

Global Fit for BF and FF in $B \rightarrow D \ell \nu$ decay

Fitting status

Motivation

- Determine $B \rightarrow D\ell\nu$ and $B \rightarrow D^*\ell\nu$ Branching Fractions (BF)
 - Hoping to solve problems like
 - $B^0 \rightarrow D^{*-}\ell^+\nu$ BF disagreement between experiments.
 - $B^0 \rightarrow D^*\ell\nu$, $B^+ \rightarrow D^*\ell\nu$ disagreement.
 - Check “Inclusive BF = Sum of Exclusive BF” ?
- Determine $B \rightarrow D\ell\nu$ Form Factor (FF) slope
 - Current uncertainty $\sim 30\%$.

B- \rightarrow Dlnu decay FF and re-weighting

- In B- \rightarrow Dlnu decays, there is one FF:
 - $h+(w) = R*f+(q^2)$
 - $W = (M_B^2 + M_D^2 - q^2)/(2M_B*M_D)$
 - $R = \sqrt{M_B*M_D}/(M_B + M_D)$
- ISGW2 Model and $f+(q^2)$ is used in MC
- HQET
 - $h+(w) = h+(1) [1 - \rho^2 (w - 1)]$
 - $\rho^2 = \text{FF slope}$
- Need to re-weight MC to change FF from ISGW2 to HQET
 - No need to generate new MC
 - We can just re-weight event by event (candidate by candidate) when making MC histograms.

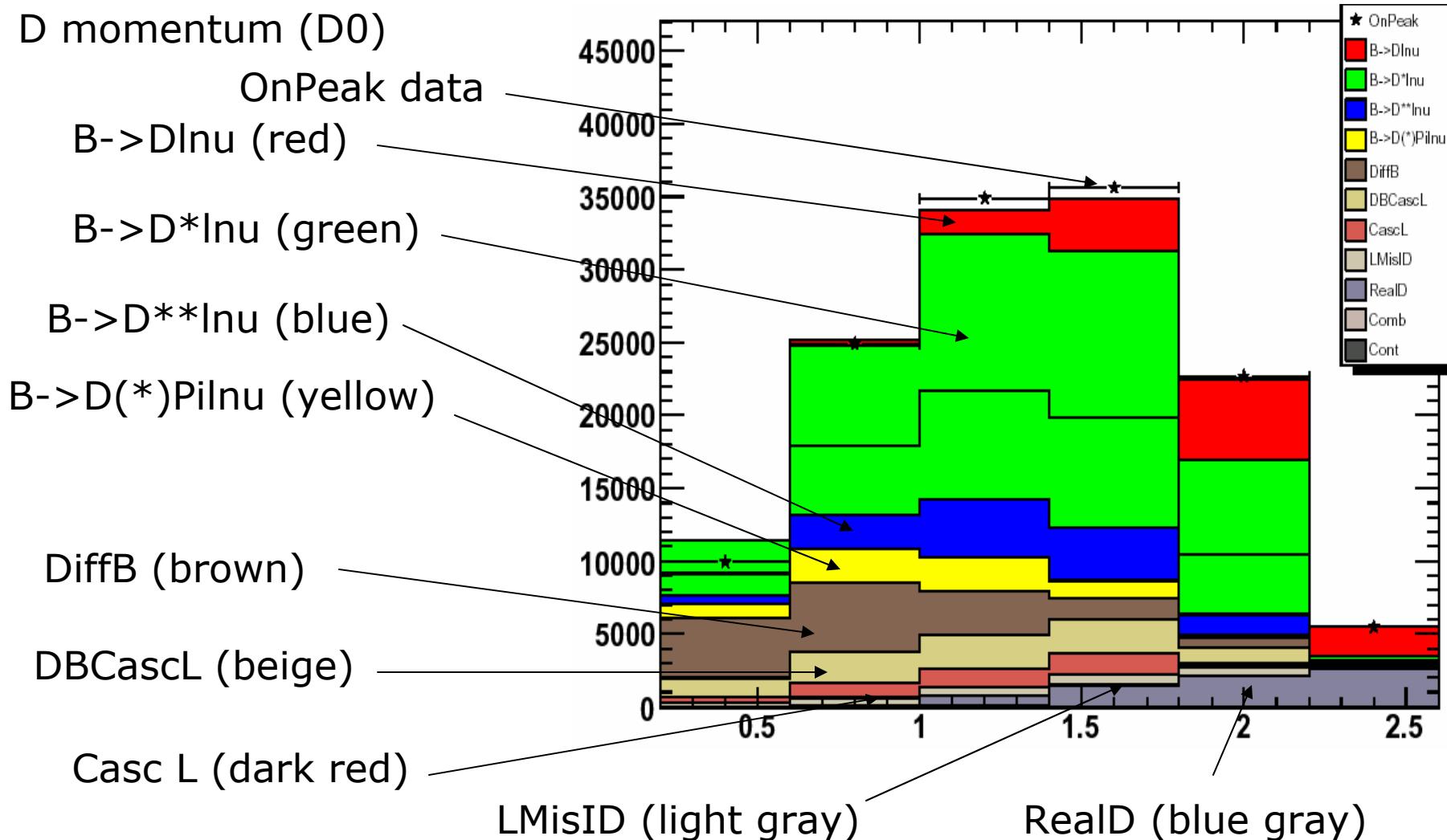
Event Selection

- BToDlnu skim
 - Select events including B->D/D*lnu candidates.
 - In practise, select DI combinations.
- Bhabha veto
 - Reject radiative Bhabha events.
- Kaon selection
 - KMicroNotPion selector
- Vertexing (by TreeFitter)
 - D vertexing probab >0.01
 - B vertexing probab >0.01
- Trust cut
 - $\cos\theta_{Dl-\text{non}Dl} < 0.88$

Signal and background

- Signal
 - $B \rightarrow D \ell \nu$
 - $B \rightarrow D^* \ell \nu$
 - $B \rightarrow D^{**} \ell \nu$
 - $B \rightarrow D(*) \Pi \ell \nu$ (non-resonant)
- Background
 - $\text{DiffB} = D$ and ℓ come from different B . ℓ come directly from B .
 - $\text{DBCascL} = D$ and ℓ come from different B . ℓ come not directly from B ($B \rightarrow D \rightarrow K \ell \nu$).
 - $\text{CascL} = D$ and ℓ come from same B . ℓ does not come directly from B ($B \rightarrow D \rightarrow K \ell \nu$).
 - $\text{LMisID} = \ell$ miss identification.
 - $\text{RealID} = \text{ccbar}$ events with real D .

After sideband subtraction



Method of analysis

- Reconstruct only D^0 and D^+ candidates. All higher D state feeds down to D .
 - $B \rightarrow D l \nu$
 - $B \rightarrow D^* l \nu$, $D^* \rightarrow D X$
 - $B \rightarrow D^{**} l \nu$, $D^{**} \rightarrow D X$
 - $B \rightarrow D \pi l \nu$ (non-resonant)
- Use clean modes $D^0 \rightarrow K \pi$ and $D^+ \rightarrow K \pi \pi$.
- Bin events in 3-D : D momentum, Lepton momentum and $\cos\theta_{B-Dl}$.
- Fit to $B \rightarrow D l \nu$ events.
 - Use MC histograms like PDF (Probability Density Functions)
 - Fit those PDFs to measured data.

Binning

- Lepton momentum bin (4bins):
 - 0.8, 1.2, 1.6, 2.0, 2.4 GeV
- D momentum bin (6 bins):
 - 0.2, 0.6, 1.0, 1.4, 1.8, 2.2, 2.6 GeV
- cosBY bin (5 bins):
 - -10, -2.5, -1.1, 0.0, 1.1, 5
- Total $120 * 2$ (D+ and D0) = 240 bins
 - Use “#evt > 25” bins -> ~187 bins are used
- Run 3 data (30.6 fb⁻¹)
and MC (~100 fb⁻¹ of BBbar and ~50 fb⁻¹ of others)
was used.

Binned chi-square fitting

$$\chi^2 = \sum_i^{D^0} \frac{\left(N_i^{data} - \sum_j C_j N_{ij}^{MC} \right)^2}{\left(\sigma_i^{data} \right)^2 + \sum_j \left(C_j \sigma_{ij}^{MC} \right)^2} + \sum_i^{D^+} \frac{\left(N_i^{data} - \sum_j C_j N_{ij}^{MC} \right)^2}{\left(\sigma_i^{data} \right)^2 + \sum_j \left(C_j \sigma_{ij}^{MC} \right)^2}$$

- Predicted number of events ($N^{\{MC\}}$)
 - Tracking efficiency and PID corrected.
 - Luminosity normalised to data.
 - Form factor (FF) re-weighted.
- Coefficients (C) include
 - Branching fractions (BF)
 - Ratios like
 - $f_{+0} = f_{+-}/f_{00}$ (production rates ratio),
 - $t_{0+} = t_{00}/t_{+-}$ (life time ratio),
 - c_{+0} = MC modeling difference in D^0 and D^+
- Isospin symmetry is assumed for $B \rightarrow D l \nu_X$ decays (not for $D^{*-} \rightarrow D$).
- Use TMINUIT to minimize chi-square.

Binned chi-square fitting

- Free parameters
 - Branching fractions
 - $\text{BF}(B \rightarrow D\ell\nu)$
 - $\text{BF}(B \rightarrow D^*\ell\nu)$
 - $\text{BF}(\text{Total } B \rightarrow D^{**}\ell\nu)$
 - $\text{BF}(\text{Total } B \rightarrow D(^*)\text{Pi}\ell\nu)$
 - Background components
 - 5 components each for D^0 and D^+ = 10 parameters
 - Other constants
 - f_{+0}
 - c_{+0}
- Used constants
 - D^{**} constants :
 $D^0*/D^+ = 0.88, D^{*'}_1/D^+_1 = 1.61, D^{*}_2/D^+_1 = 0.77$
 - $D(^*)\text{Pi}$ constants : $D\text{pi}/D^*\text{Pi} = 0.66$

Validation of fitting

- Split Run3 MC into two halves.
- Use first half as a fake data.
- Fit this fake data by the second half of MC
- Results : looks good
 - Number of bins = 179, number of parameters = 16,
number of dof = $190 - 18 = 163$
Chi-square = 154
 - Fitted branching fractions are consistent with the values used in the MC
 - $B \rightarrow D l \nu$: 0.02073 ± 0.00089 (0.0210 in SP6)
 - $B \rightarrow D^* l \nu$: 0.0565 ± 0.0016 (0.0560 in SP6)
 - $B \rightarrow D^{**} l \nu$: 0.01557 ± 0.00099 (0.0150 in SP6)
 - $B \rightarrow D^* P l \nu$: 0.0111 ± 0.0015 (0.0120 in SP6)

First results of fitting to Data

- Branching fractions
 - $\text{BF}(B \rightarrow D \ell \nu) = 0.0250 \pm 0.0012$ (4.8 %)
 - $\text{BF}(B \rightarrow D^* \ell \nu) = 0.0614 \pm 0.0019$ (3.2 %)
 - $\text{BF}(B \rightarrow D^{**} \ell \nu) = 0.0109 \pm 0.0014$ (13 %)
 - $\text{BF}(B \rightarrow D(^*) \ell \nu) = 0.0139 \pm 0.0018$ (13 %)
- $D \ell \nu$ FF slope
 - $\rho^2 = 1.459 \pm 0.053$ (3.6 %)
- Float background components separately for D^0 and D^+
- Float f_{+0} and c_{+0} . Gaussian constraints on f_{+0} and c_{D^+0}
- No significant correlation between variables.

$B^+/B^0 \rightarrow D^* \ell \nu$ BF

- Relax isospin symmetry constraint on $B^+ \rightarrow D^* \ell \nu$ and $B^0 \rightarrow D^* \ell \nu$
- Result
 - $BF(B^+ \rightarrow D^* \ell \nu) = 0.0585 \pm 0.0037$
 - $BF(B^0 \rightarrow D^* \ell \nu) = 0.0602 \pm 0.0049$
- Isospin symmetry holds!
 - Using B^+/B^0 lifetime ratio $t_{+0} = 1.071$
 - $(0.0602 \pm 0.0049) * 1.071 = 0.0645 \pm 0.0052$

Problems of the fitting results

- $\text{\#dof} = \text{\#bins} - \text{\#parameters} = 187 - 17 = 170$
Chi-square = 307 : not really good.
- Some of fitted background components are far from 1.
 - $\text{LMisID}(D^0) = 0.175464 \pm 0.224735$
 - $\text{DiffB}(D^+) = 0.591759 \pm 0.119507$
 - $\text{DBCascL}(D^+) = 0.564115 \pm 0.155397$

Next steps

- Improve chi-square
 - Vary $B \rightarrow D^* \ell \nu$ FF parameters.
 - Re-weight $D^{**} \ell \nu$ MC
 - Re-weight $D(^*) \ell \nu$ (non-resonant) MC.
- Review constraints on $D^{**} \ell \nu$ and $D(^*) \ell \nu$ BFs in the fit.
- Review backgrounds.