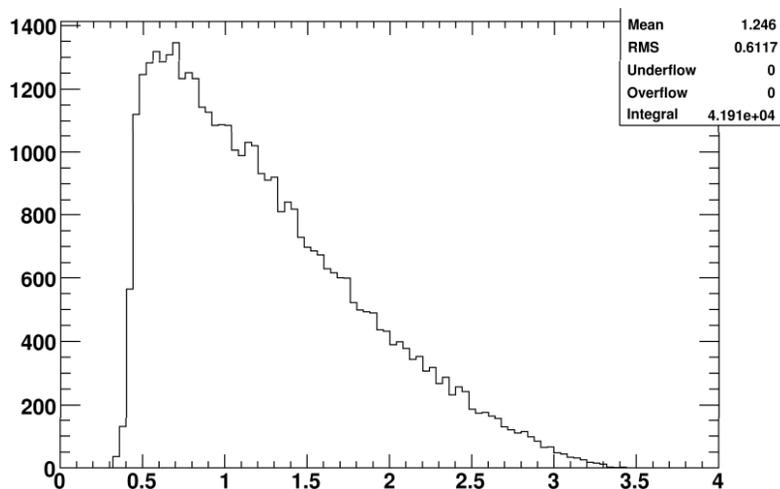


LLSW  $F(w)$

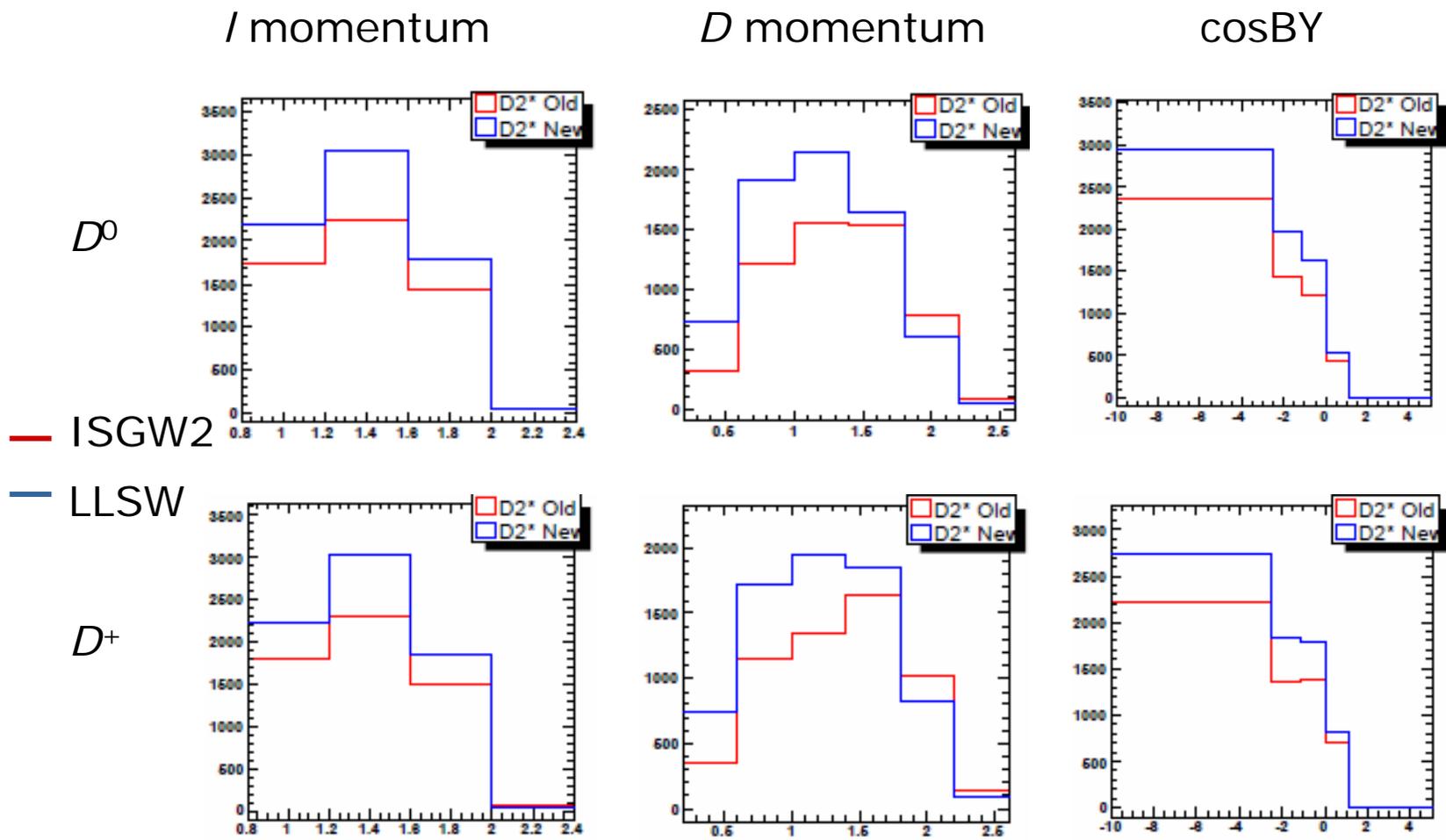


Weight

$$R_N = 2.40$$



# $D_2^*$ kinematic variables



Normalized to OnPeak luminosity.

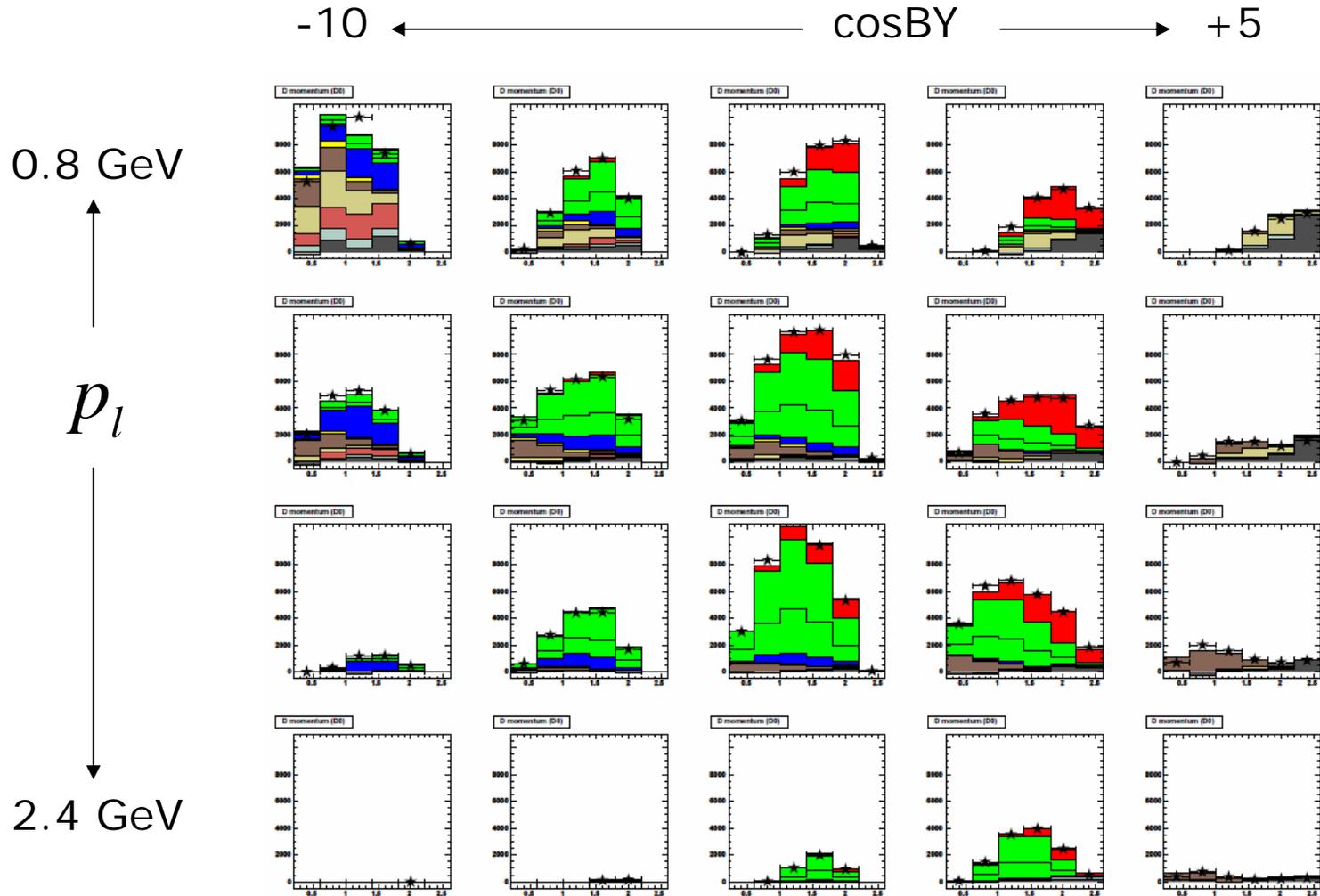
# Fit Result (Run2 only)

$B^+$	ISGW2	LLSW
Slope	1.4959 $\pm$ 0.0049	1.4524 $\pm$ 0.0054
BR( $Dl\nu$ )	0.0282 $\pm$ 0.0011 (4.0%)	0.0295 $\pm$ 0.0011
BR( $D^*l\nu$ )	0.0591 $\pm$ 0.0015 (2.5%)	0.0610 $\pm$ 0.0015
BR(Other)	0.0221 $\pm$ 0.0011 (4.9 %)	0.0189 $\pm$ 0.0009

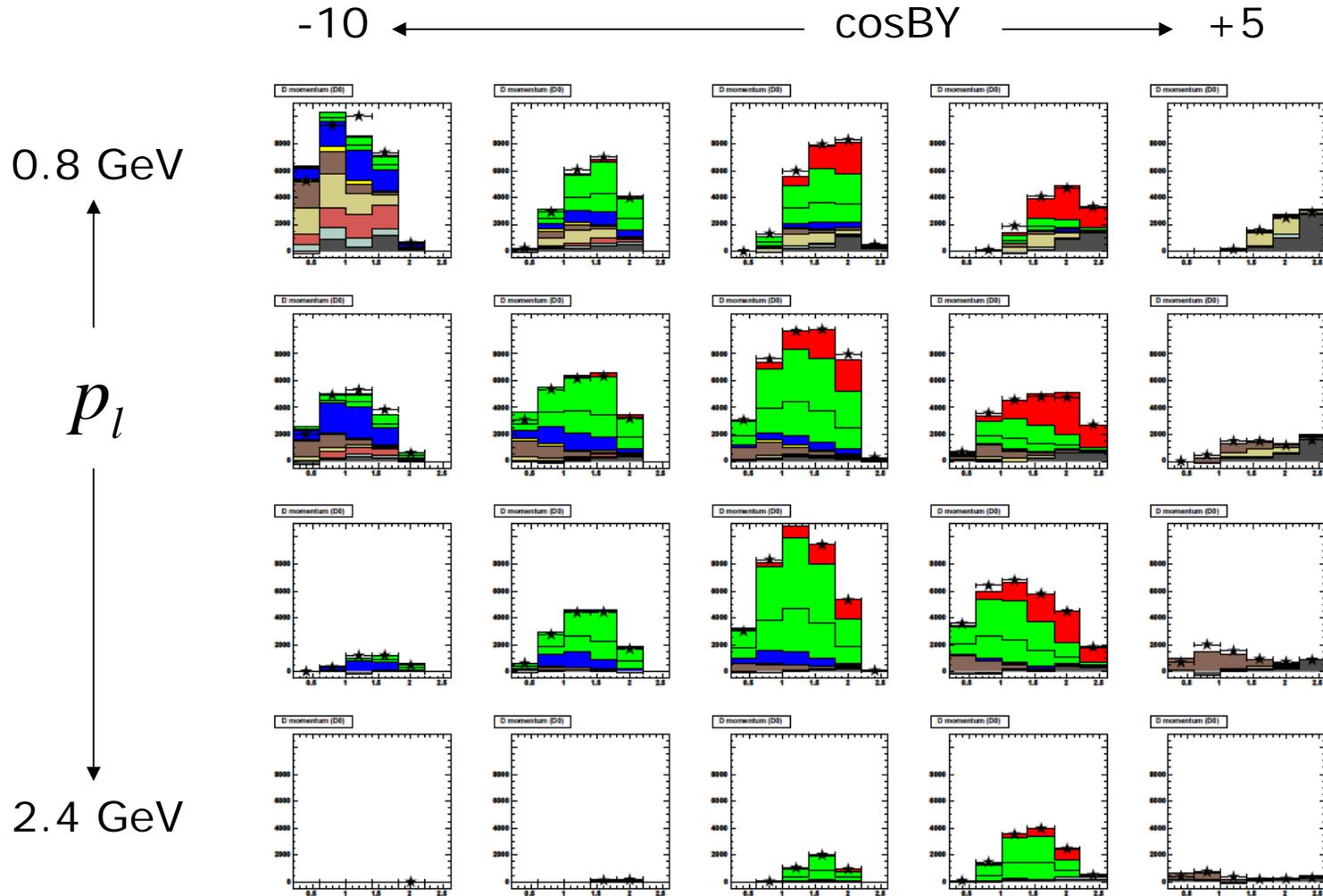
Difference between ISGW2 and LLSW is 3-5% (14% for BR(Other)).  
Similar size to statistical uncertainty.

Chi-square did not improve much (346  $\rightarrow$  334, ndof=180).

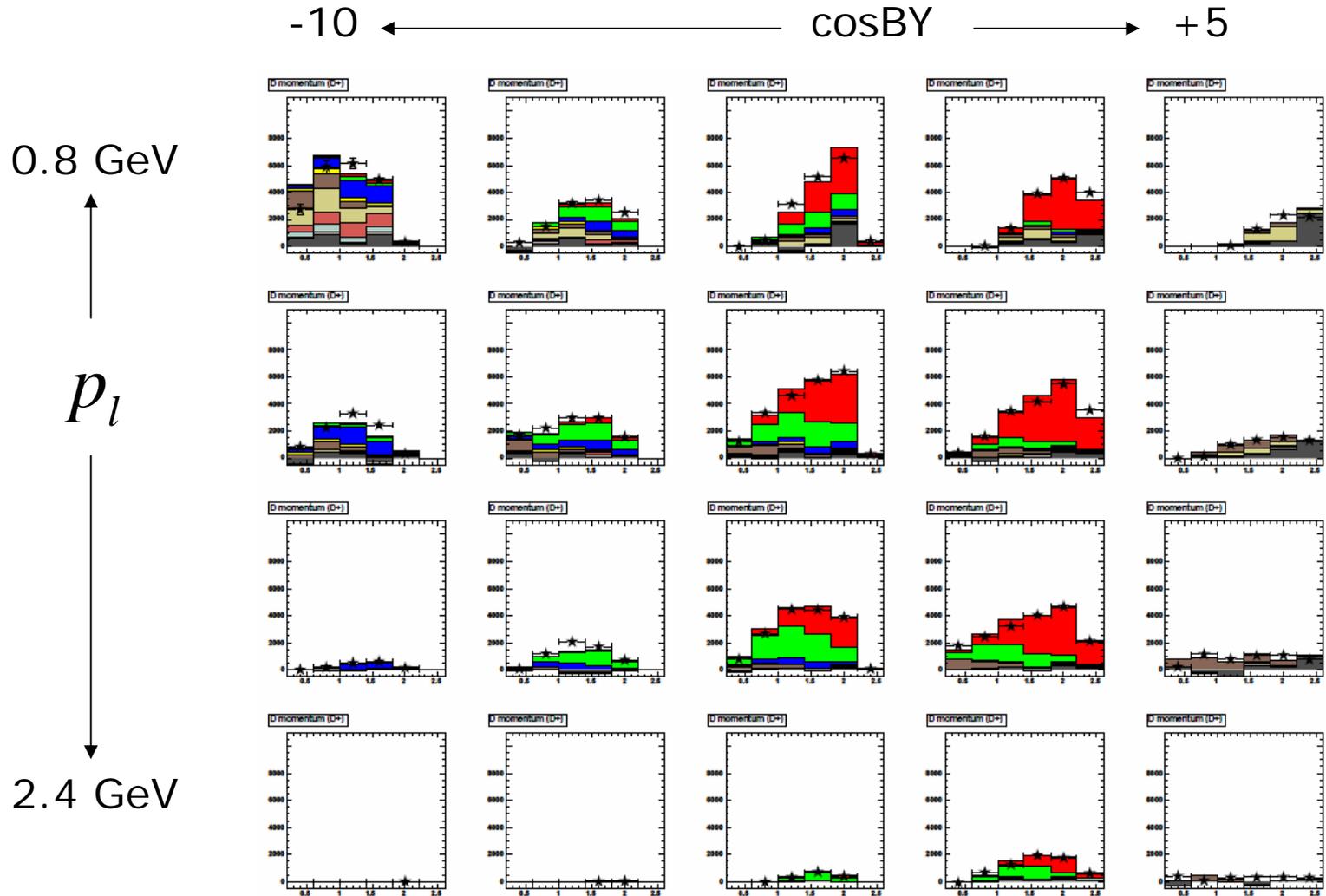
# ISGW2 : $D^0$ momentum



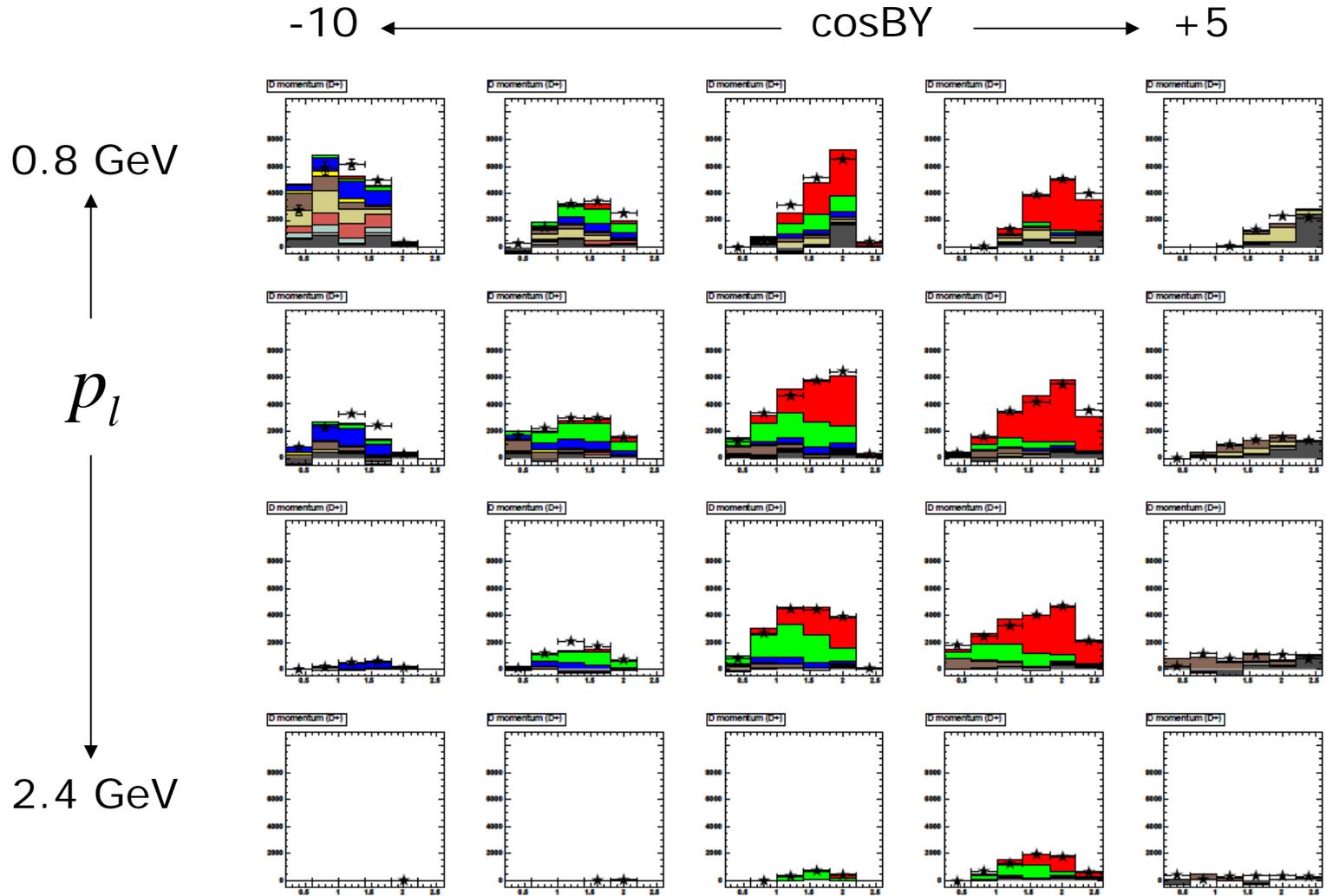
# LLSW : $D^0$ momentum



# ISGW2 : $D^+$ momentum



# LLSW : $D^+$ momentum



# Summary

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- A lot of questions on LLSW model:
  - Plots look as those should do?
  - Best formula?
  - Appropriate numerical values?
  - How much those values can be varied?
- 3-5% effect on fit results
  - Current fit code may have a small bug....
- BAD1586 V2 will be ready soon.
  - Details of FF and re-weighting are in the BAD.